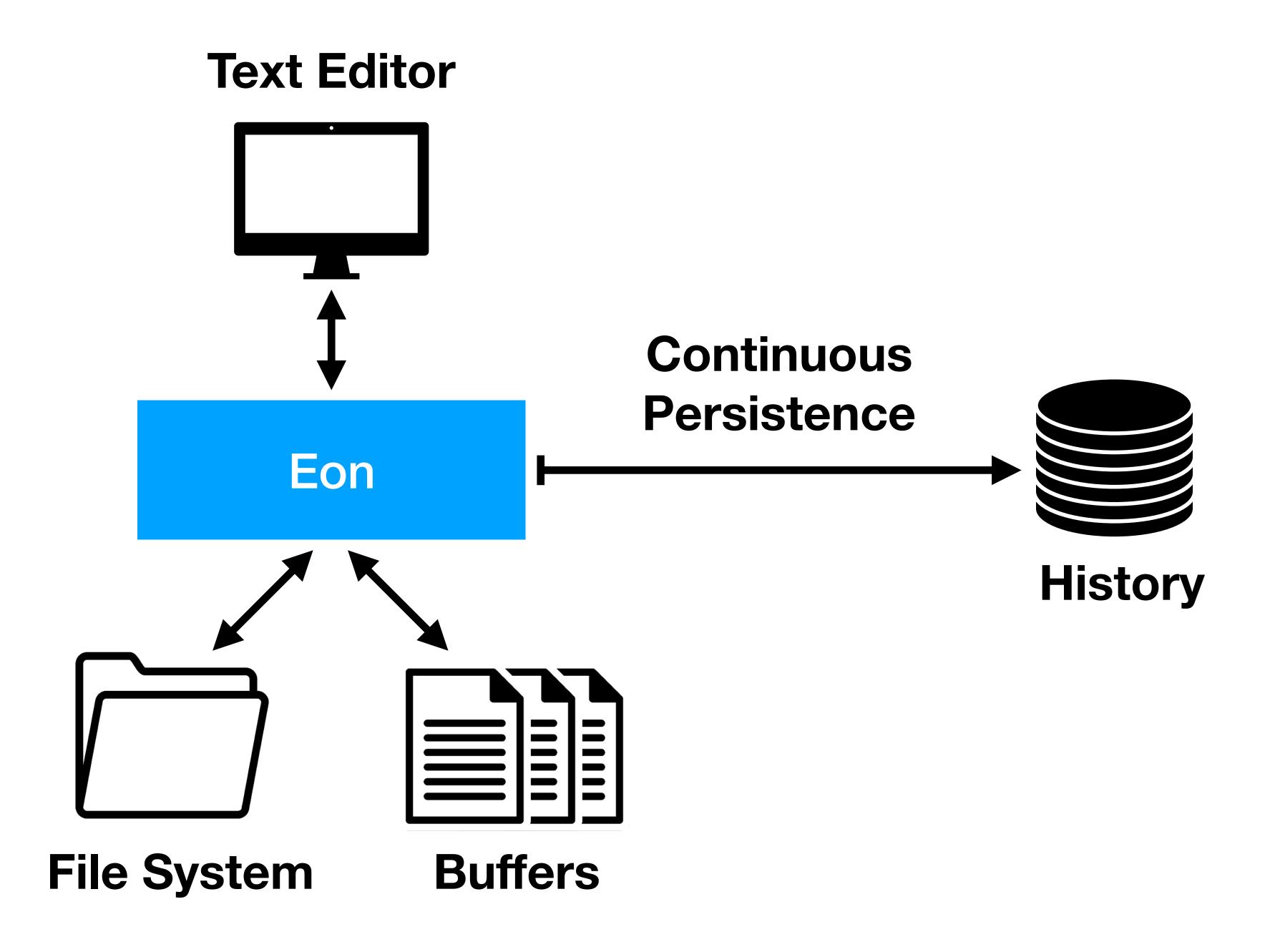
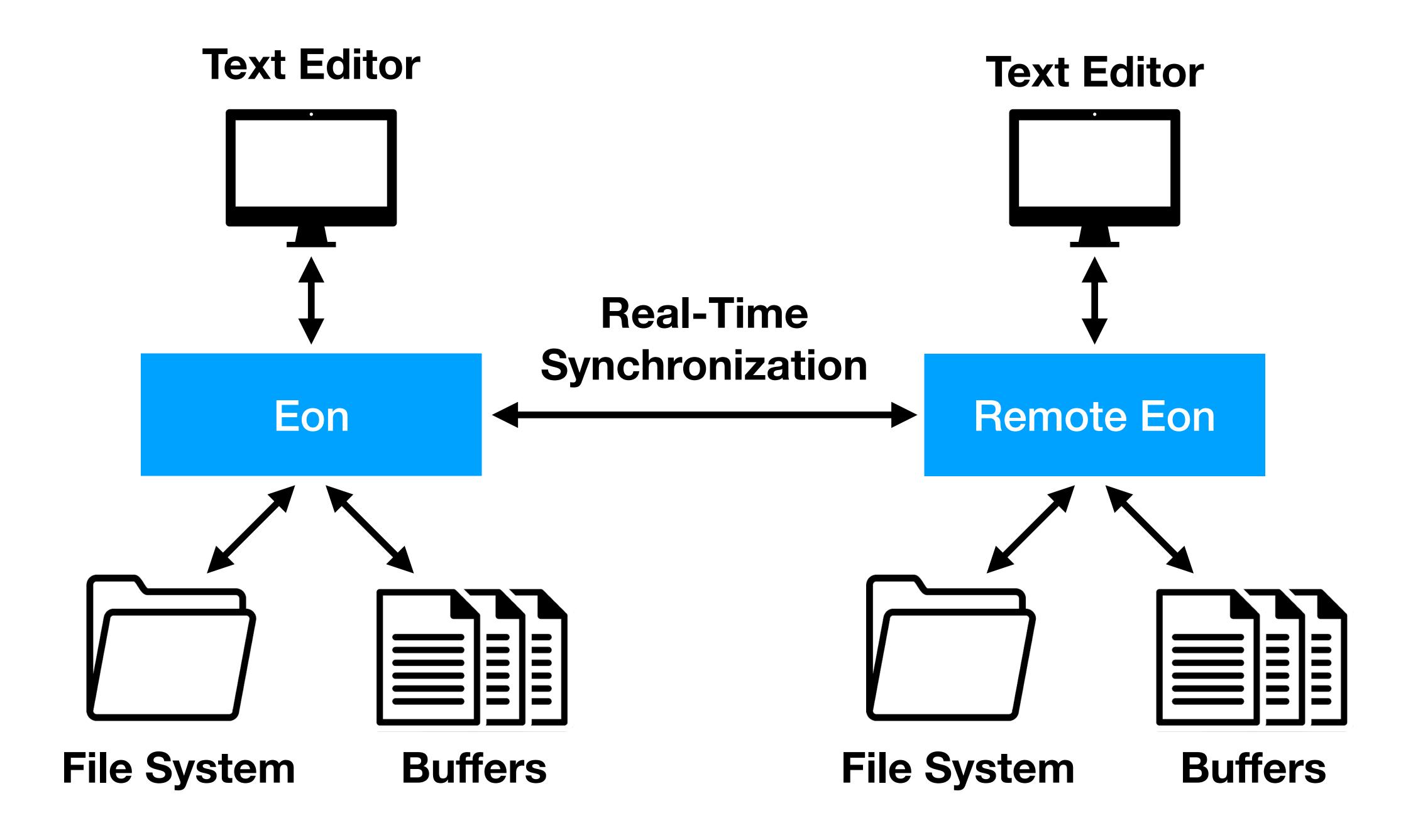
Real-time, Fine-grained Version Control with CRDTs

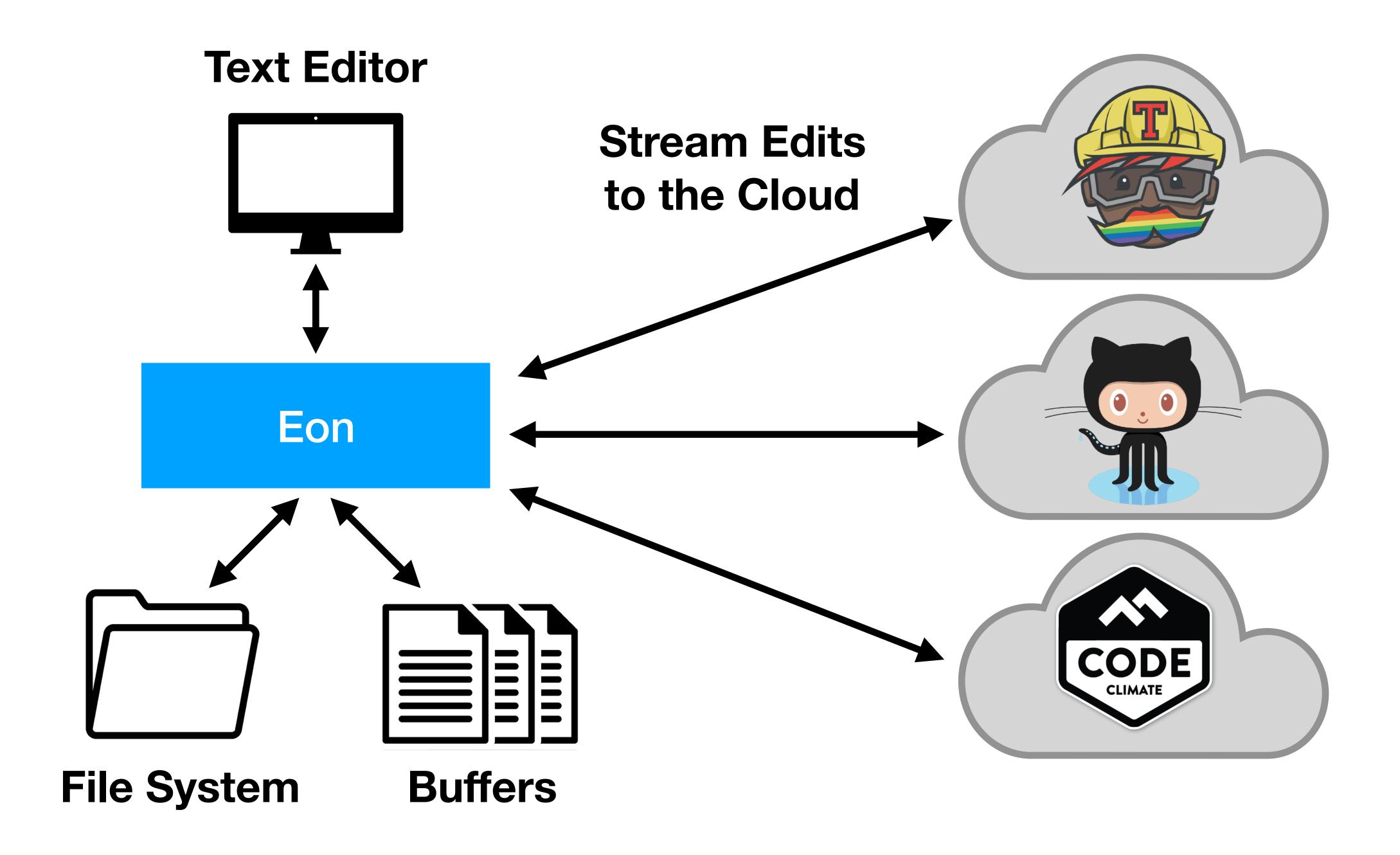


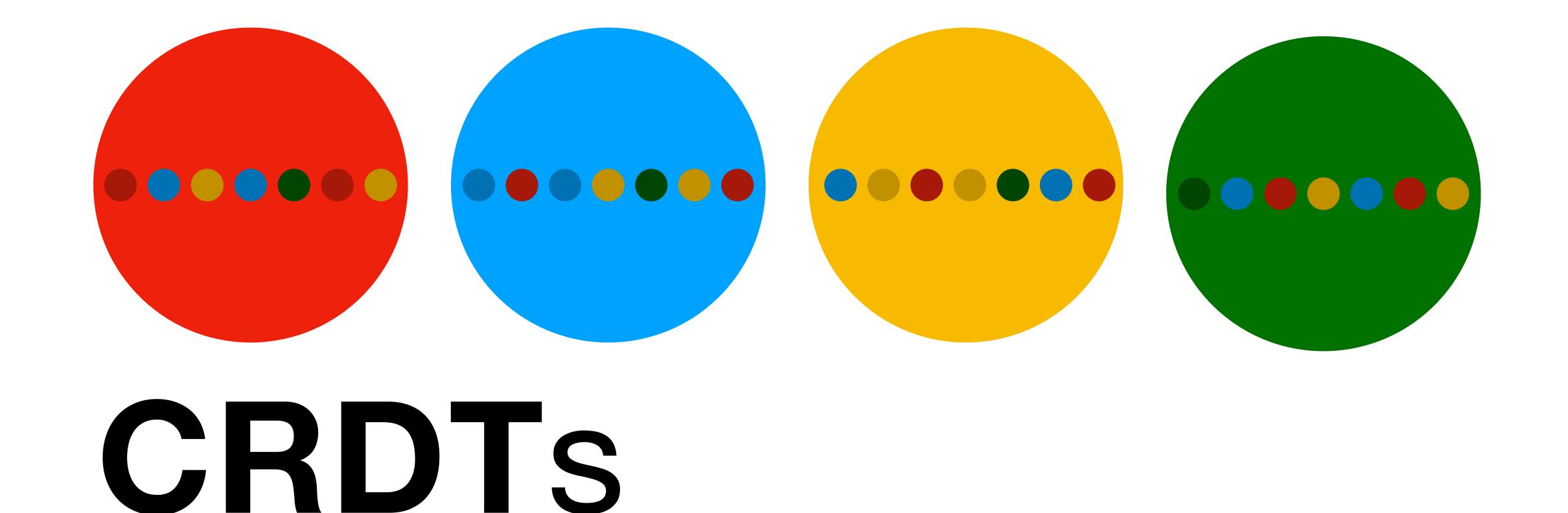




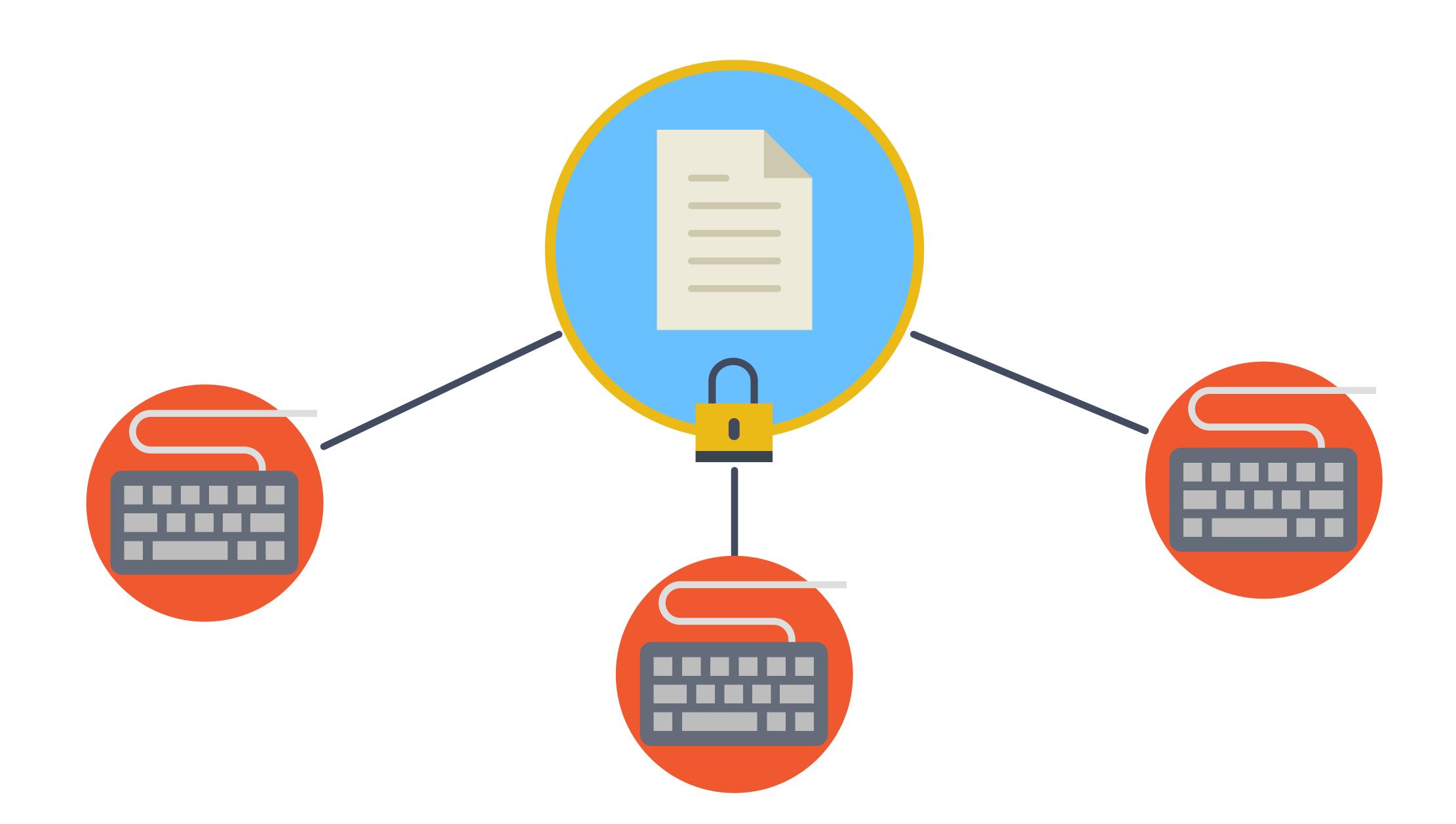




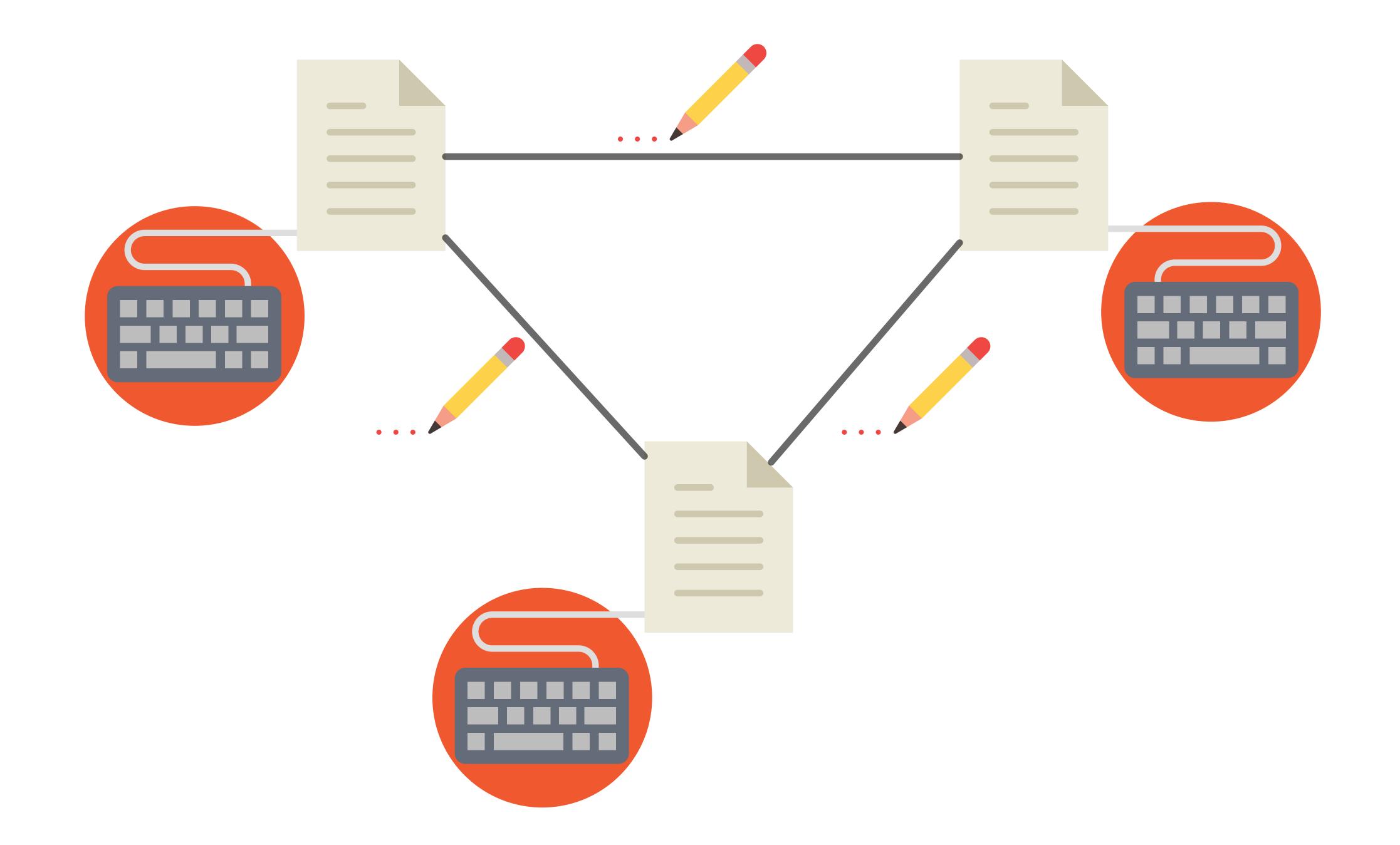




Conflict-Free Replicated Data Types







a b c

a b c

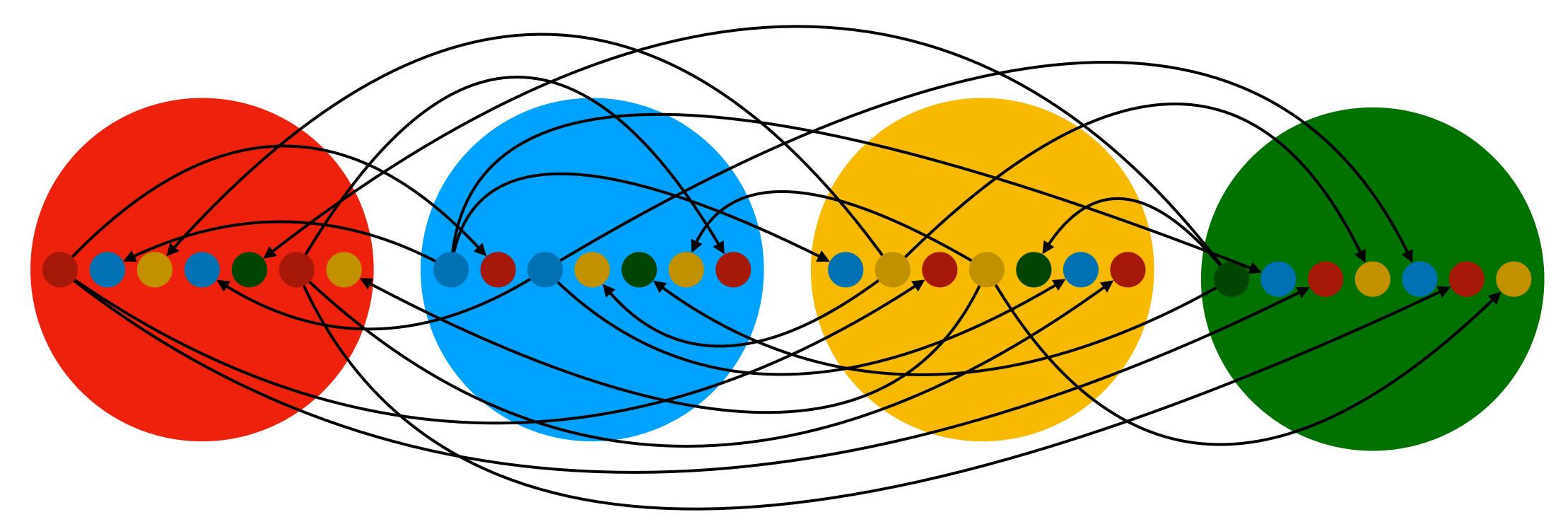
a b c insert(x, 1) a x b c

a b c
insert(y, 2)
a b y c

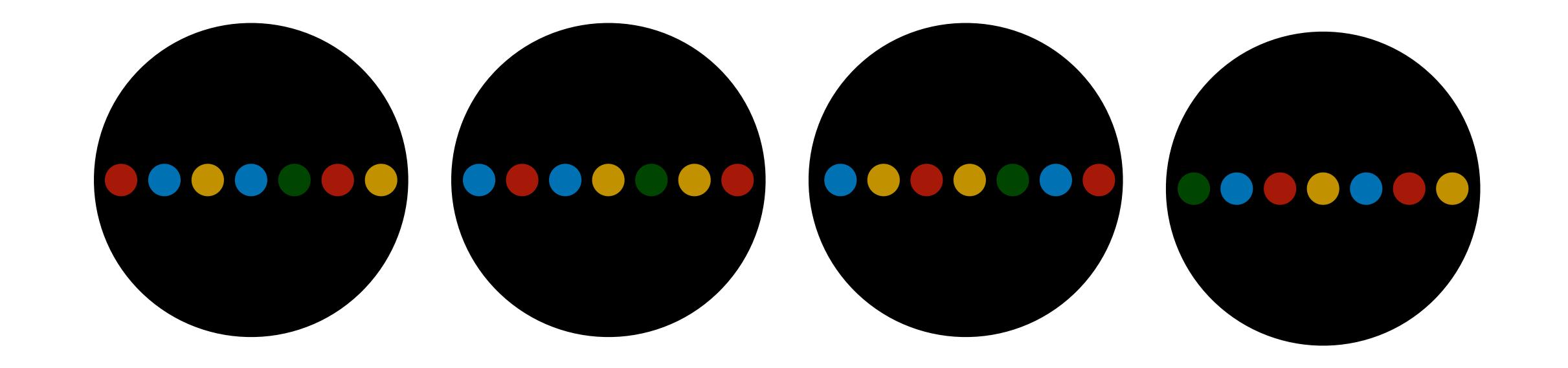
a b c a b c insert(x, 1) insert(y, 2) a x b c a b y c insert(x, 1) a x b y c

```
a b c
                              a b c
 insert(x, 1)
                              insert(y, 2)
 a x b c
                             a b y c
 insert(y, 2)
                             insert(x, 1)
a x y b c
                            a x b y c
```

a b c a b c insert(x, 1) insert(y, 2) a x b c a b y c insert(y, 3) insert(x, 1)**Operational Transformation** a x b y c a x b y c



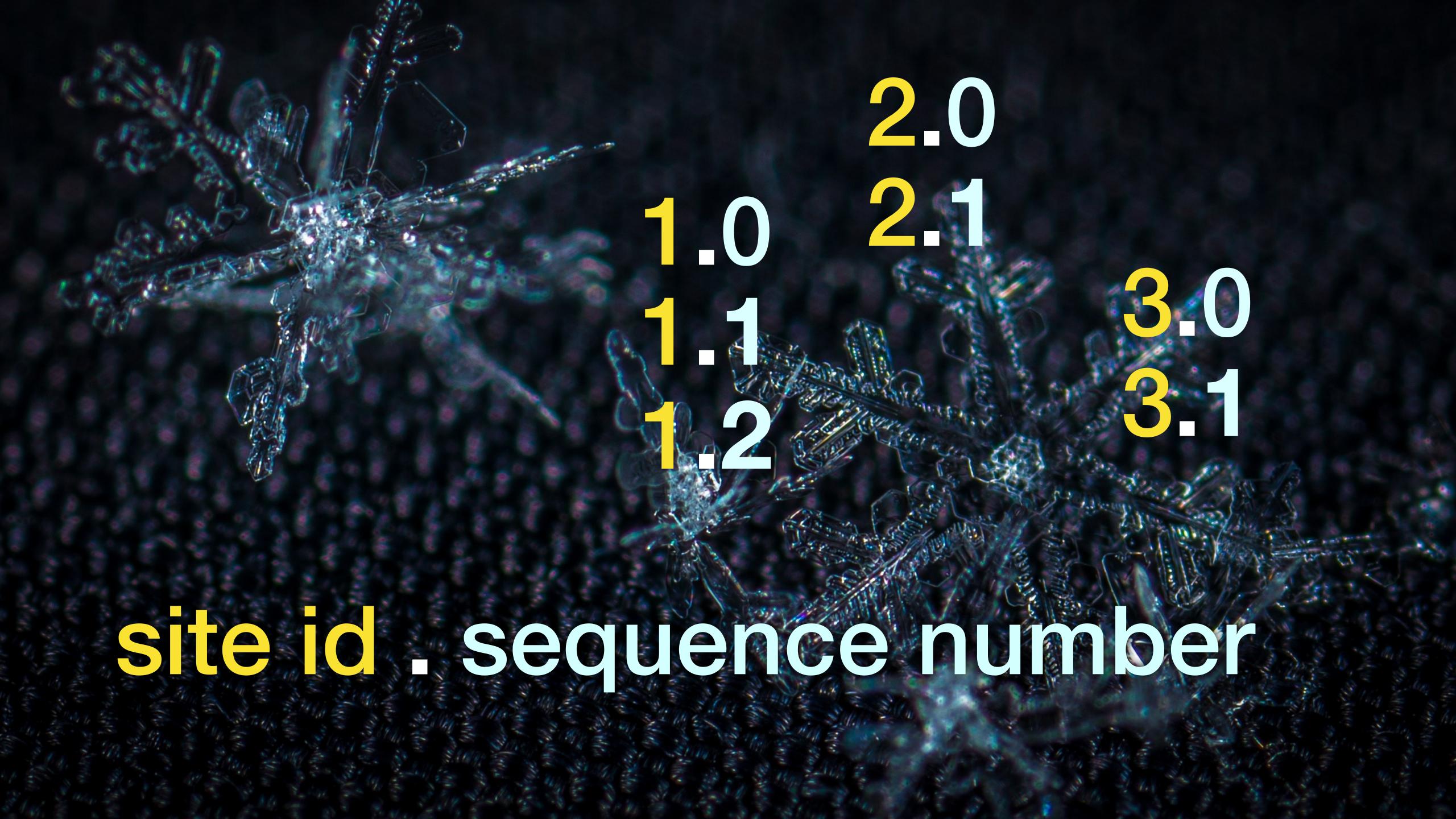
Concurrent operations are commutative



All replicas converge to the same state

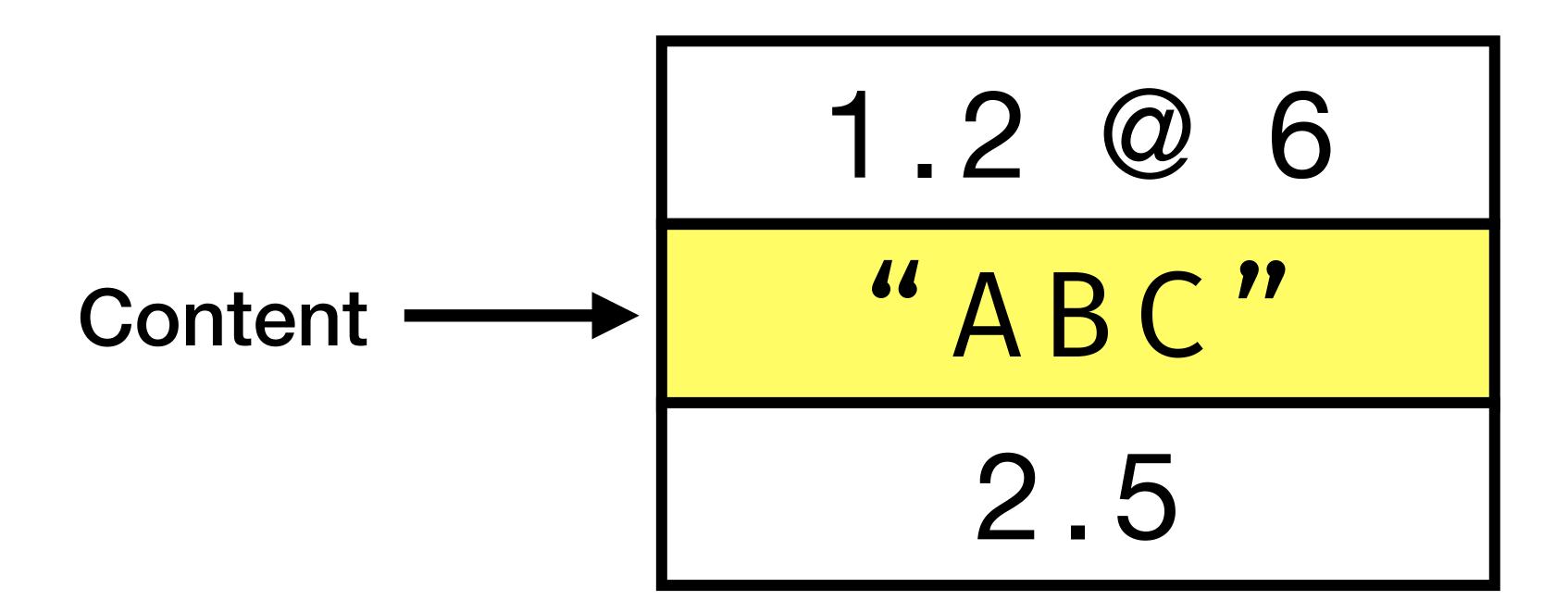


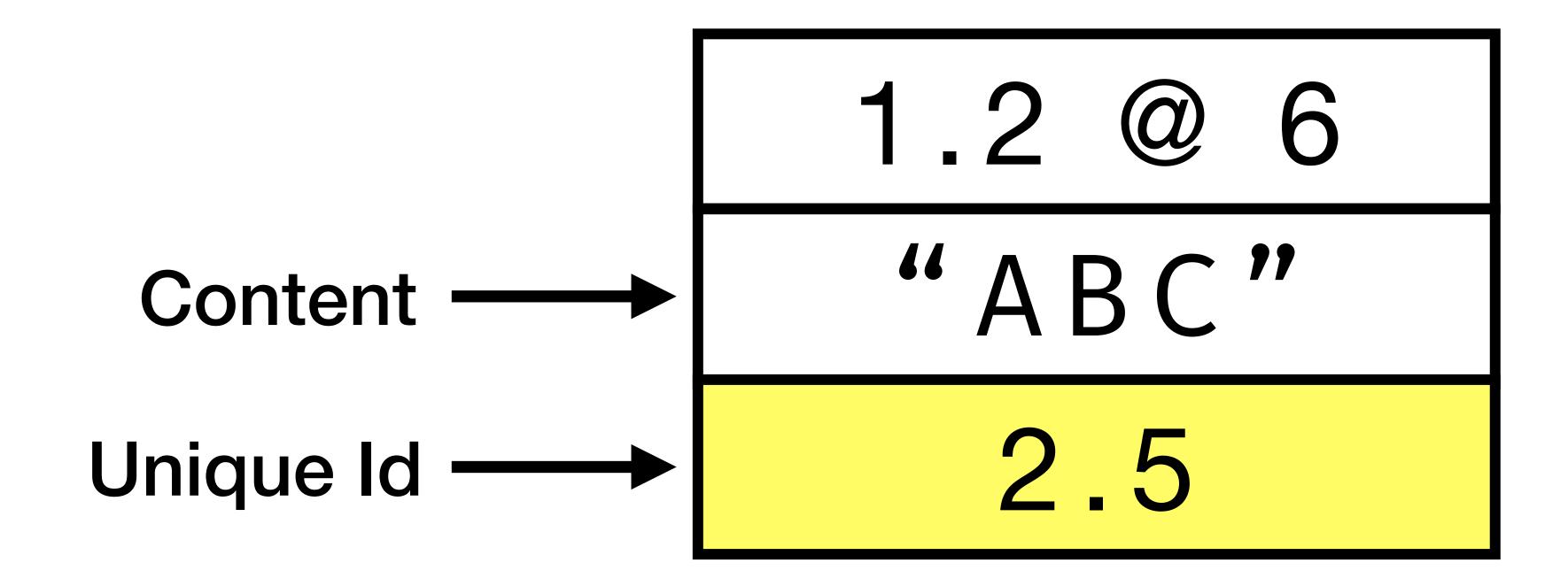


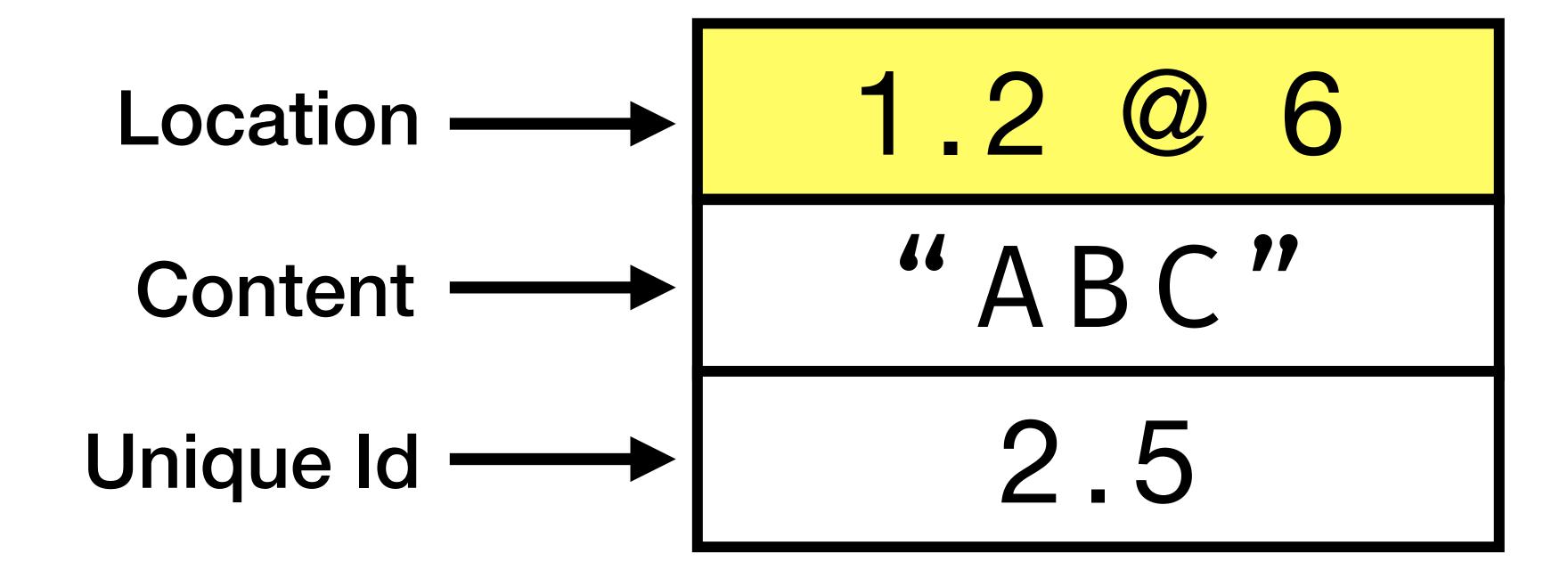


Insertions

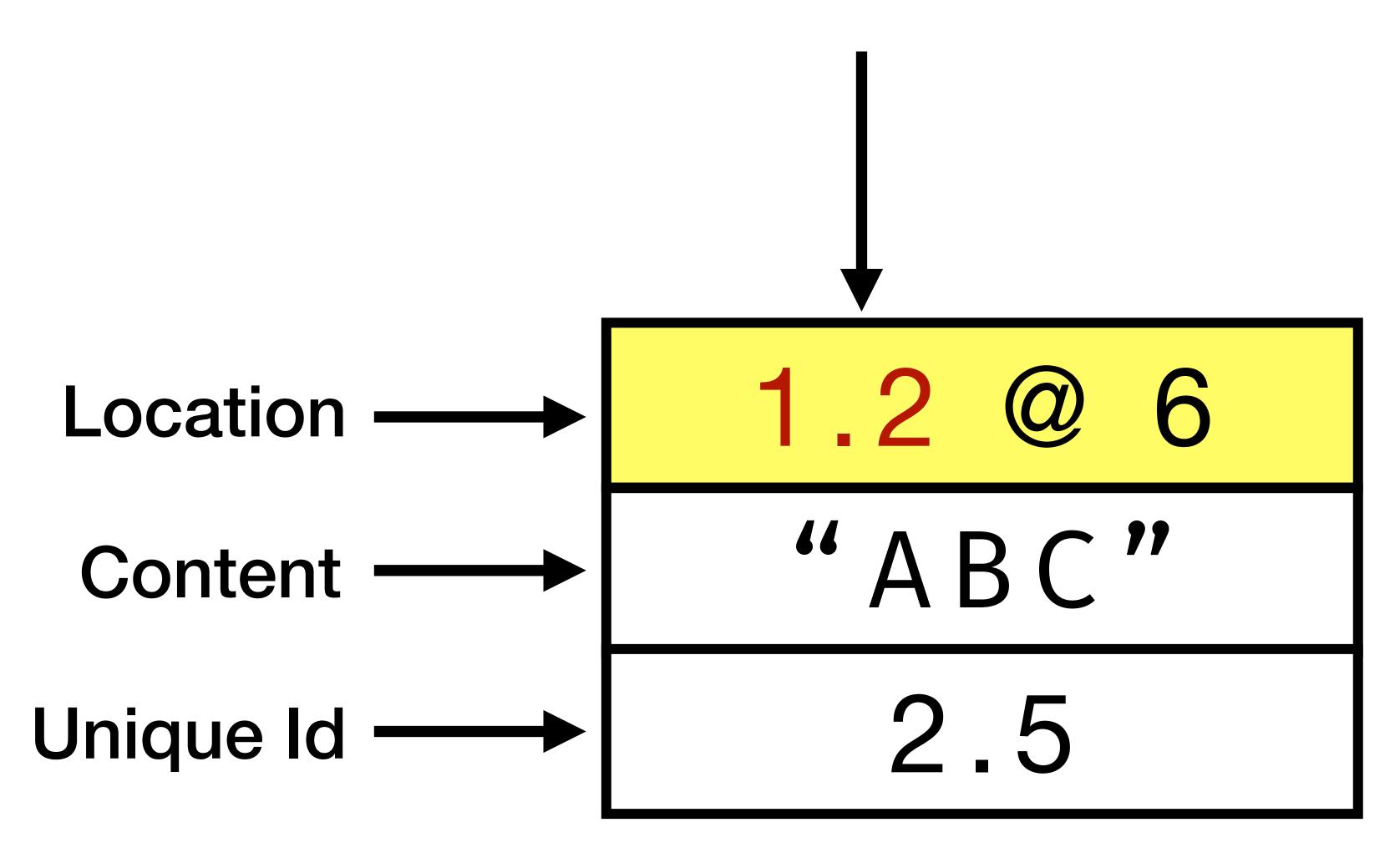
1.2 @ 6 "ABC" 2.5



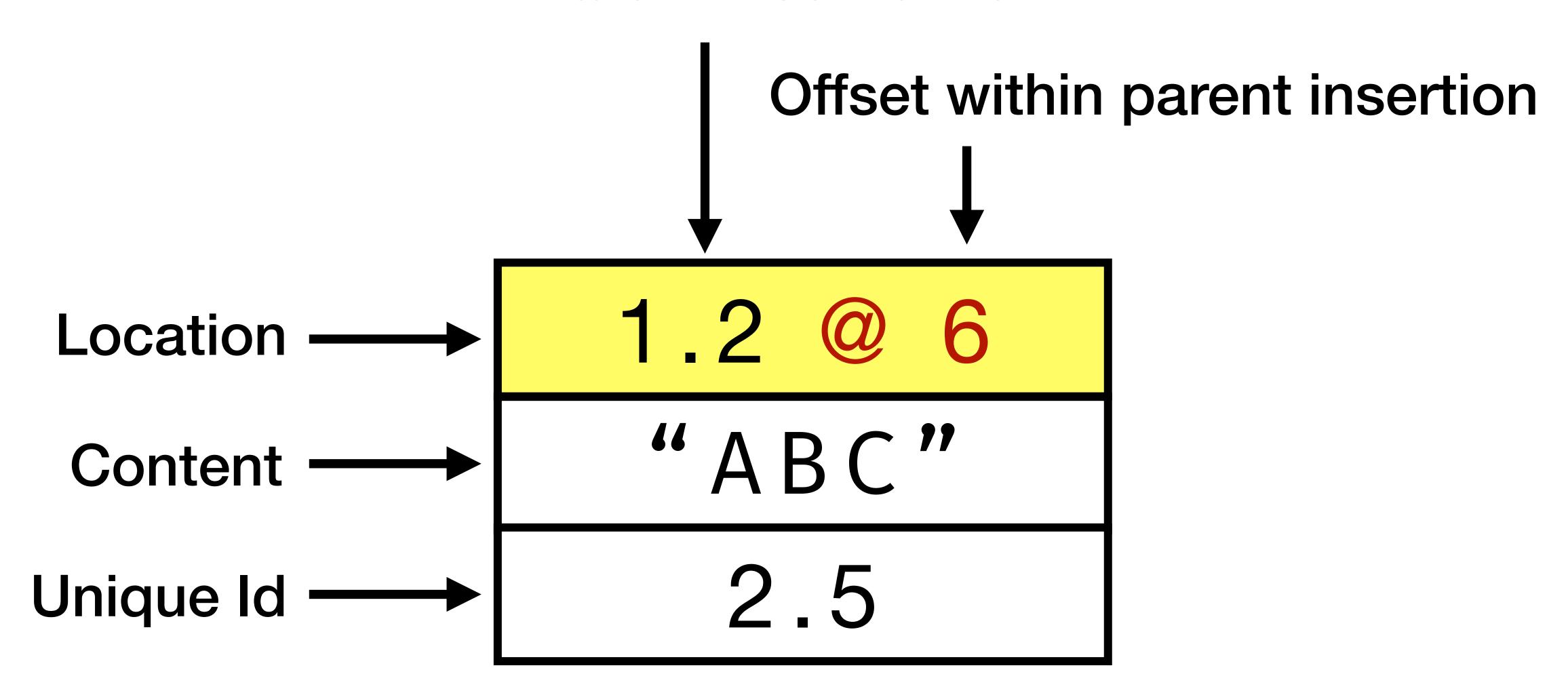




Parent insertion id



Parent insertion id



0.0 @ 0 ABC

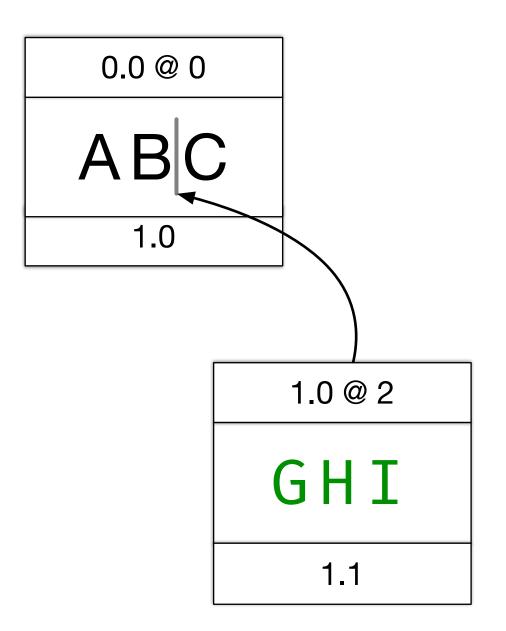
Site 2

0.0 @ 0

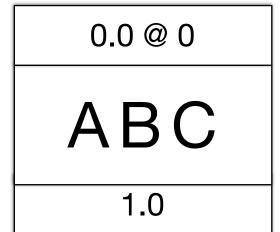
ABC

ABC

ABC



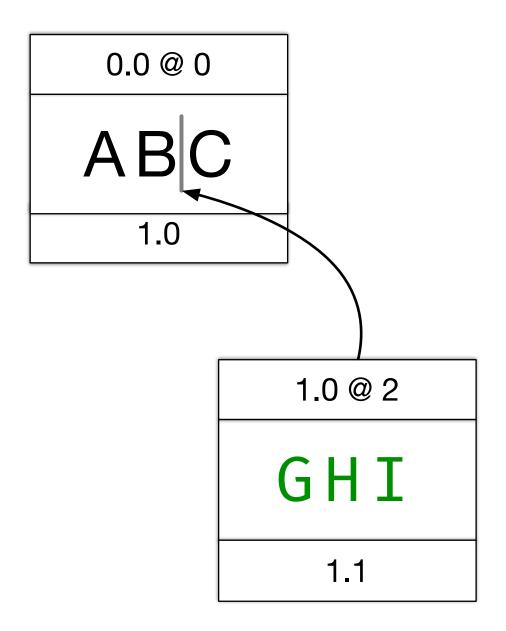
Site 2



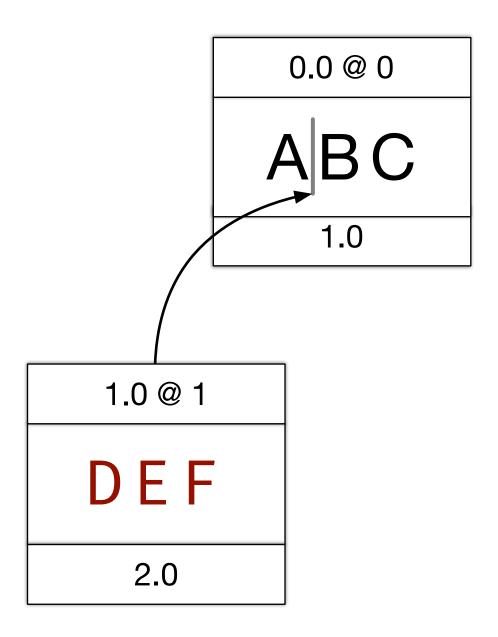
ABGHIC

ABC

Site 1

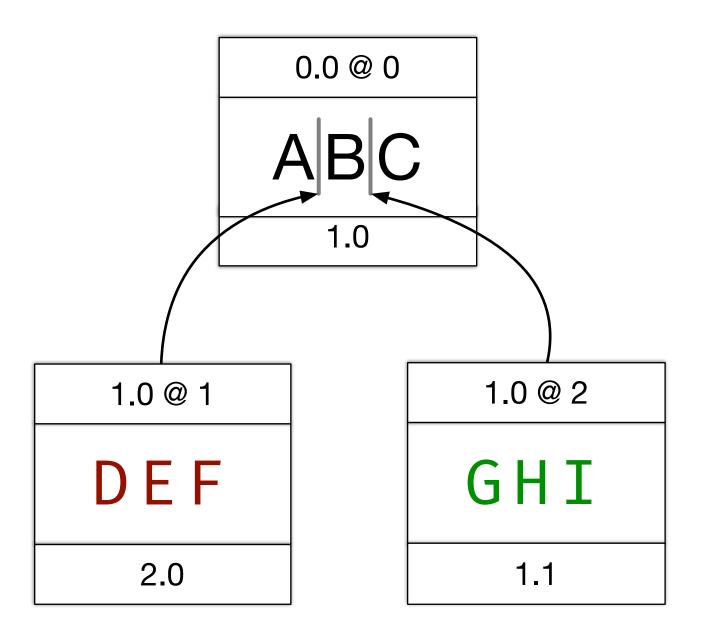


Site 2

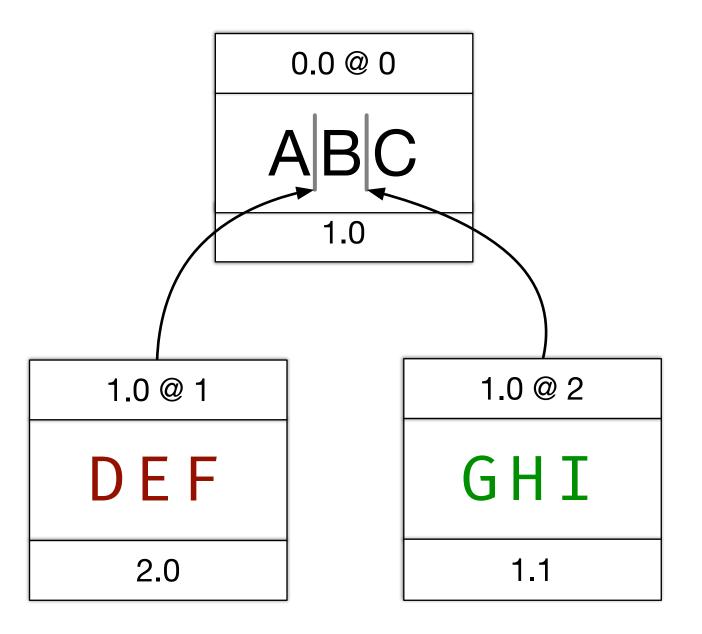


ABGHIC

ADEFBC

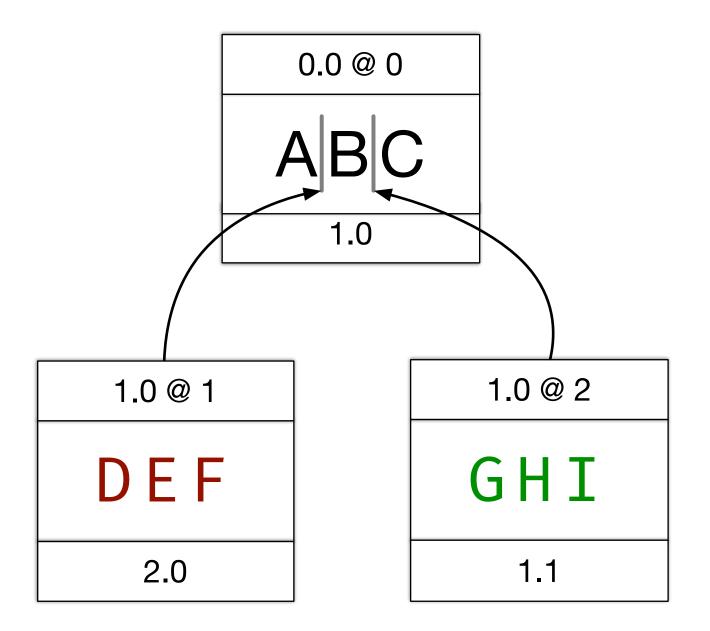


Site 2

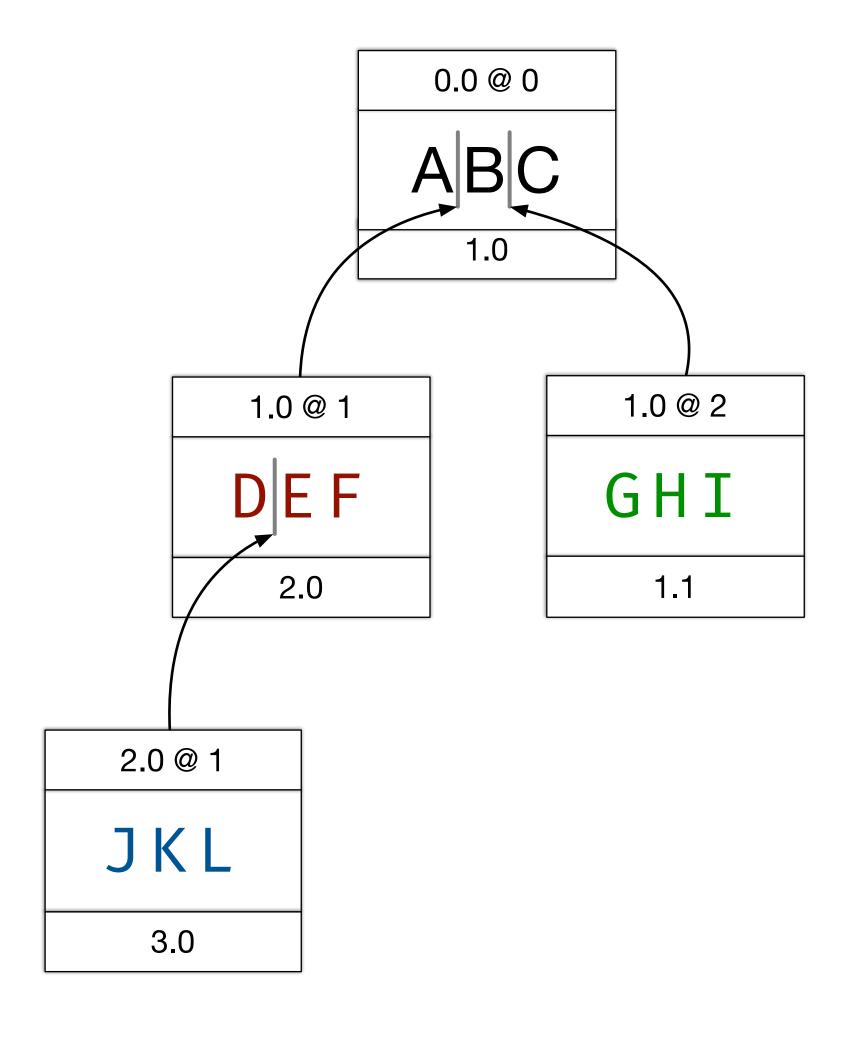


ADEFBGHIC

ADEFBGHIC

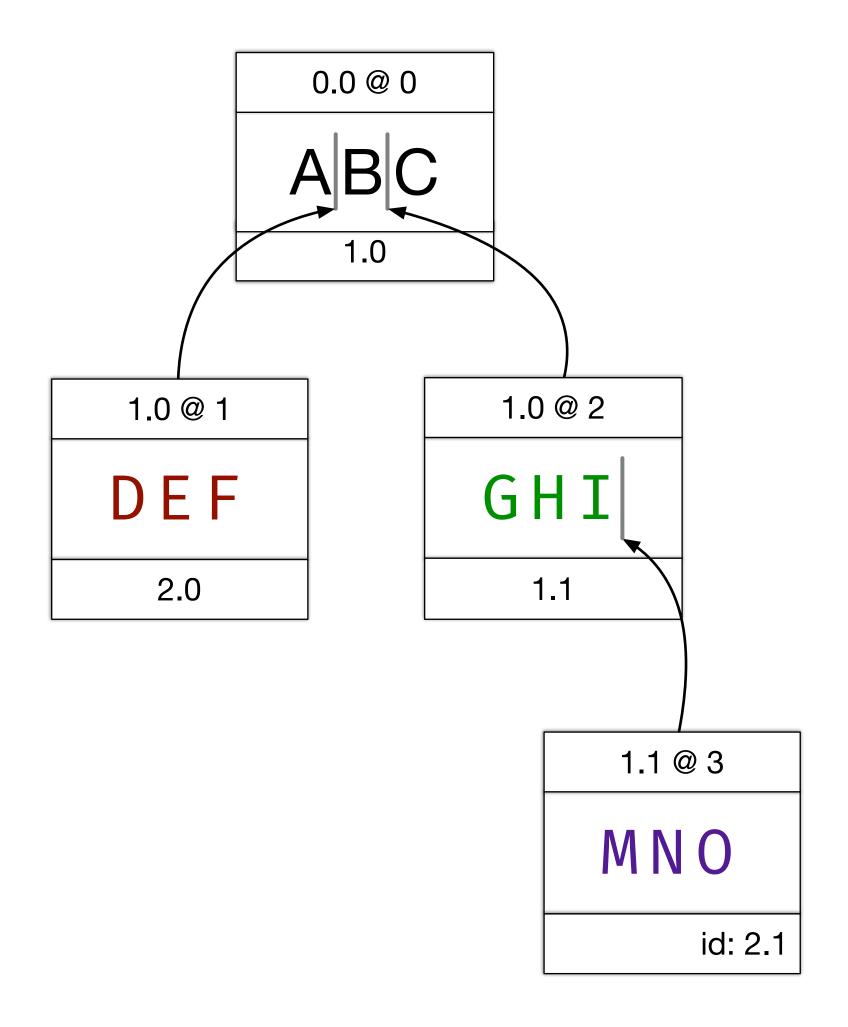


Site 2



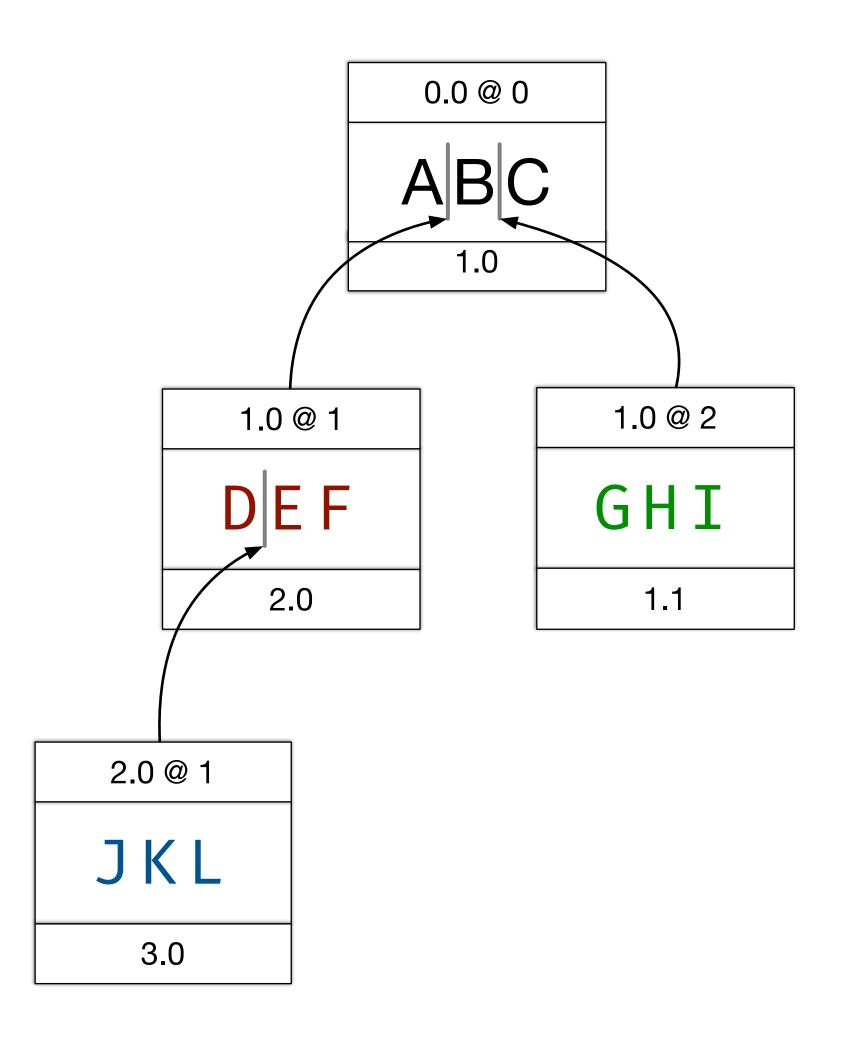
ADEFBGHIC

ADJKLEFBGHIC

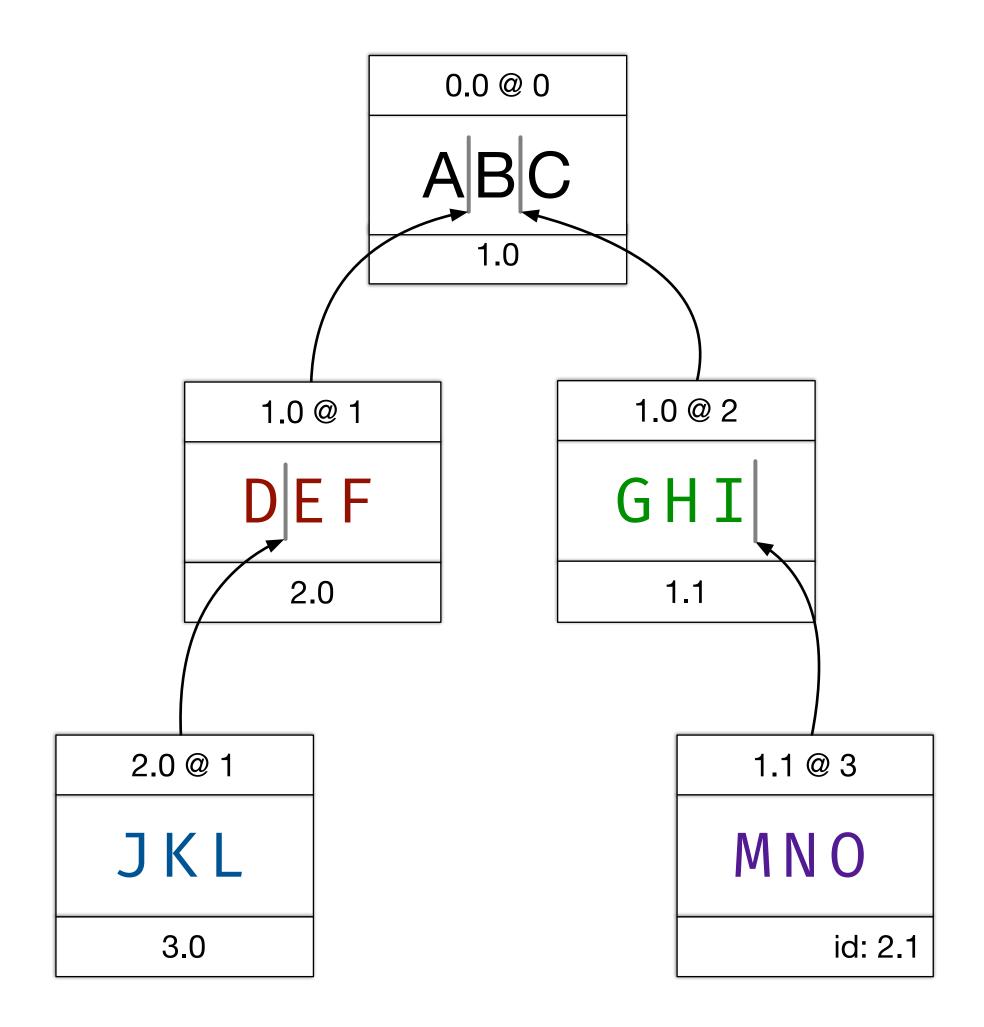


ADEFBGHICMNO

Site 2

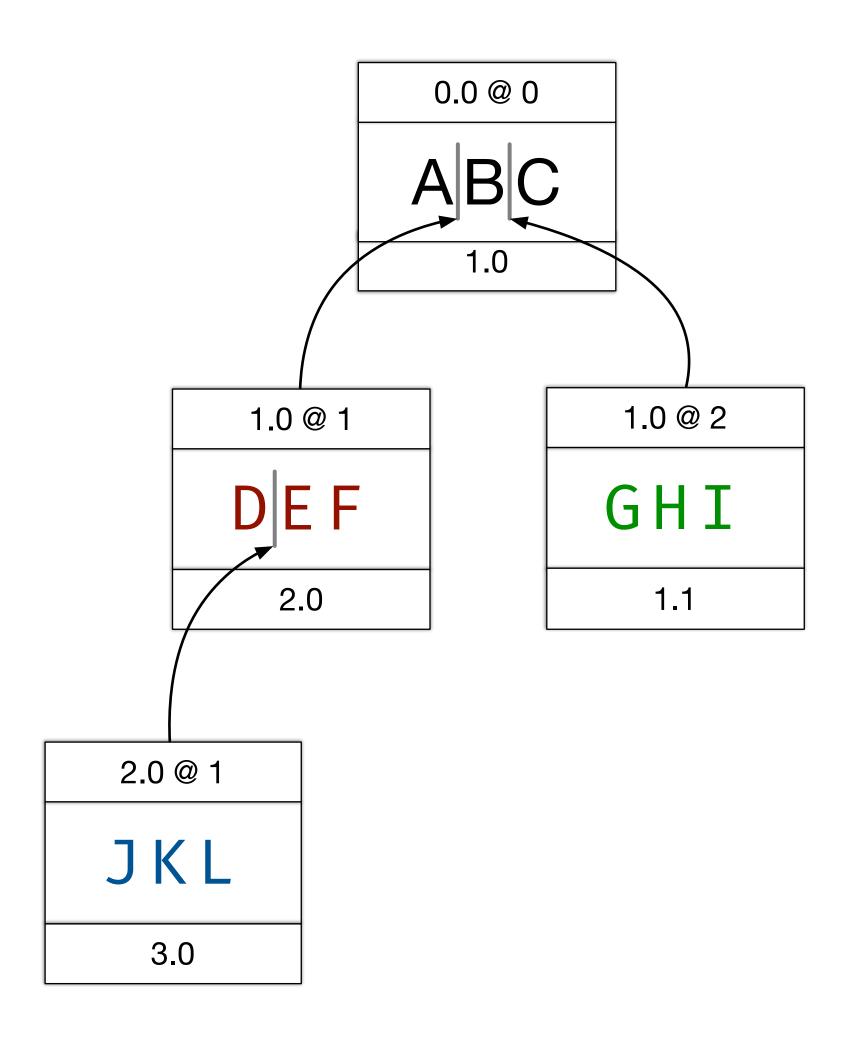


ADJKLEFBGHIC

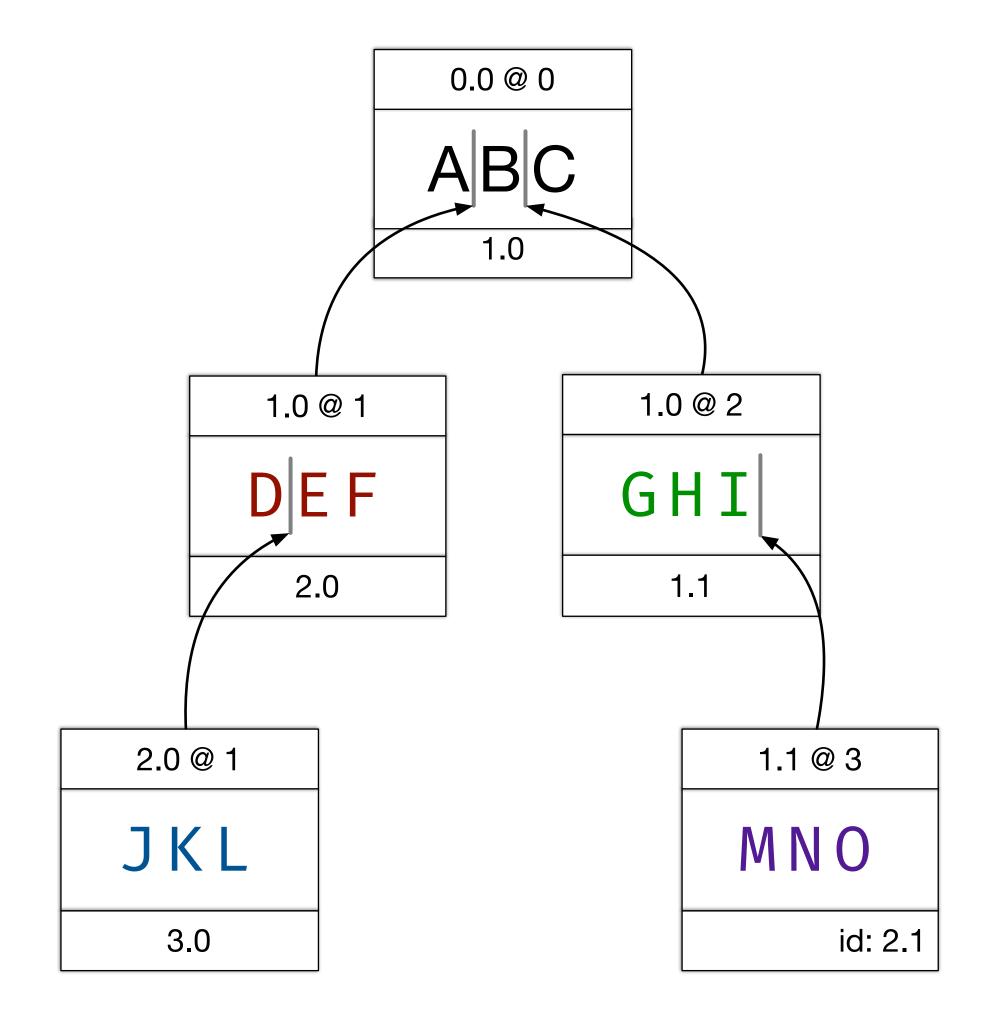


ADJKLEFBGHICMNO

Site 2

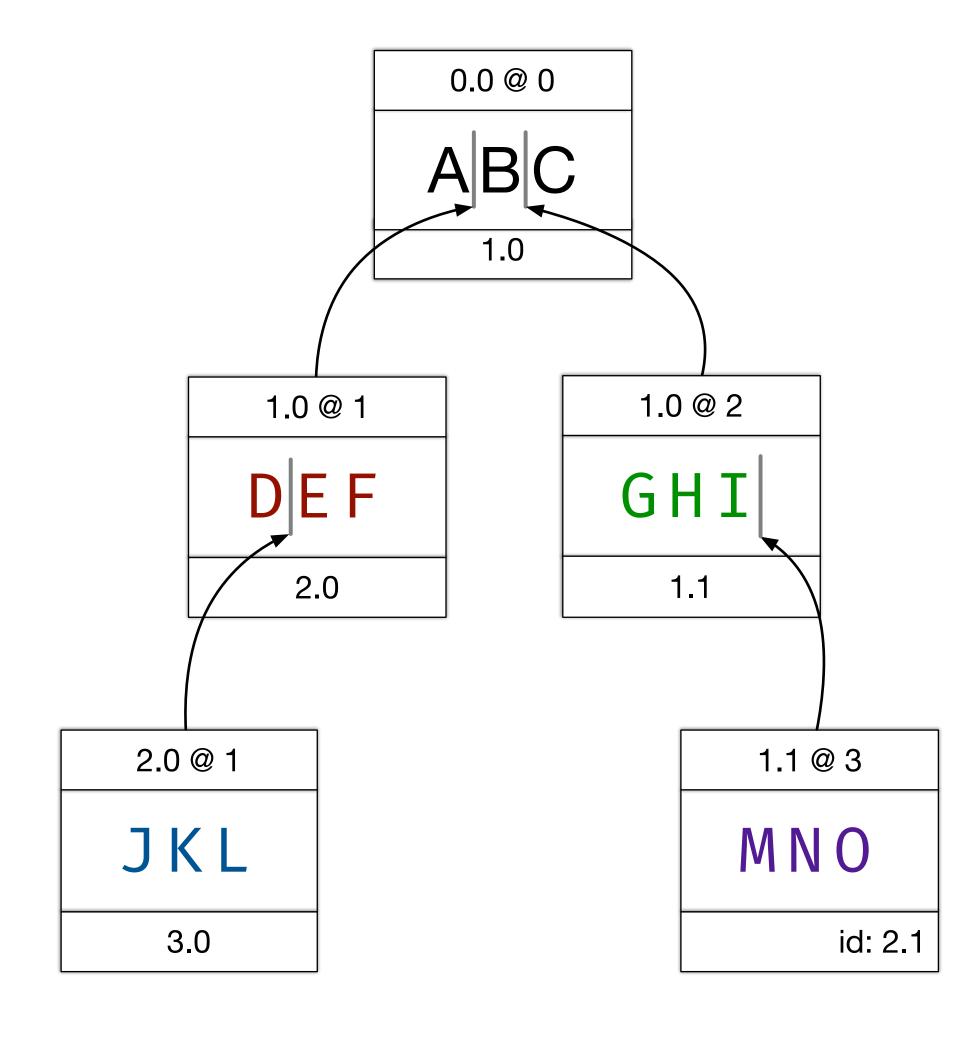


ADJKLEFBGHIC

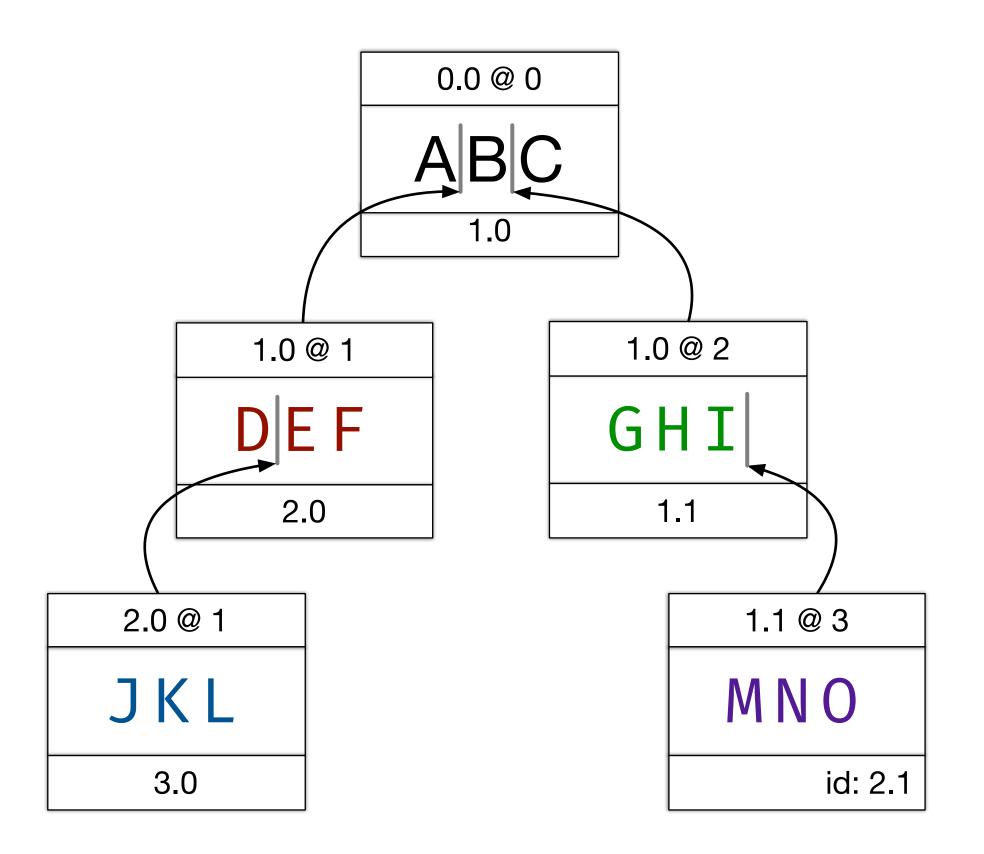


ADJKLEFBGHICMNO

Site 2



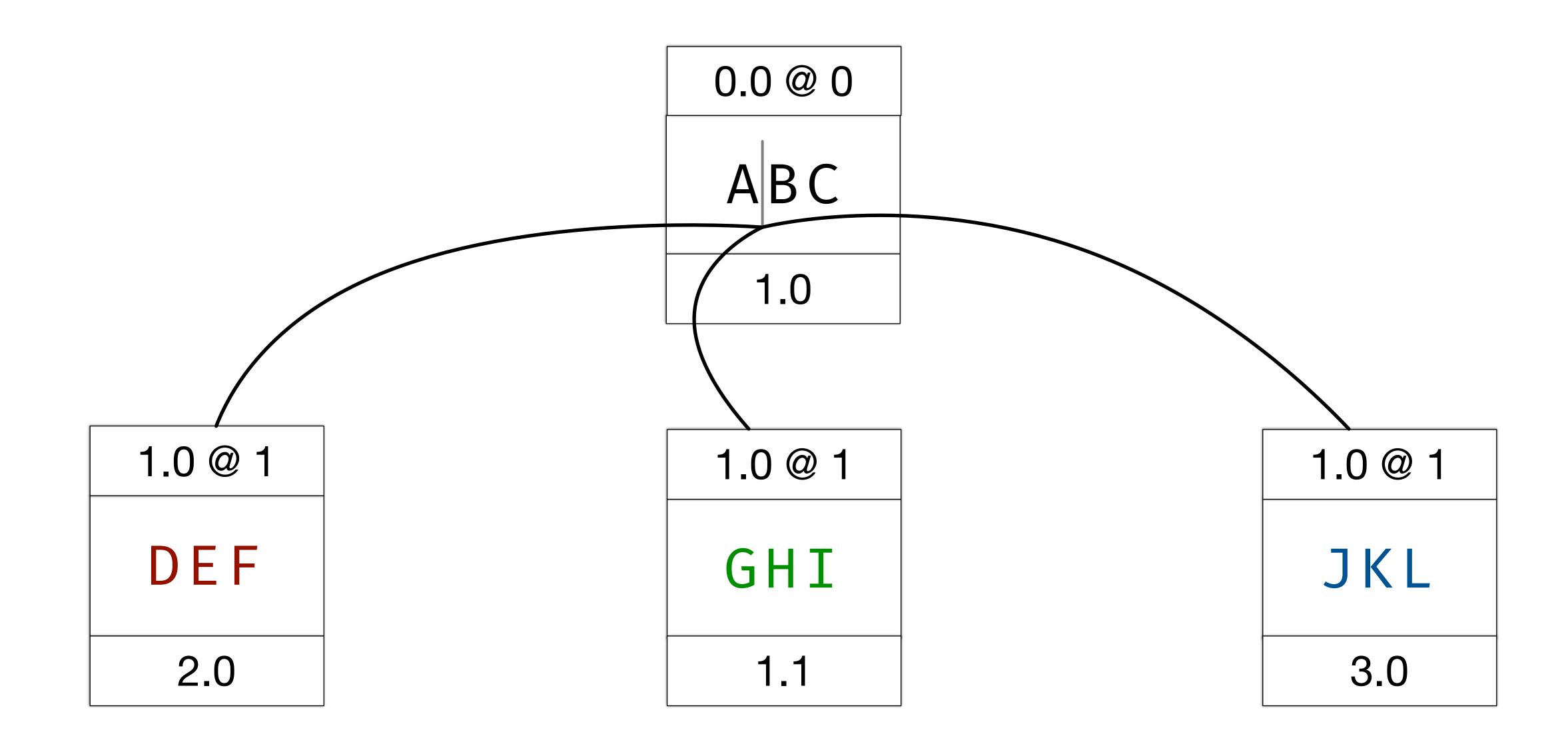
ADJKLEFBGHICMNO



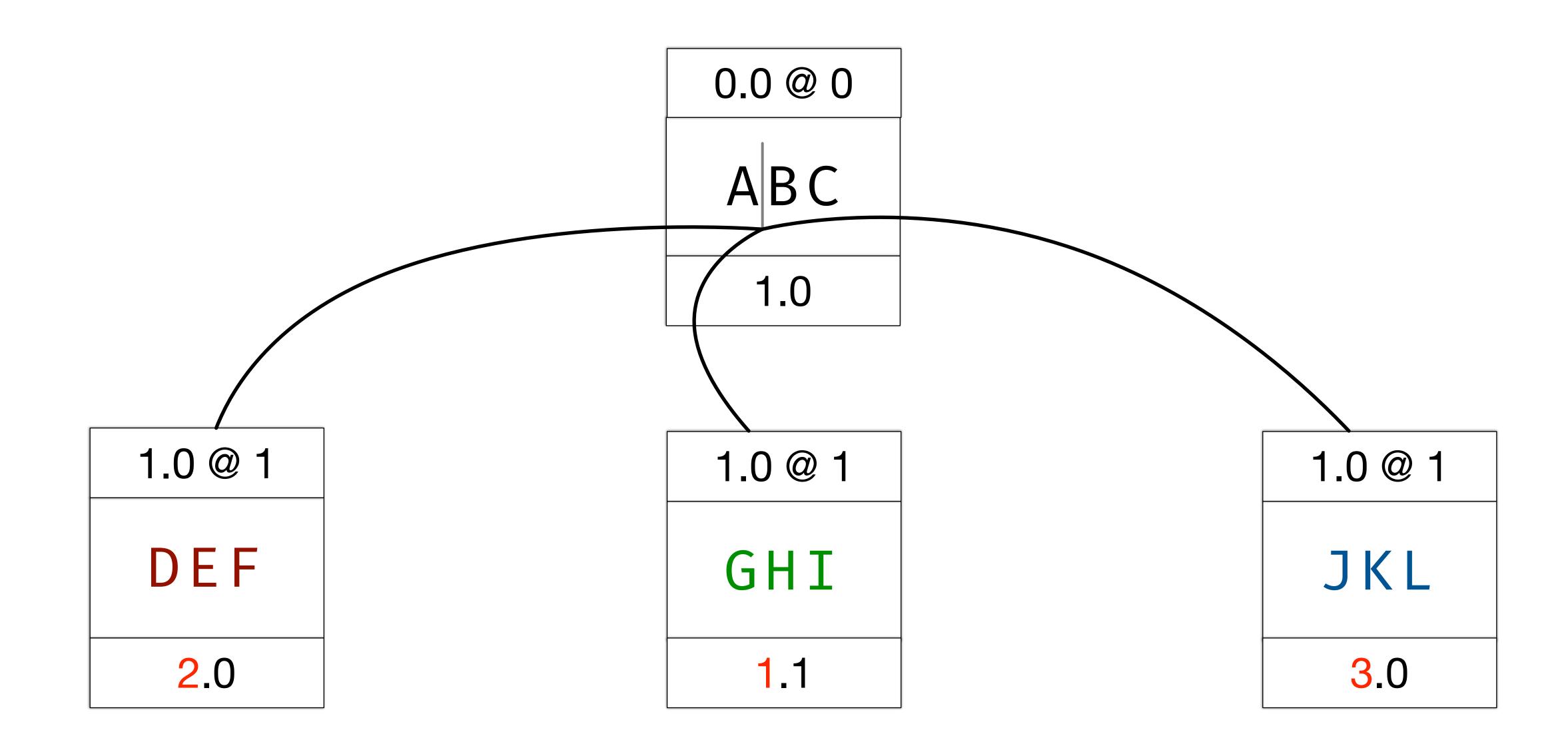
Fragment Sequence:

1.0 0 0	2.0 0 0	3.0 0 0	1.0 a 2	1.0 a 1	1.1 0 0	1.0 0 2	1.1 0 0
Α	D	JKL	EF	В	GHI	C	MNO

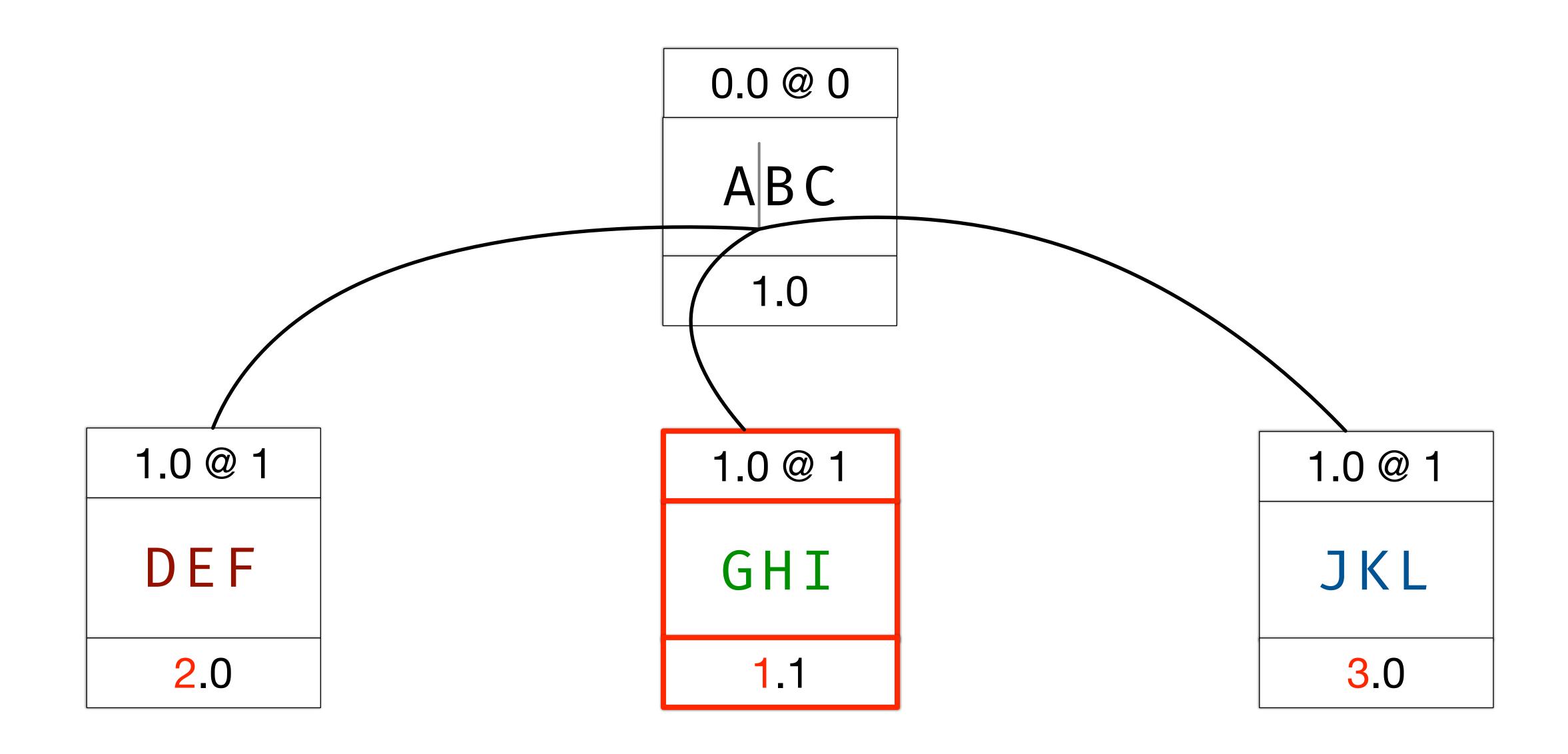




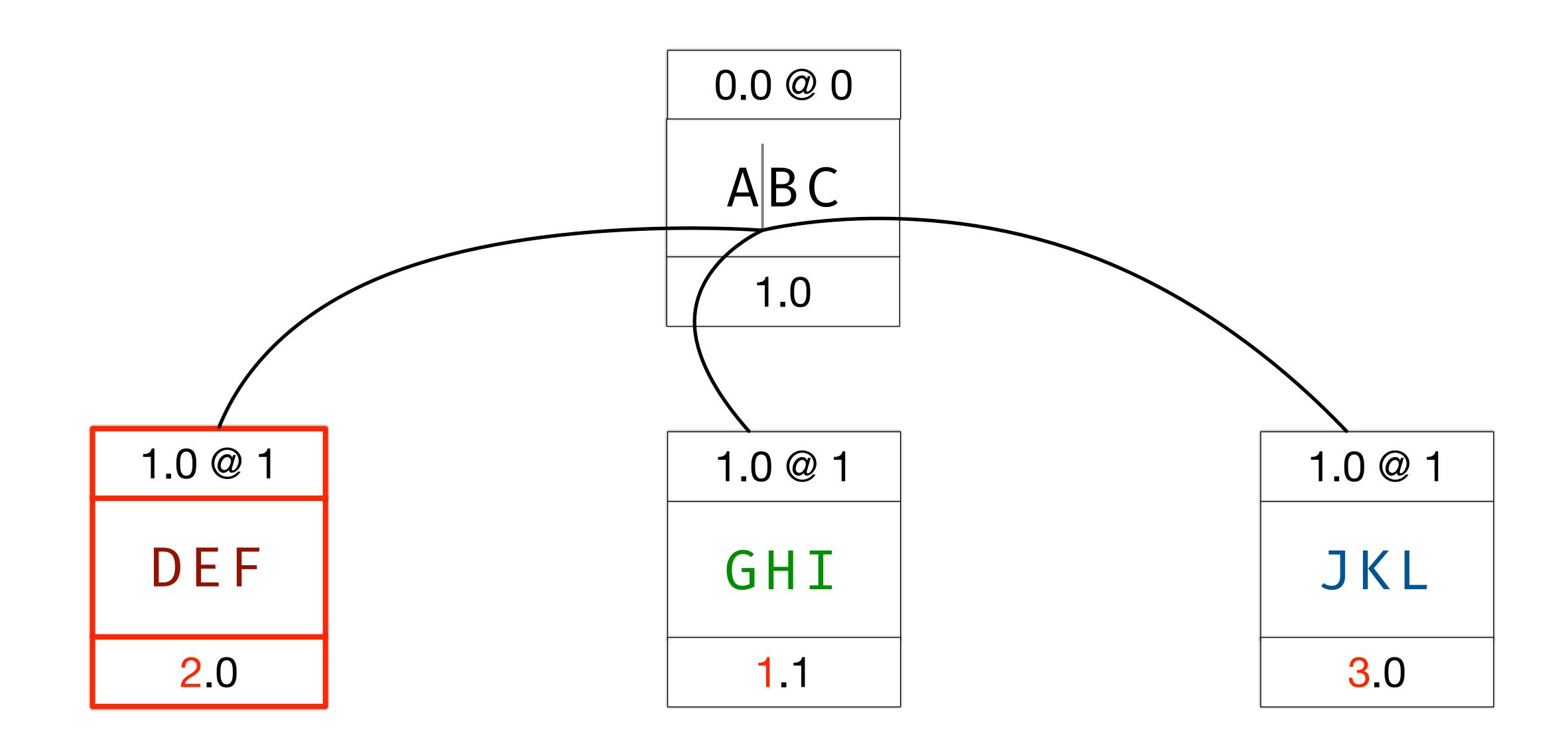
ABC



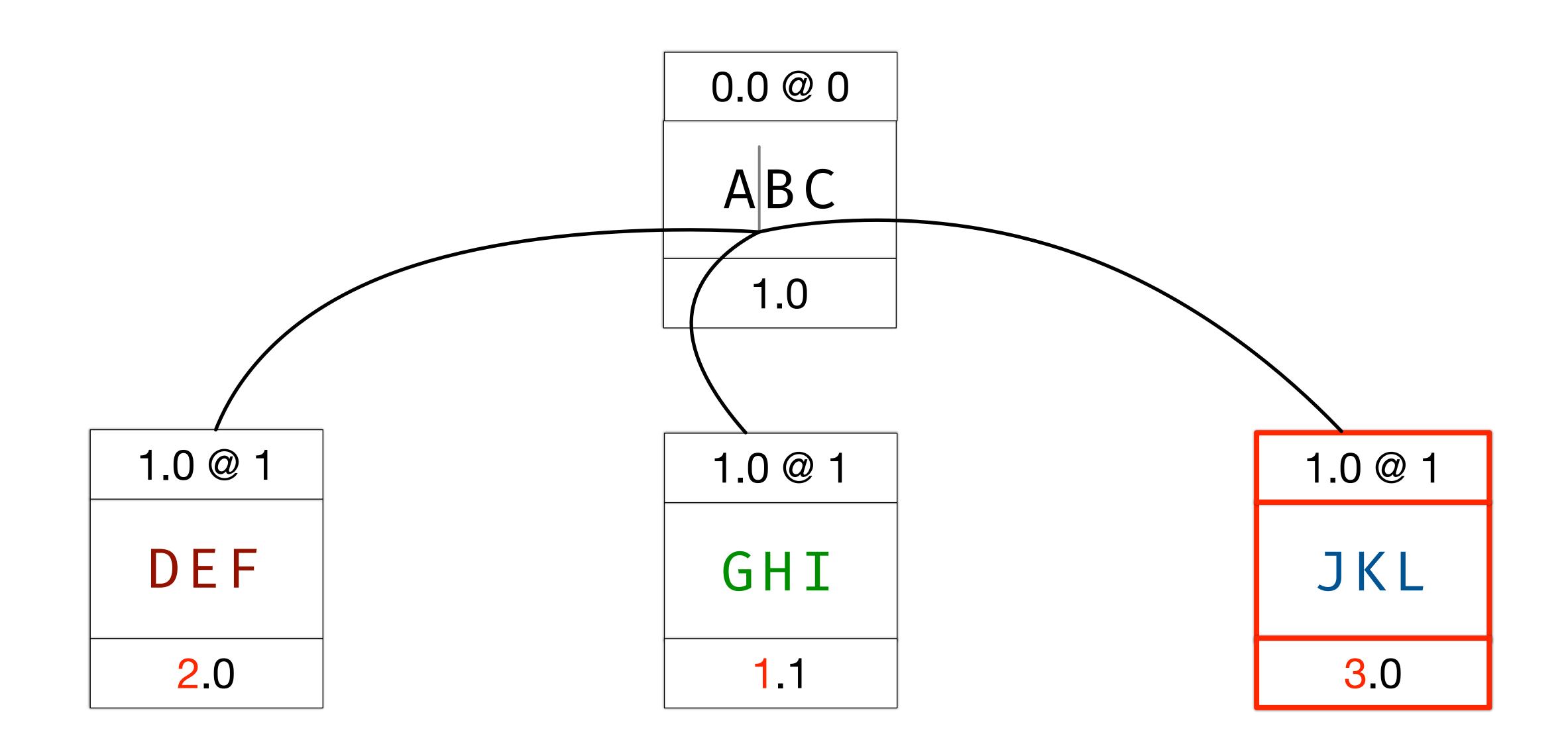
ABC



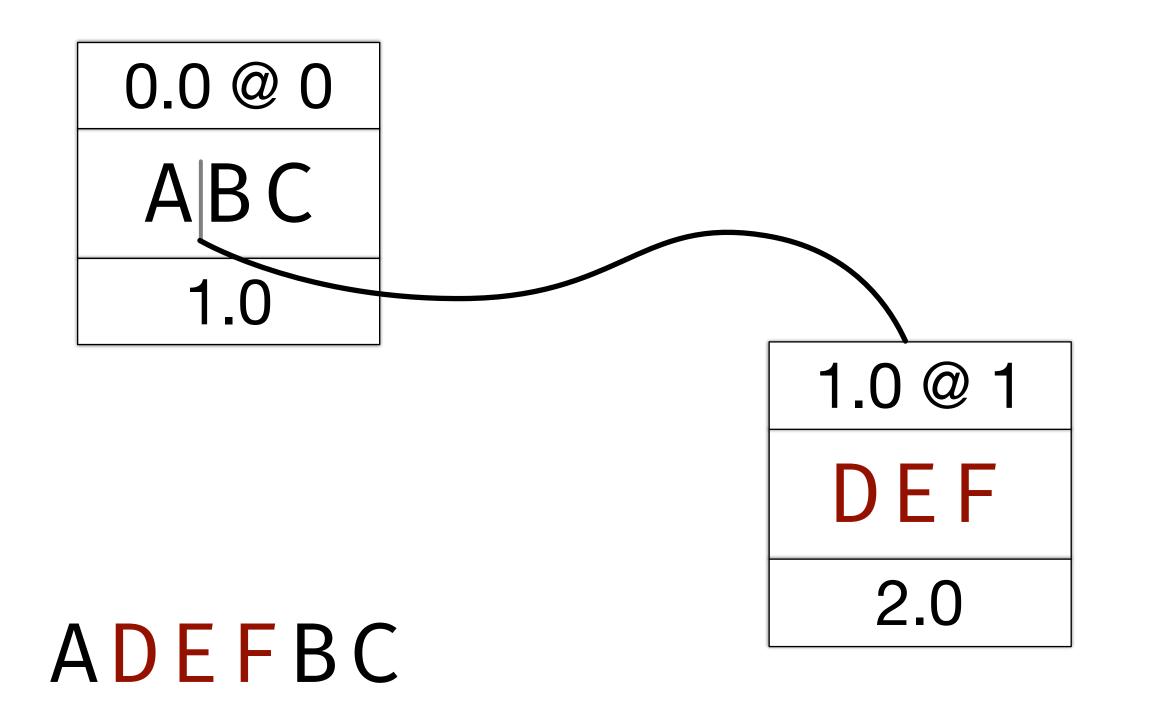
AGHIBC



AGHIDEFBC

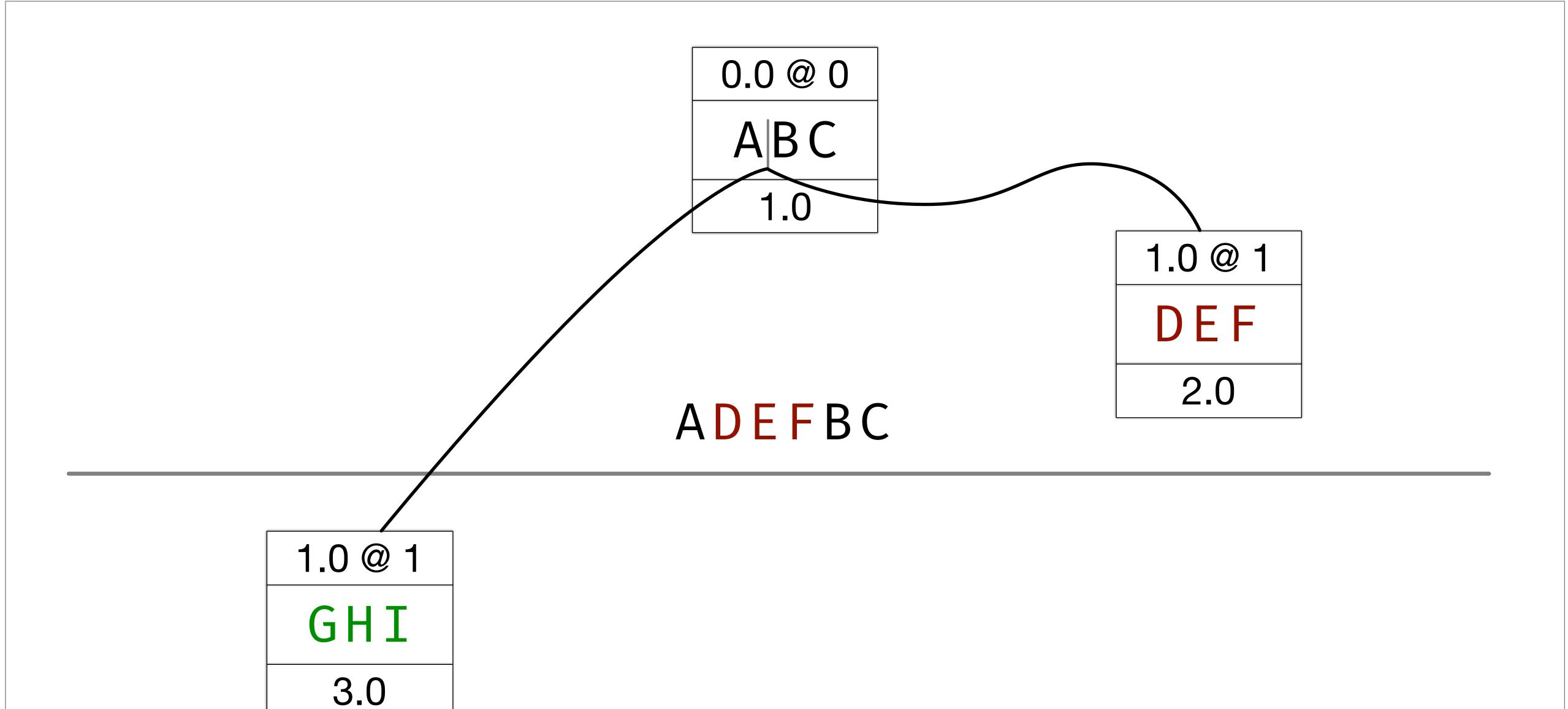


AGHIDEFJKLBC

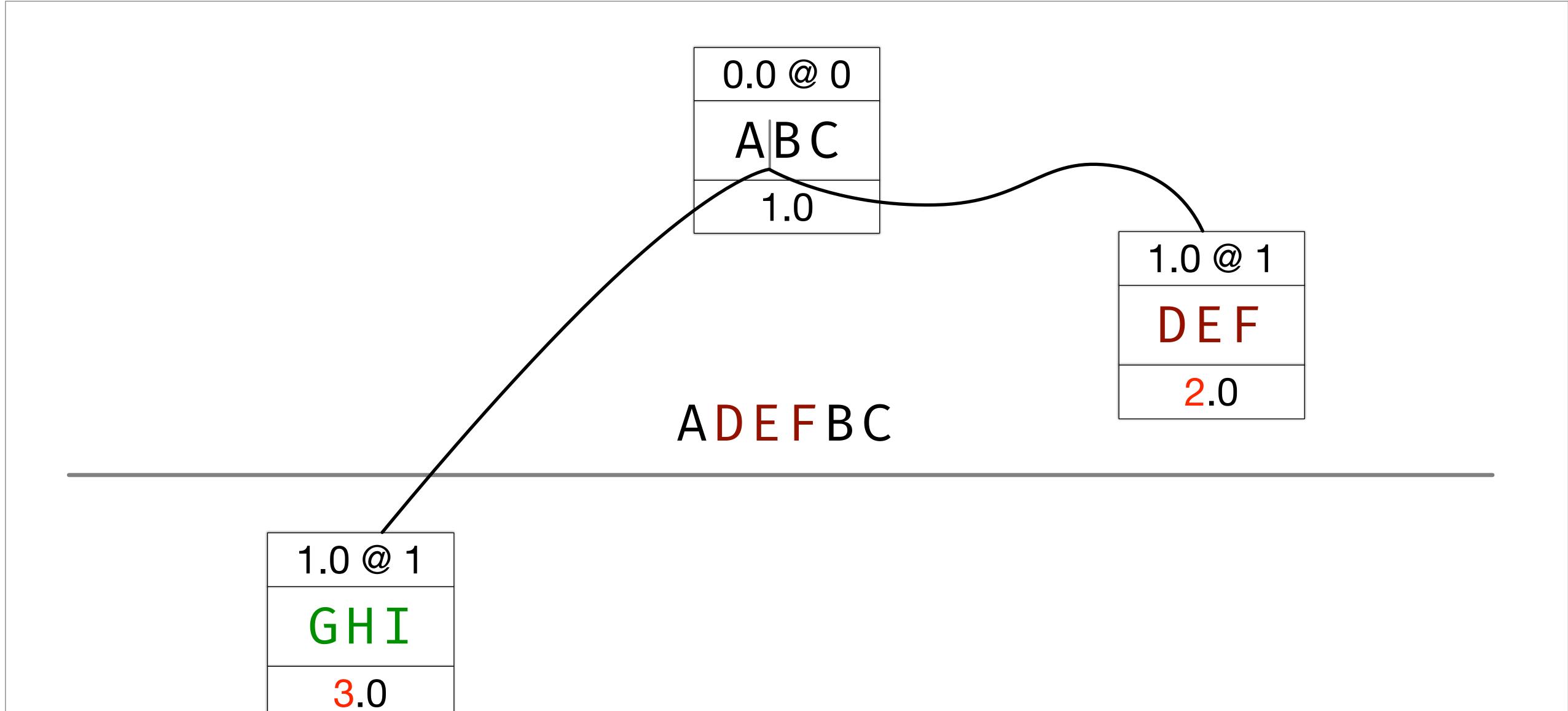


GHI 3.0

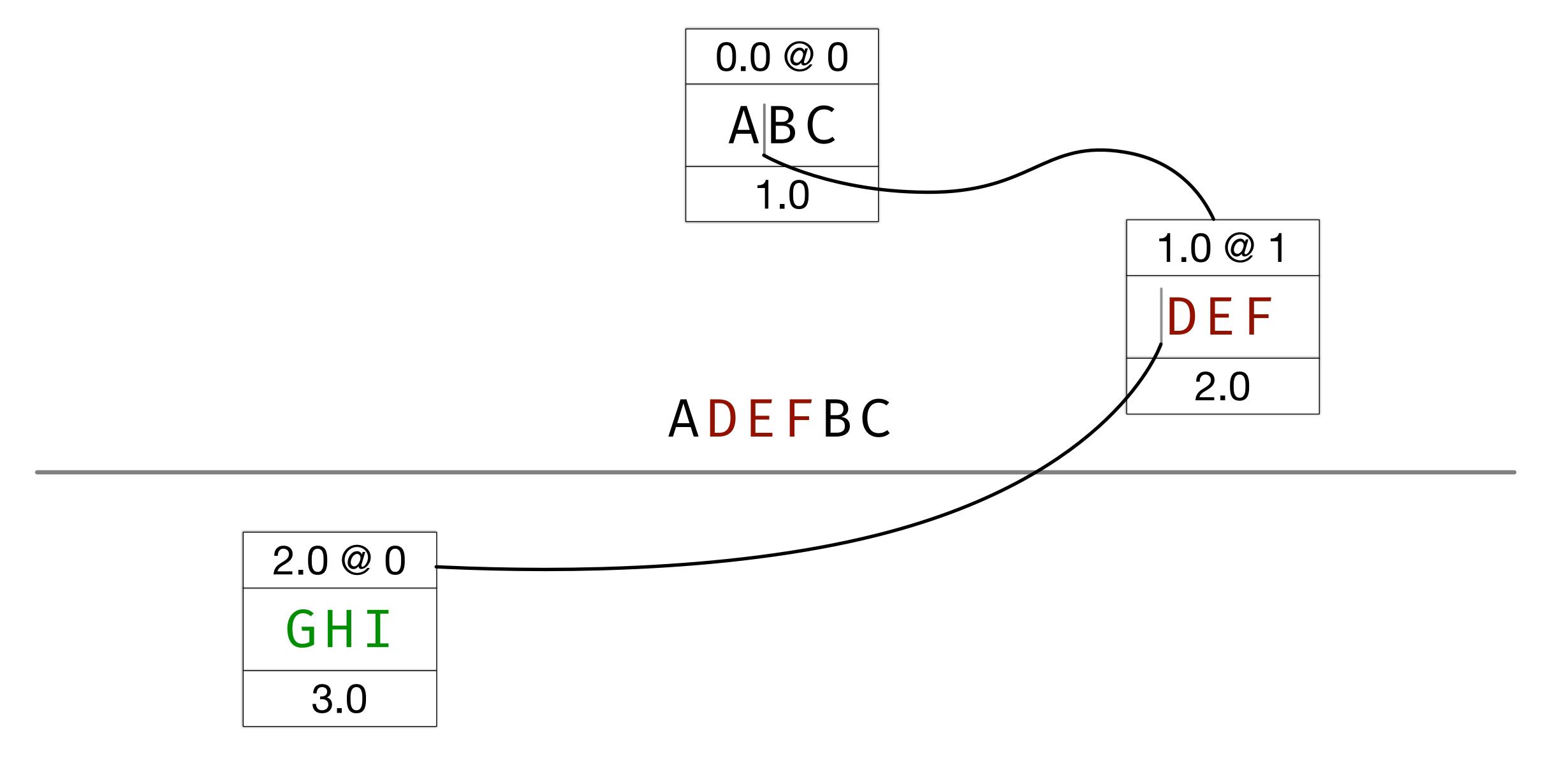
ADEFBC



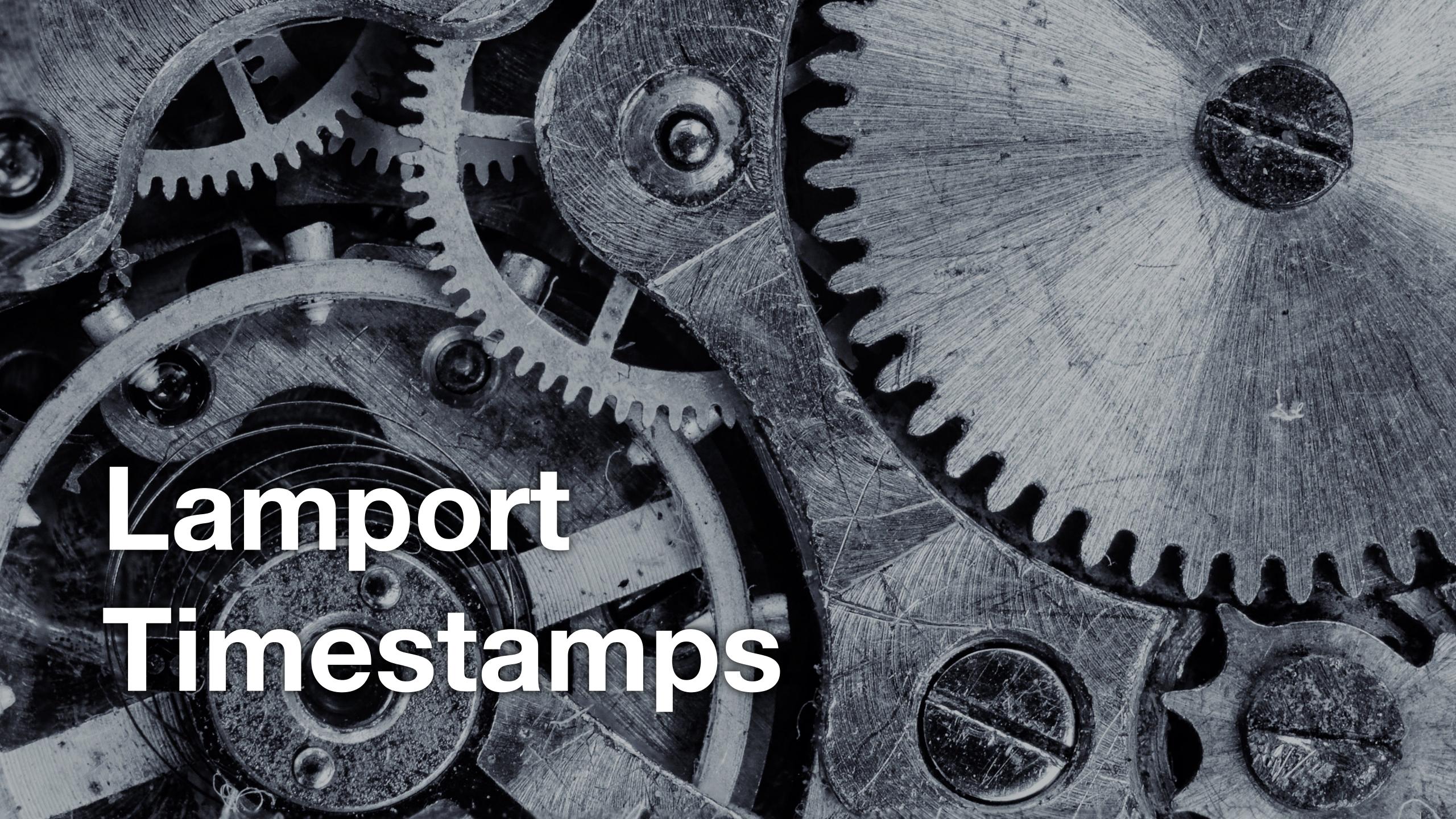
ADEFBC

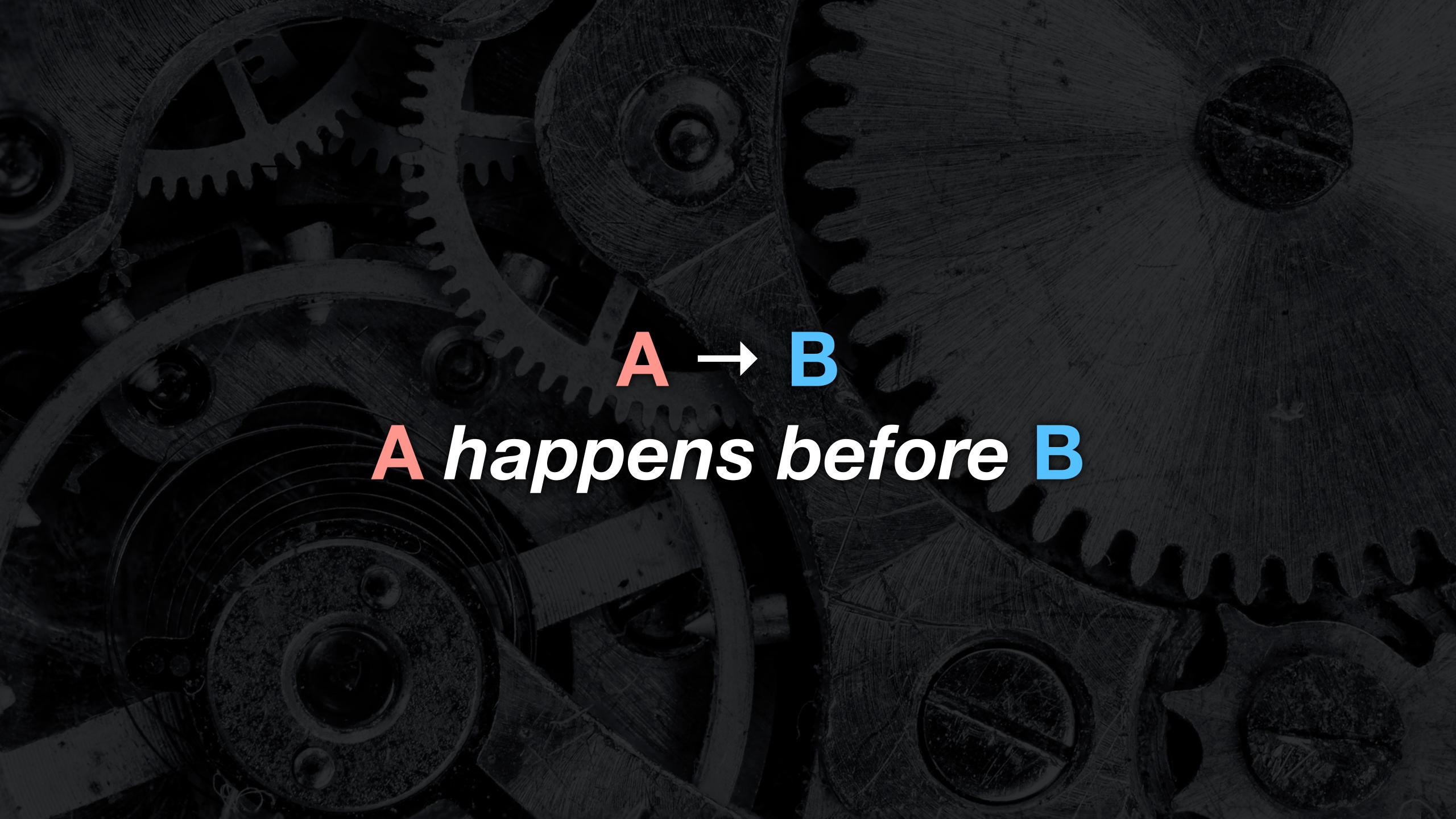


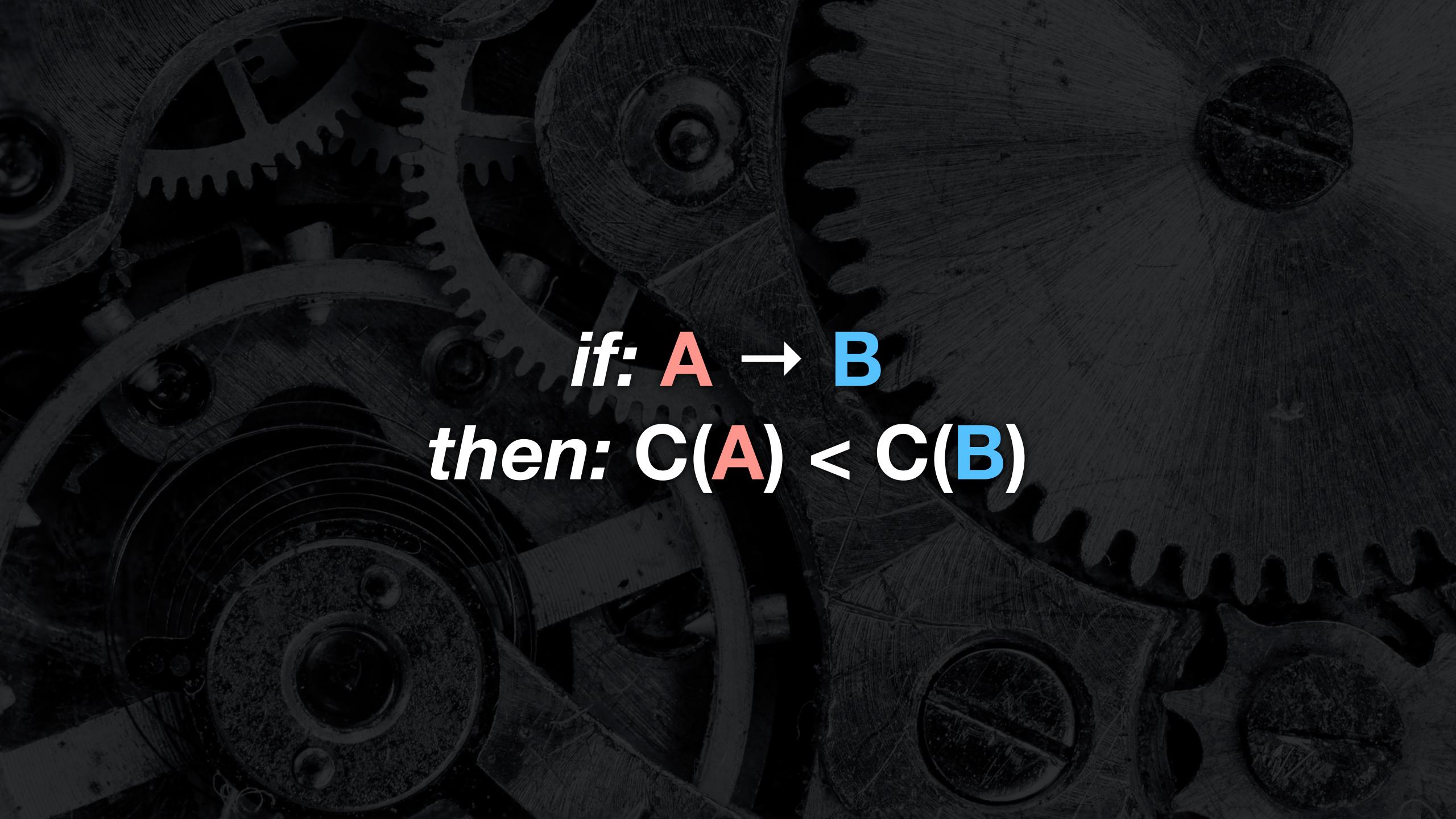
ADEFGHIBC



AGHIDEFBC





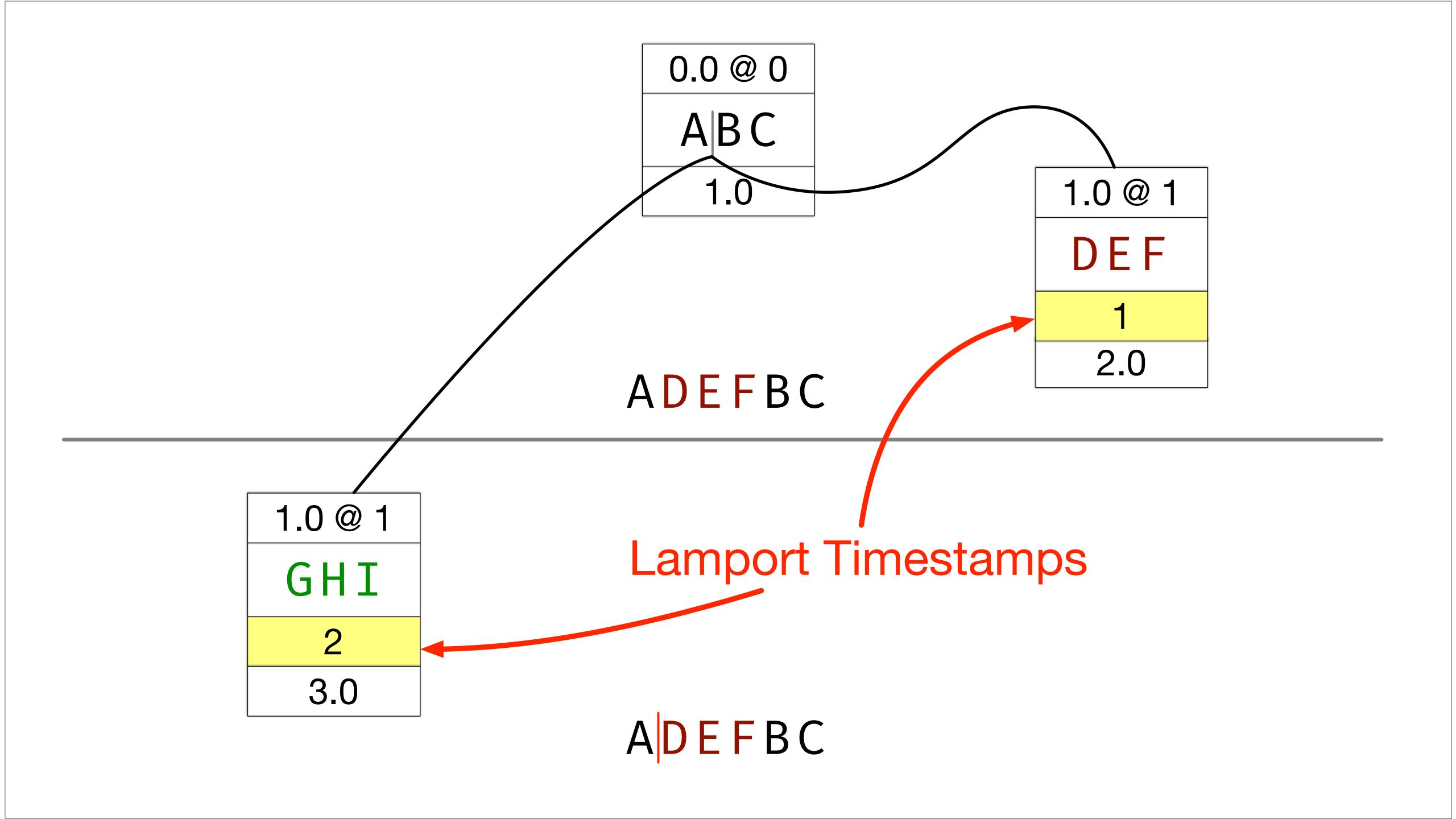


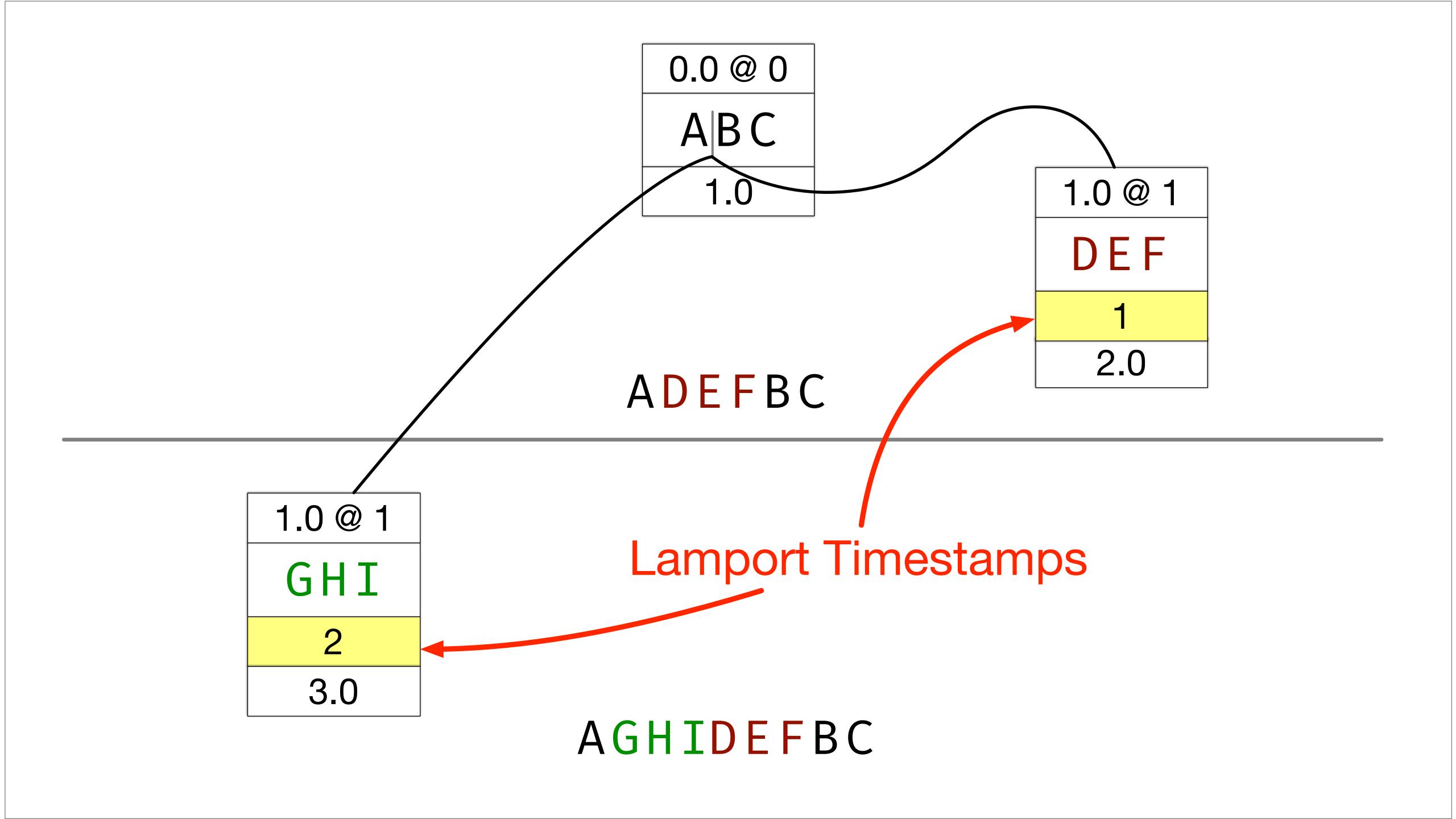
Sending:

```
clock += 1;
let timestamp = clock;
send(message, clock);
```

Receiving:

```
let (message, timestamp) = receive();
  clock = max(clock, timestamp) + 1;
```

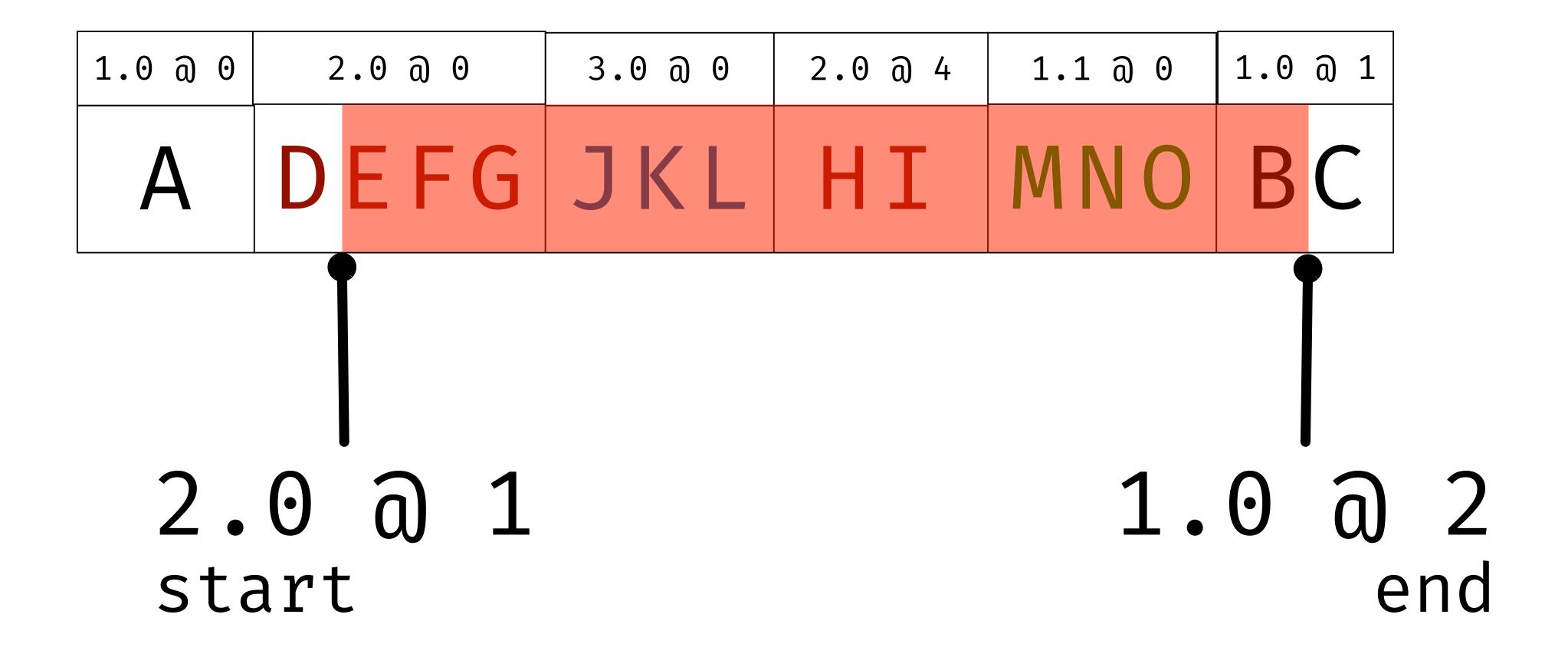


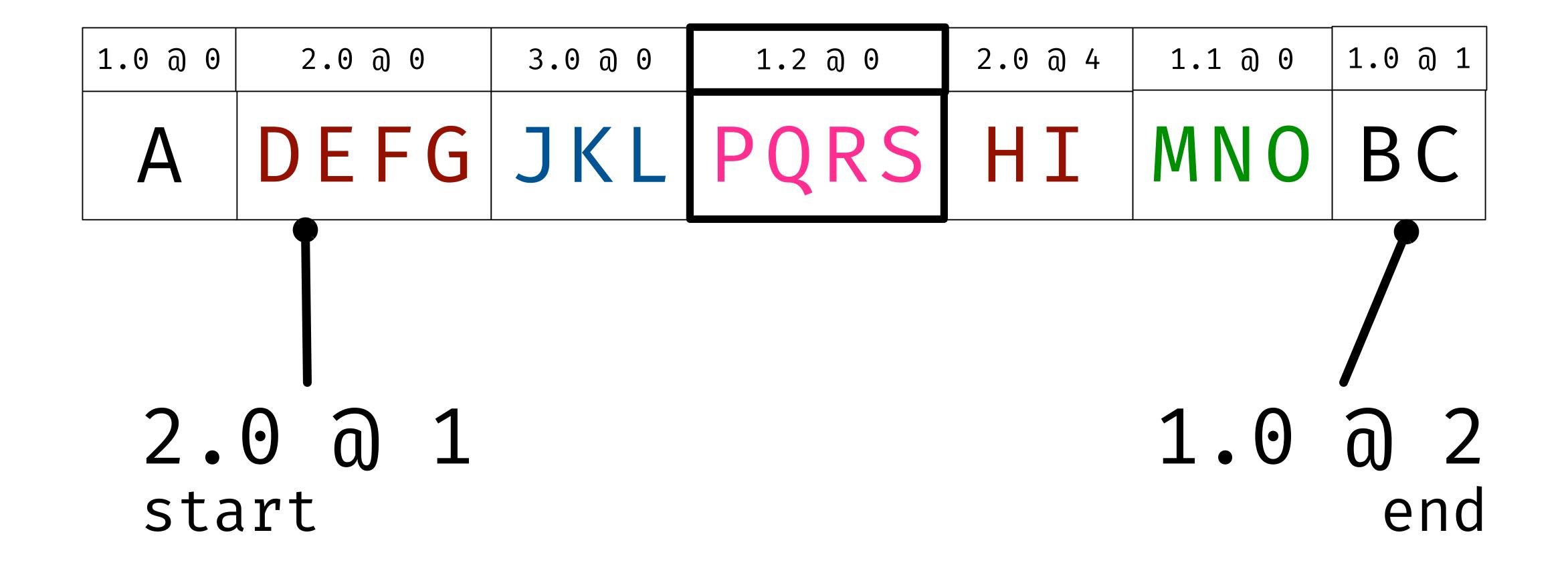


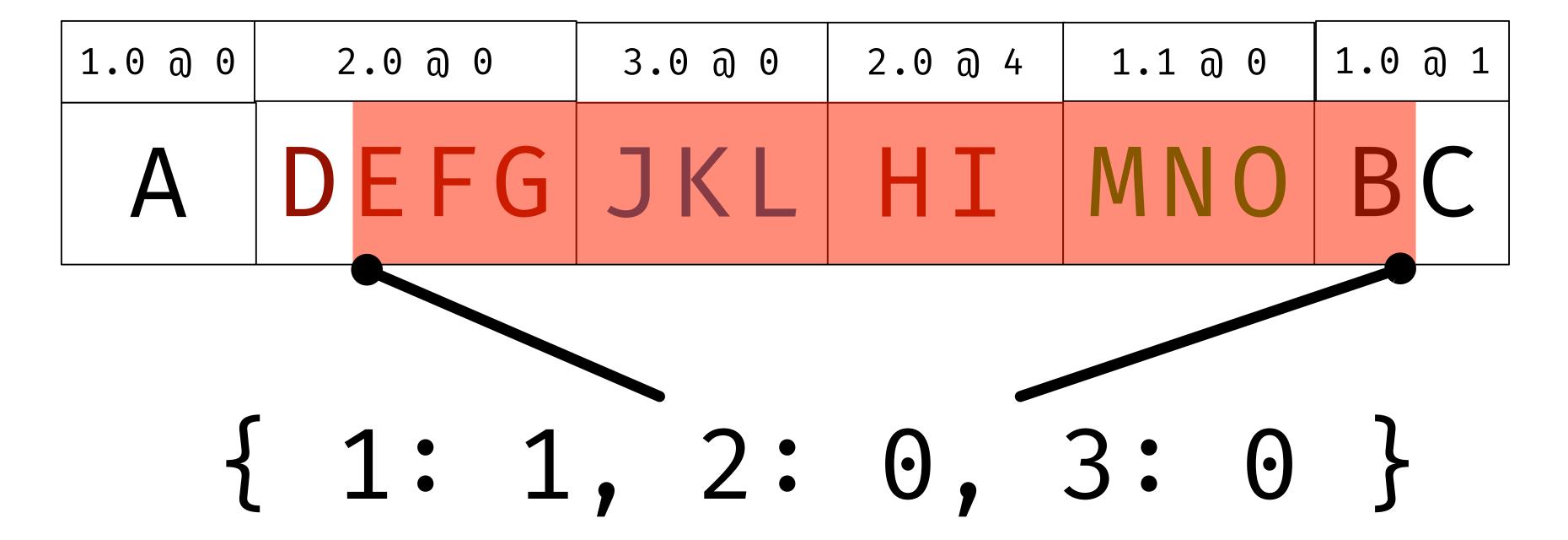


1.0 0 0	2.0 a 0	3.0 a 0	2.0 a 4	1.1 a 0	1.0 a 1
A	DEFG	JKL	ΗI	MNO	BC

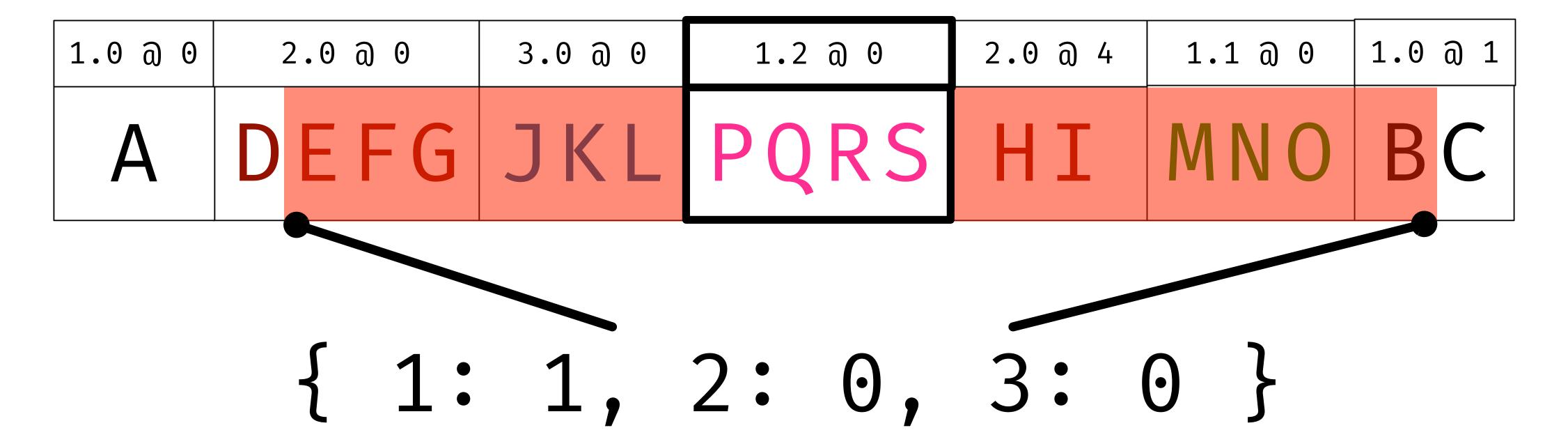
1.0 a 0	2.0 0 0		2.0 a 0 3.0 a 0 2.0 a 4		1.1 a 0	1.0 0 1	
A	DE	FG	JKL	НΙ	MNO	BC	







max sequence numbers in range



max sequence numbers in range

Deleted fragments are "tombstoned"

1.0 a 0	2.0 0 0	2.0 0 1	3.0 0 0	1.2 a 0	2.0 a 4	1.1 0 0	1.0 0 1	1.0 0 2
A	D	EFG	JKL	PQRS	ΗI	MNO	В	C
	•							,



2.1

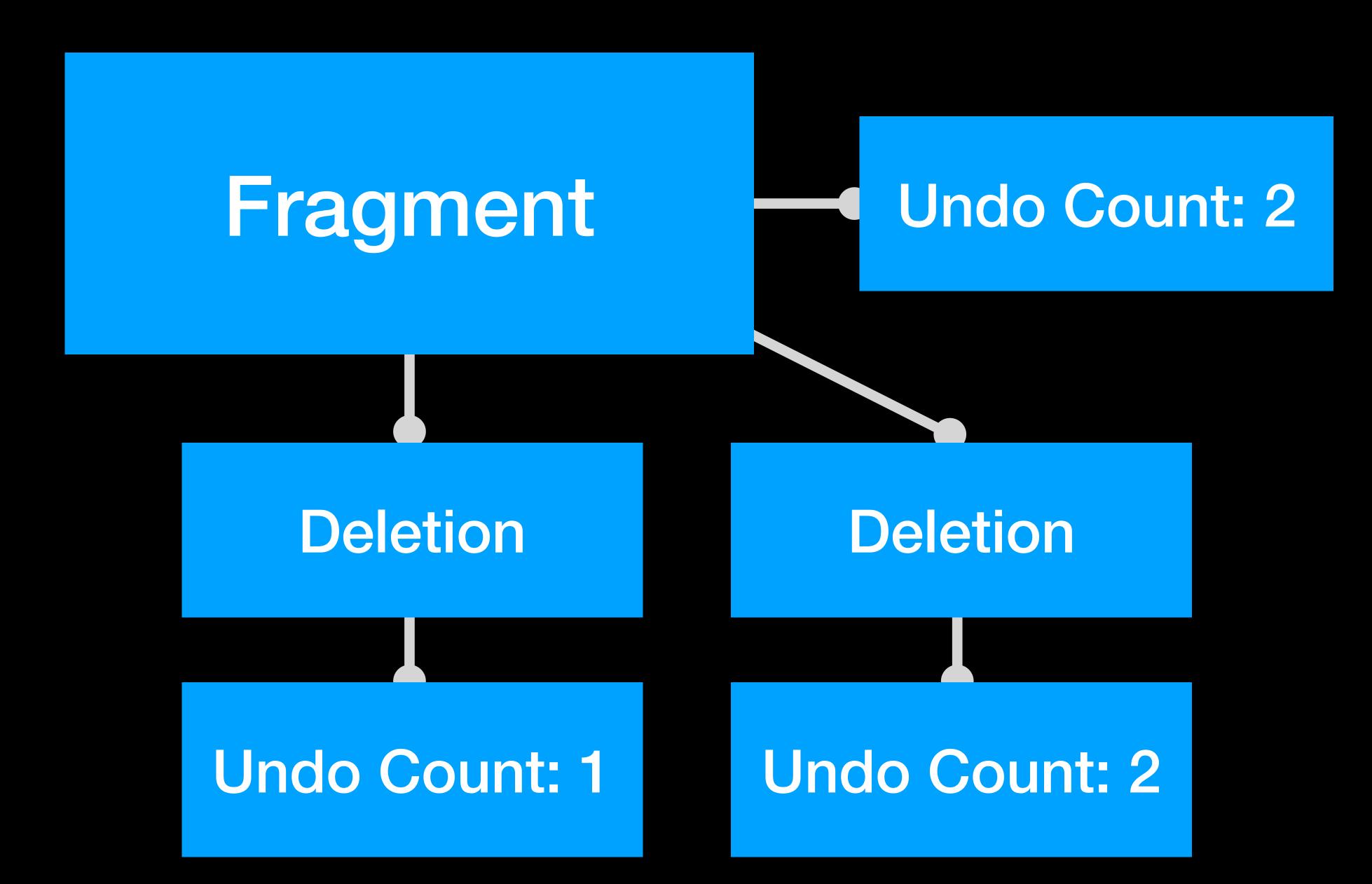
1

2.1

2.1

Undo and Redo





Fragment

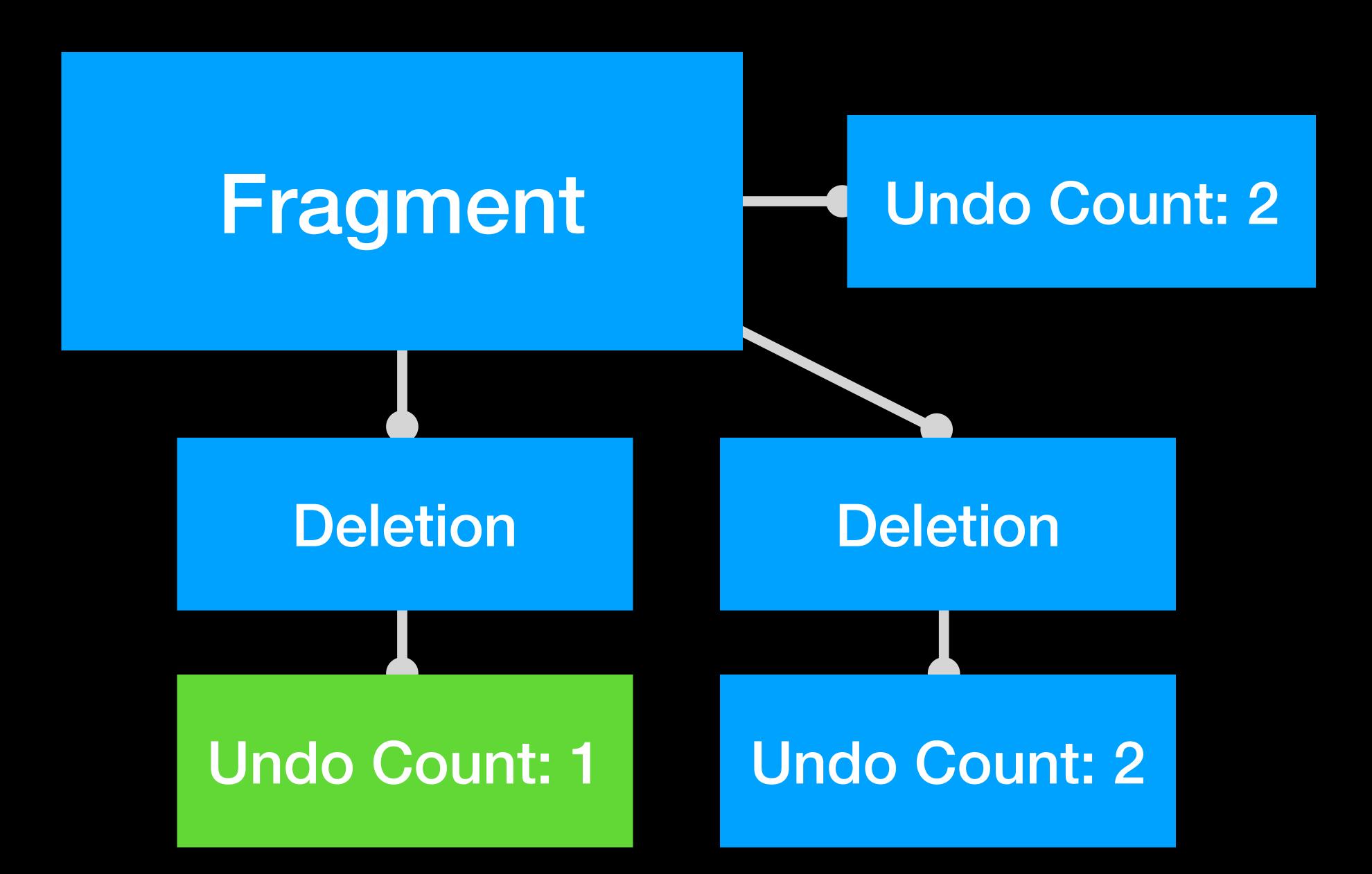
Undo Count: 2

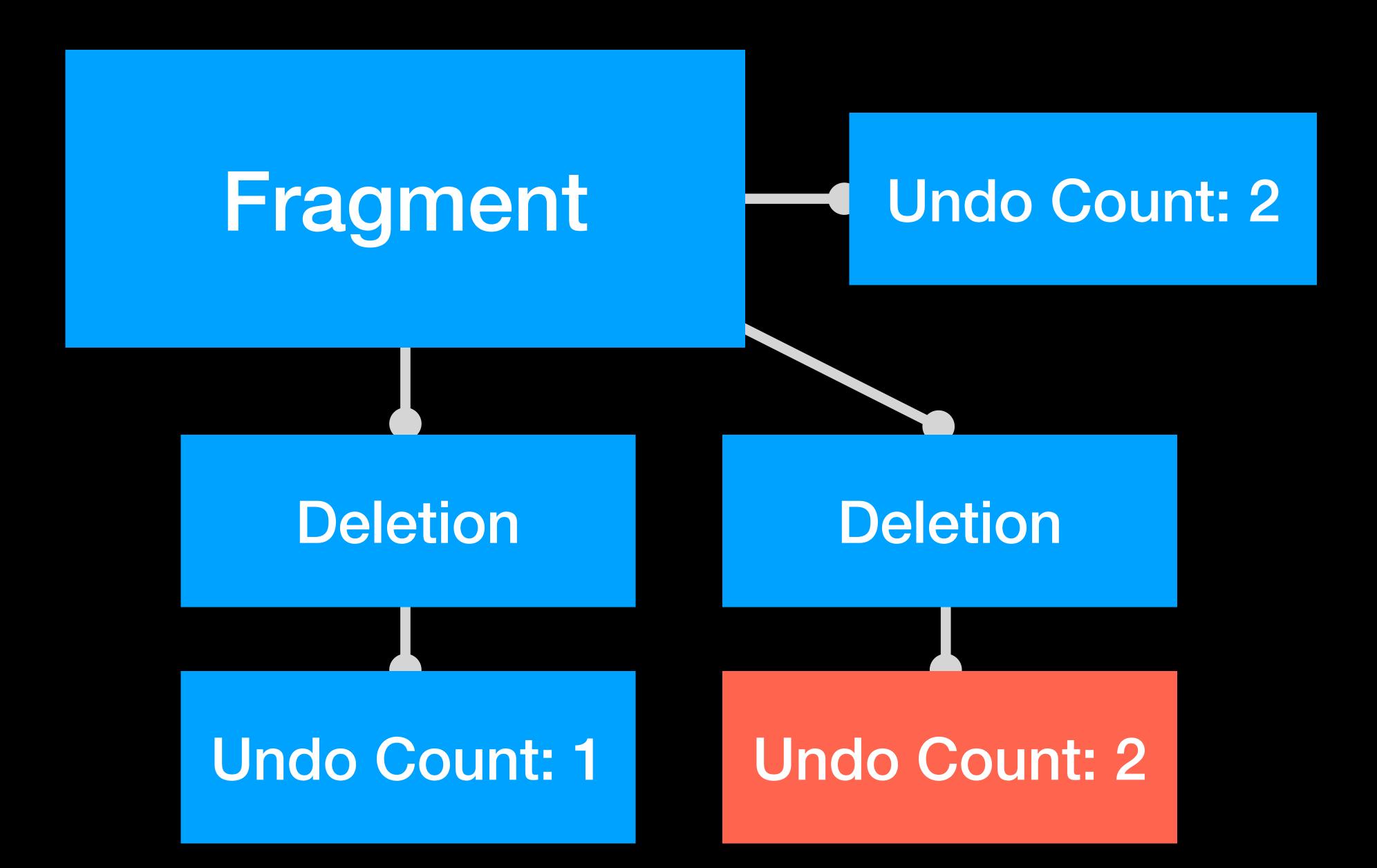
Deletion

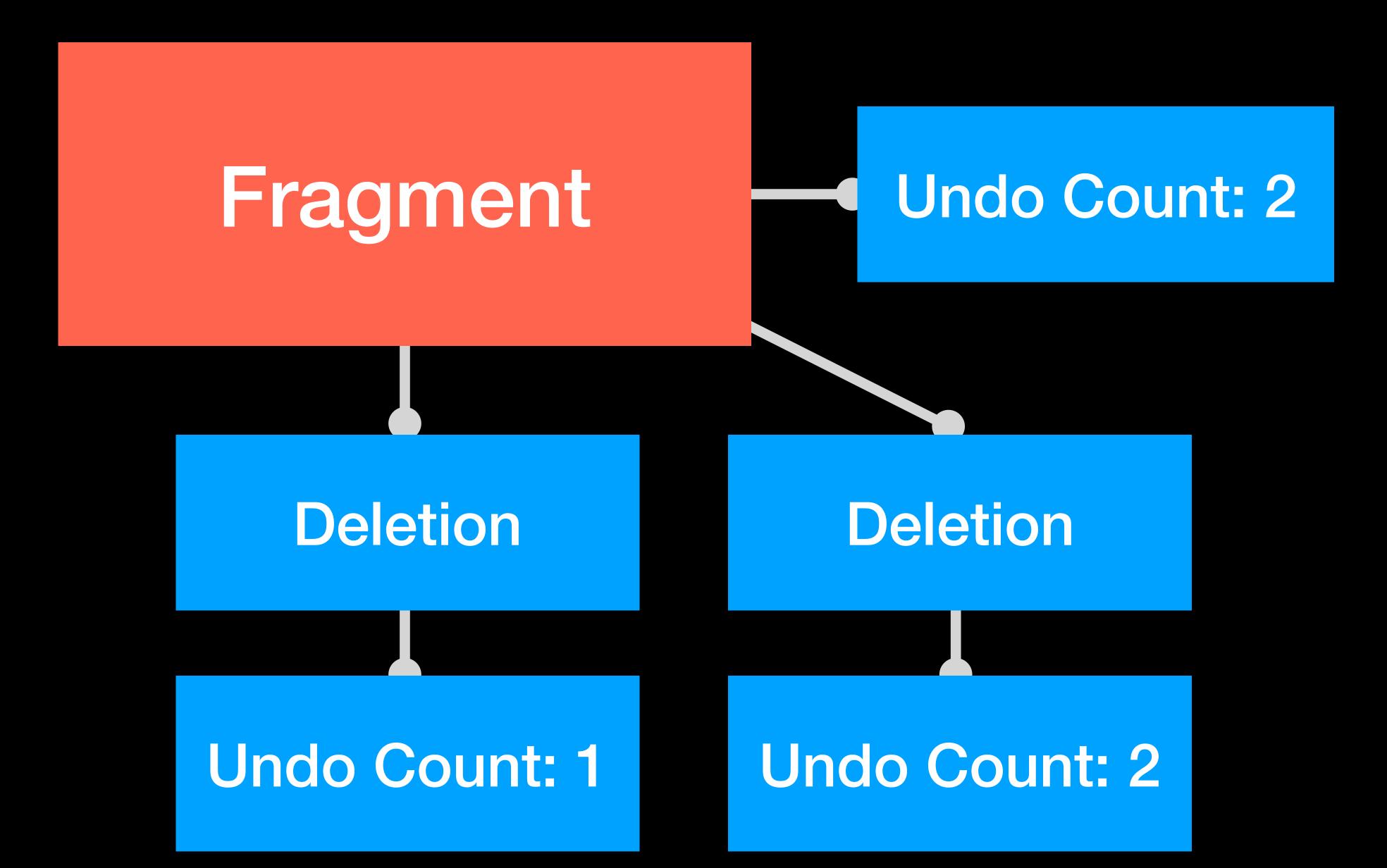
Deletion

Undo Count: 1

Undo Count: 2









2	0	2	3	4	2	3	0	1
AB	D	EF	JKL	PQRS	GH	MNO	Ι	C
1.0 0 0	2.0 0 0	2.0 a 1	3.0 0 0	1.2 0 0	2.0 a 3	1.1 0 0	2.0 a 5	1.0 0 2

Insert "X" at 12

2	0	2	3	4	2	3	0	1
AB	D	EF	JKL	PQRS	GH	MNO	Ι	C
1.0 0 0	2.0 a 0	2.0 0 1	3.0 0 0	1.2 0 0	2.0 a 3	1.1 0 0	2.0 a 5	1.0 a 2

Insert "X" at 12

2	0	2	3	4	2	3	0	1
AB	D	EF	JKL	PQRS	GH	MNO	Ι	C
1.0 0 0	2.0 0 0	2.0 0 1	3.0 0 0	1.2 0 0	2.0 a 3	1.1 a 0	2.0 a 5	1.0 a 2

Insert "X" at 12

2	0	2	3	4	2	3	0	1
AB	D	EF	JKL	PQRS	GH	MNO	Ι	C
1.0 0 0	2.0 0 0	2.0 a 1	3.0 0 0	1.2 0 0	2.0 a 3	1.1 a 0	2.0 0 5	1.0 a 2

Insert "X" at 12

			1					
2	0	2	3	4	2	3	0	1
AB	D	EF	JKL	PQRS	GH	MNO	Ι	C
1.0 a 0	2.0 a 0	2.0 a 1	3.0 0 0	1.2 0 0	2.0 a 3	1.1 0 0	2.0 0 5	1.0 a 2

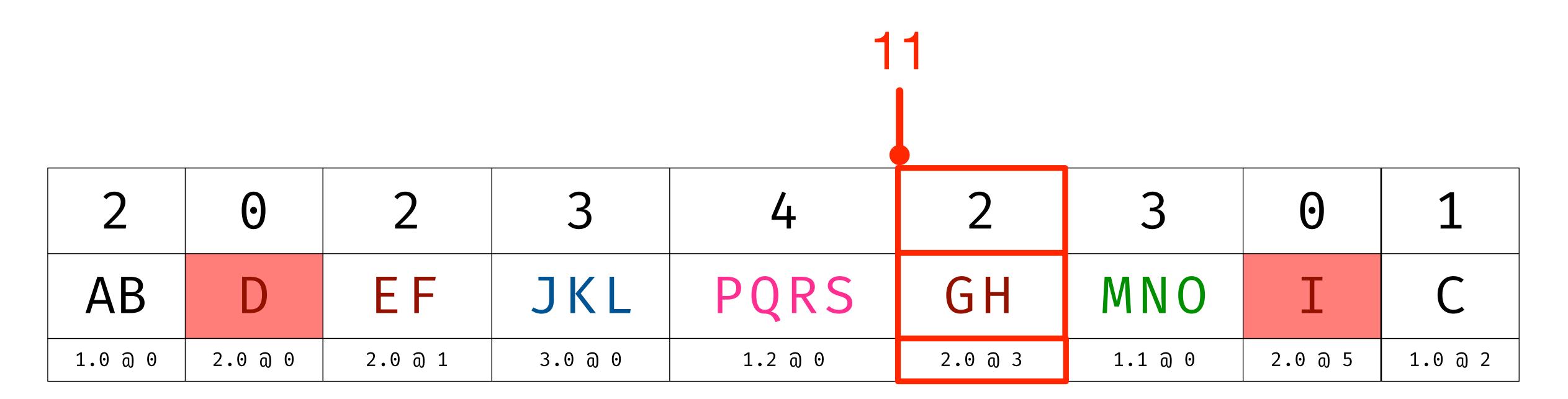
Insert "X" at 12

2	0	2	3	4	2	3	0	1
AB	D	EF	JKL	PQRS	GH	MNO	Ι	C
1.0 0 0	2.0 a 0	2.0 a 1	3.0 0 0	1.2 0 0	2.0 a 3	1.1 a 0	2.0 a 5	1.0 a 2

Insert "X" at 12

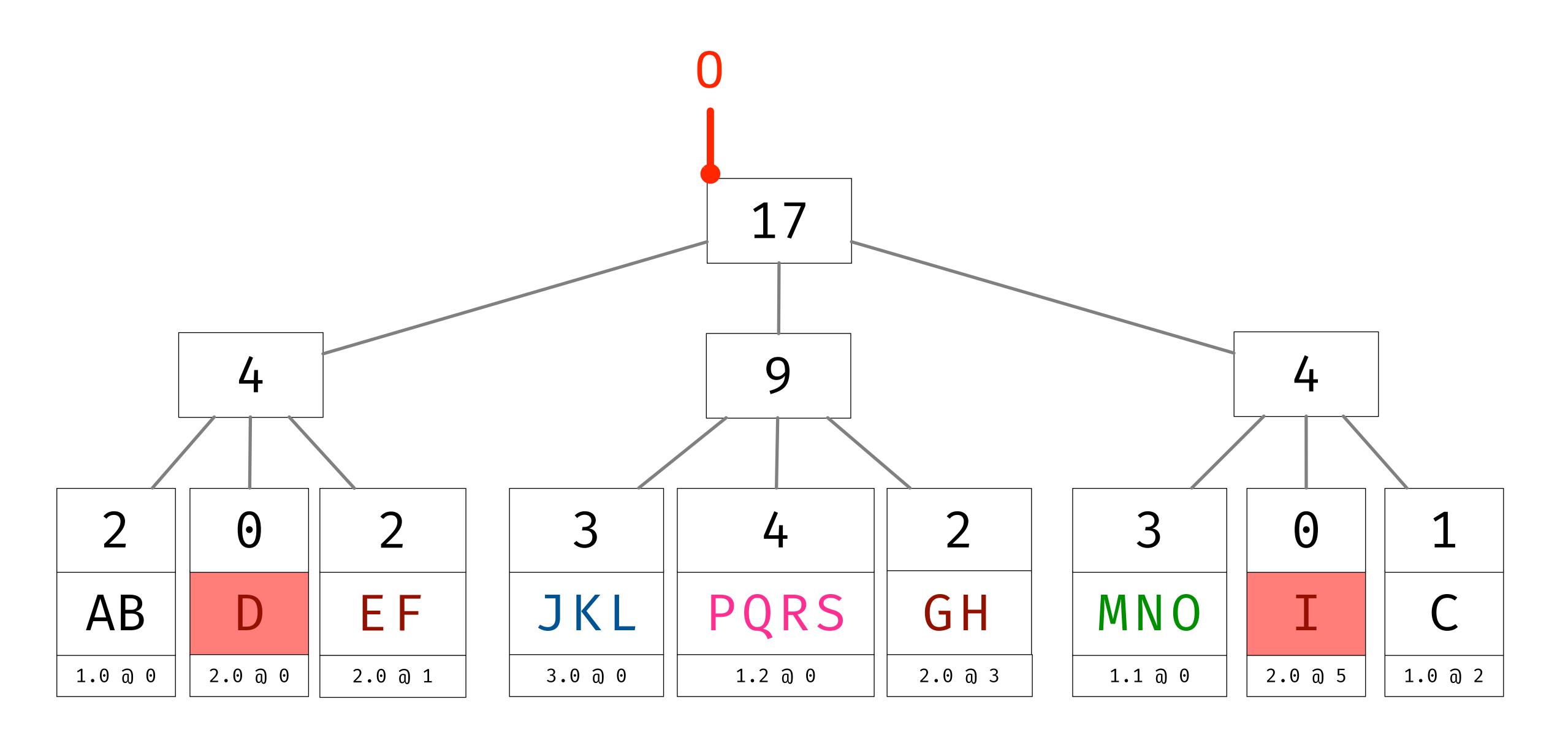
		11						
2	0	2	3	4	2	3	0	1
AB	D	EF	JKL	PQRS	GH	MNO	Ι	C
1.0 a 0	2.0 0 0	2.0 0 1	3.0 0 0	1.2 0 0	2.0 a 3	1.1 0 0	2.0 a 5	1.0 a 2

Insert "X" at 12

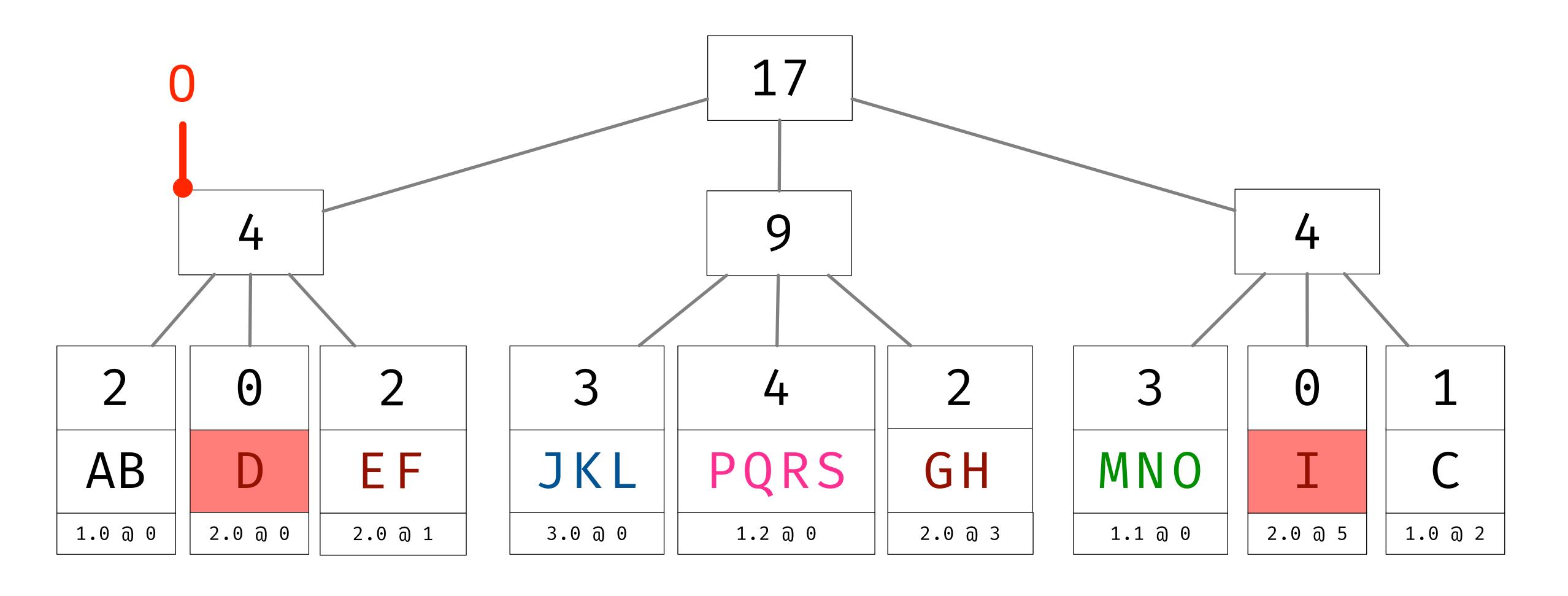


Local: Insert "X" at 12

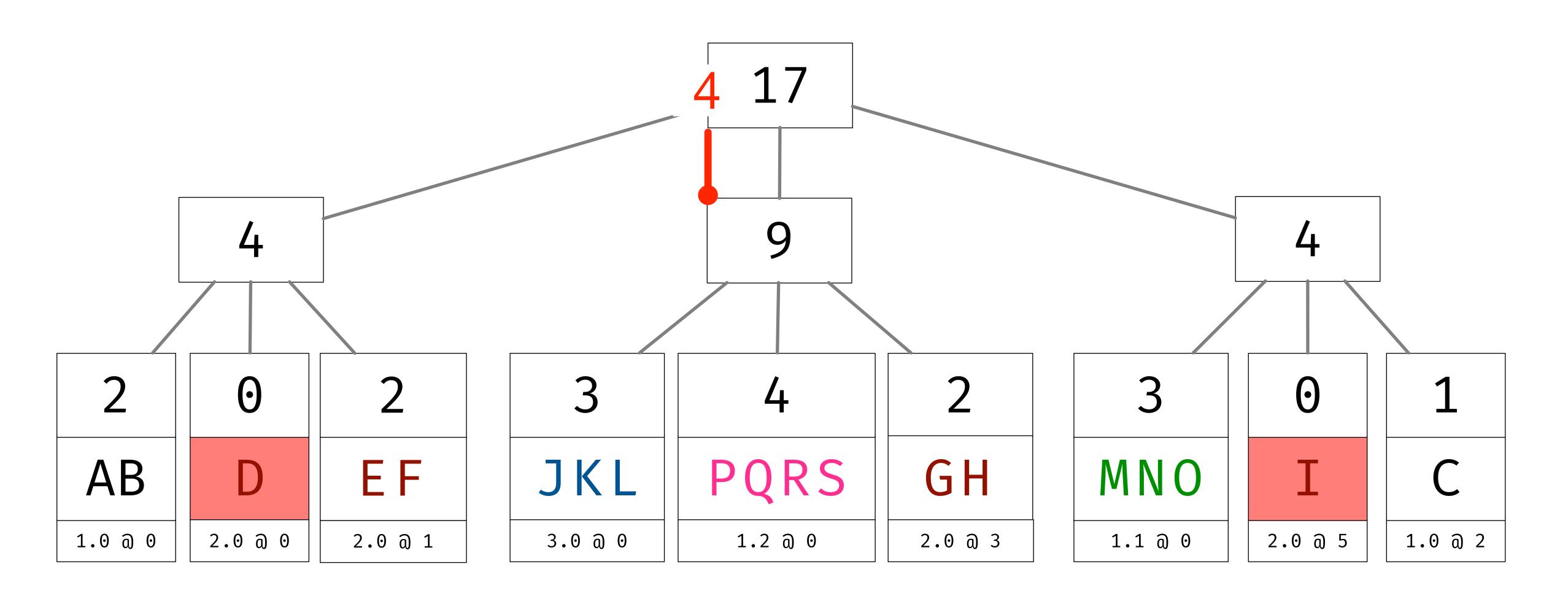
Remote: Insert "X" at 2.0 @ 4



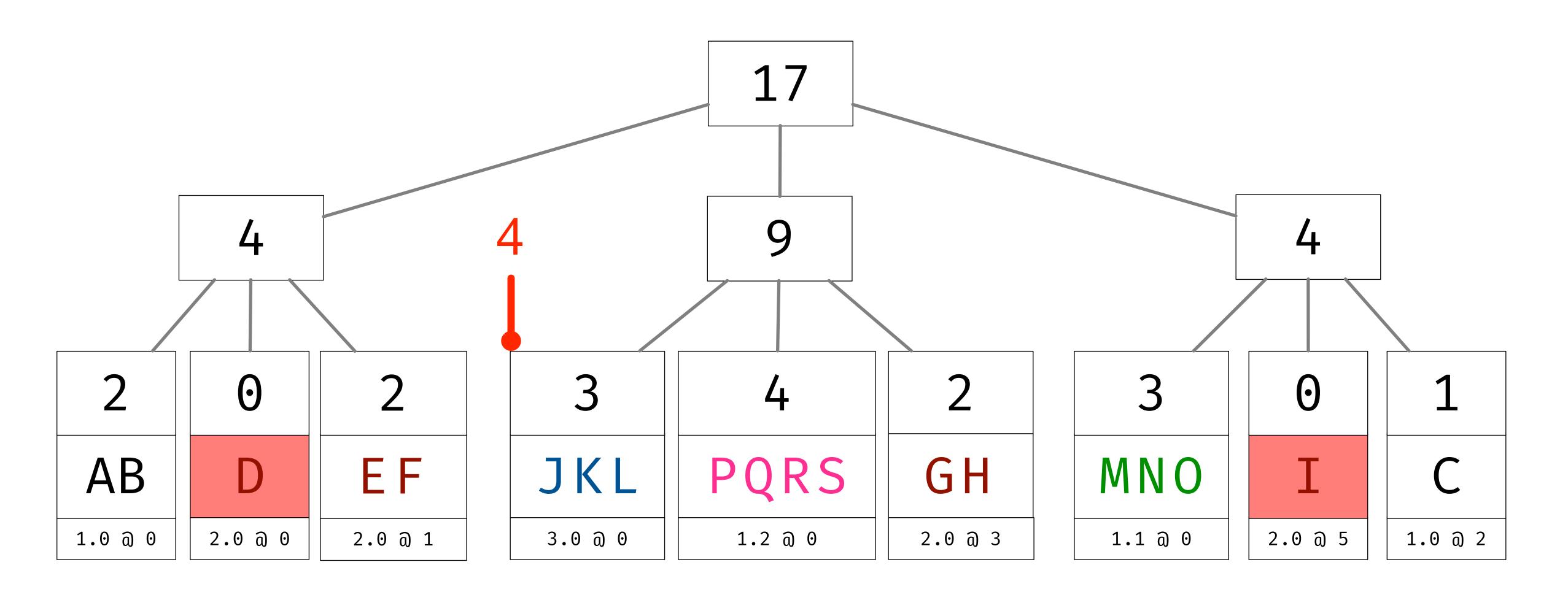
Insert "X" at 12



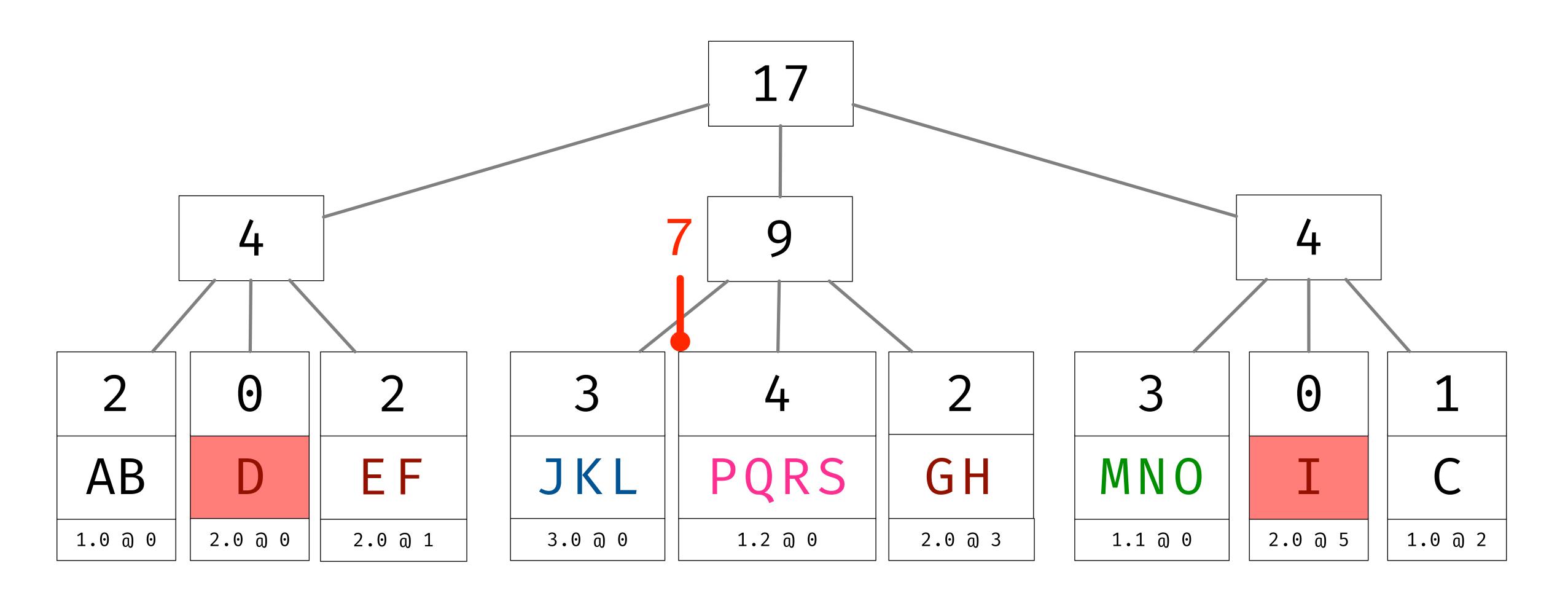
Insert "X" at 12



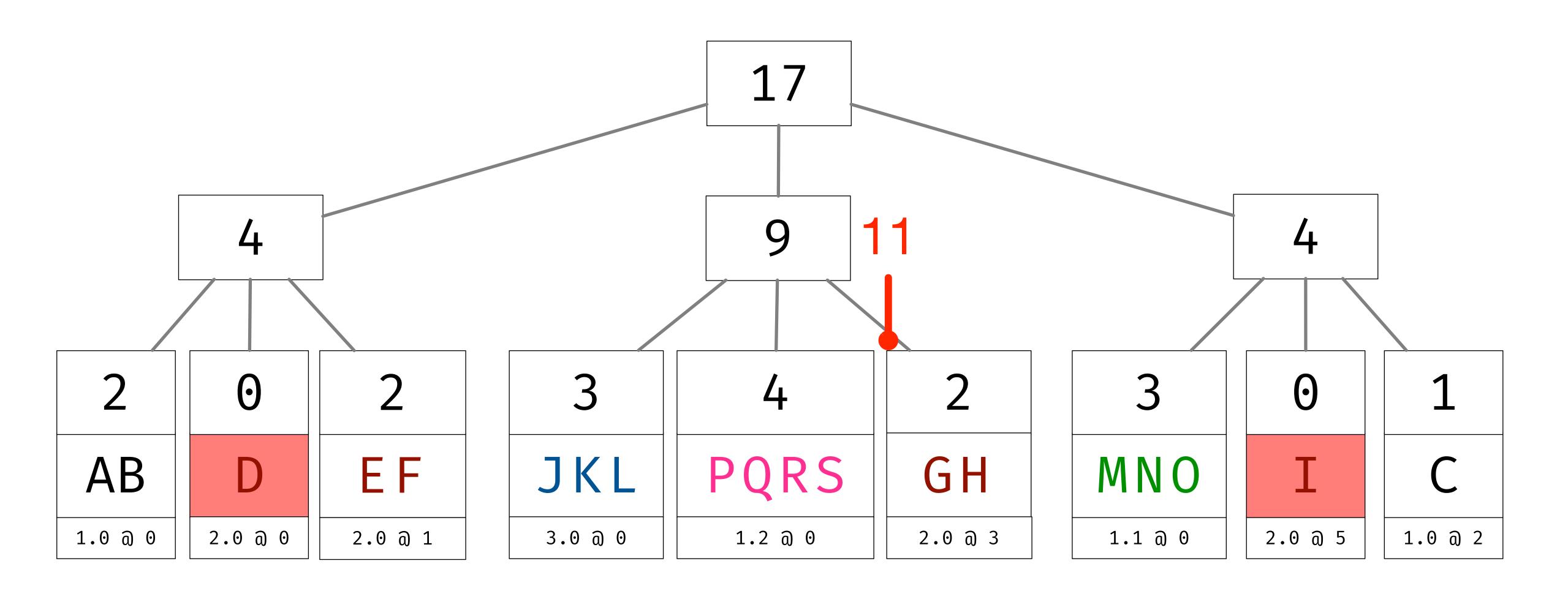
Insert "X" at 12



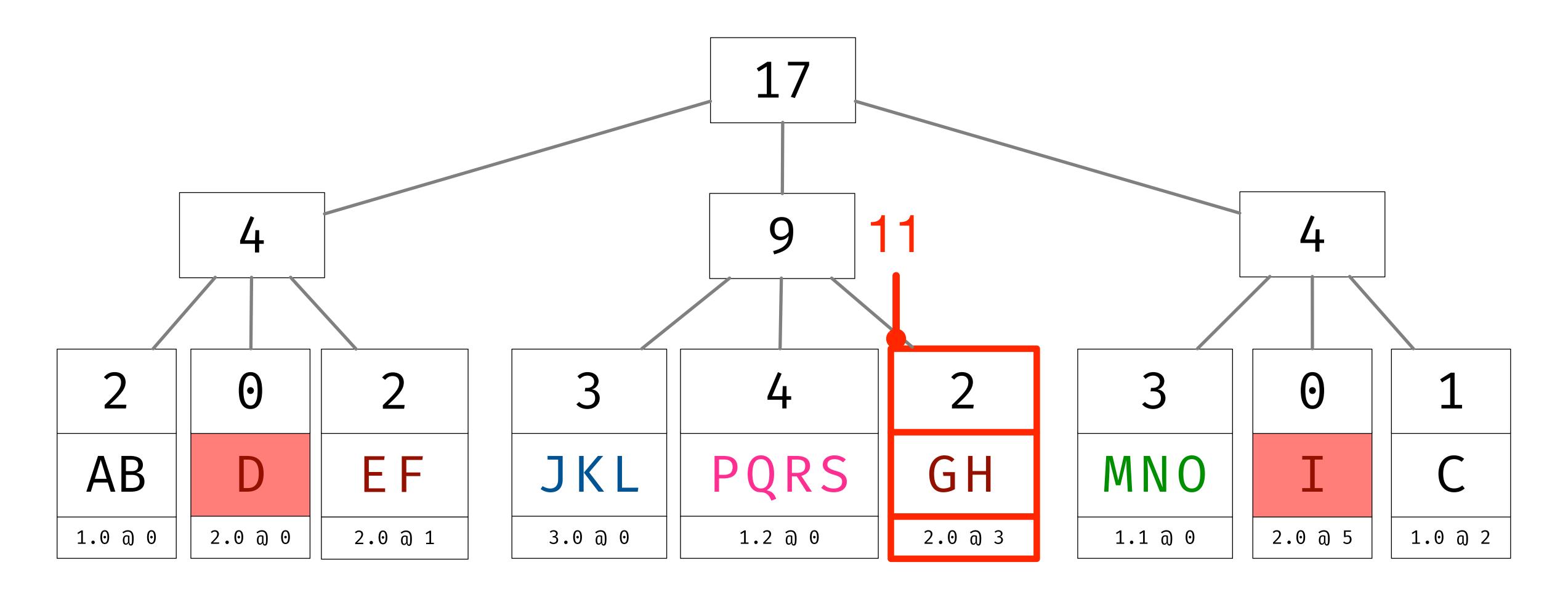
Insert "X" at 12



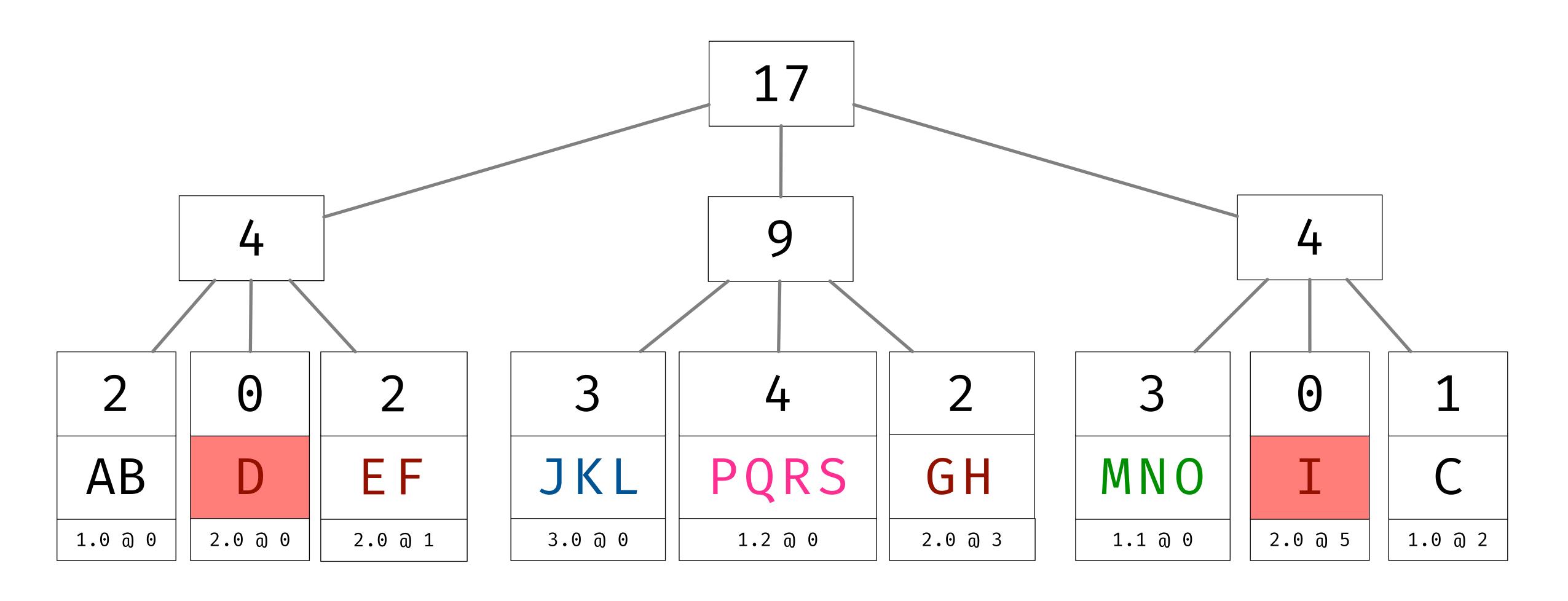
Insert "X" at 12



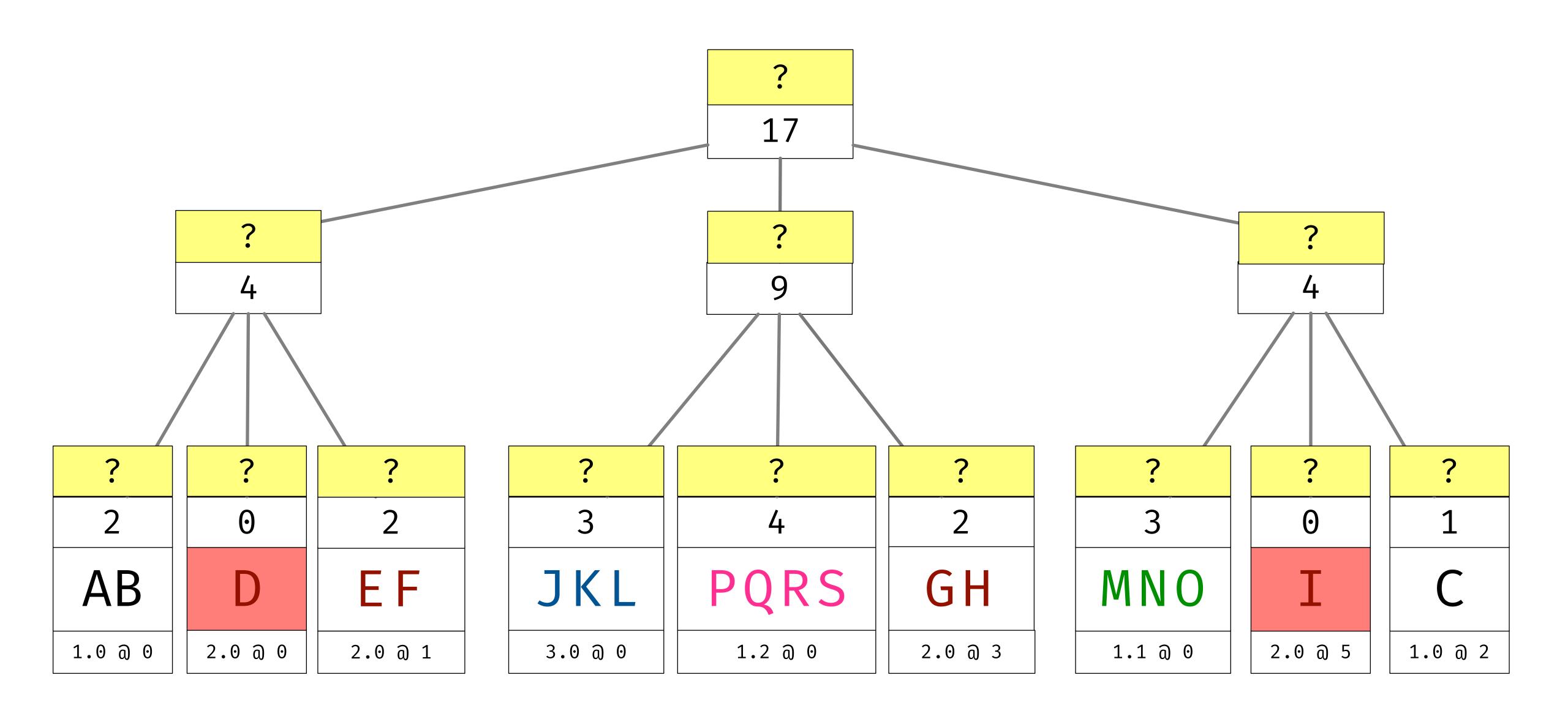
Insert "X" at 12



Insert "X" at 2.0 @ 4



Insert "X" at 2.0 @ 4



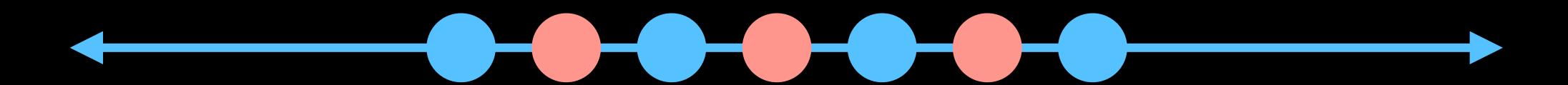
Insert "X" at 2.0 @ 4

Fragment Identifiers

Totally-Ordered

Fragment Identifiers

Totally-Ordered



Dense

Integers?

Floats?

1.1 < 1.2



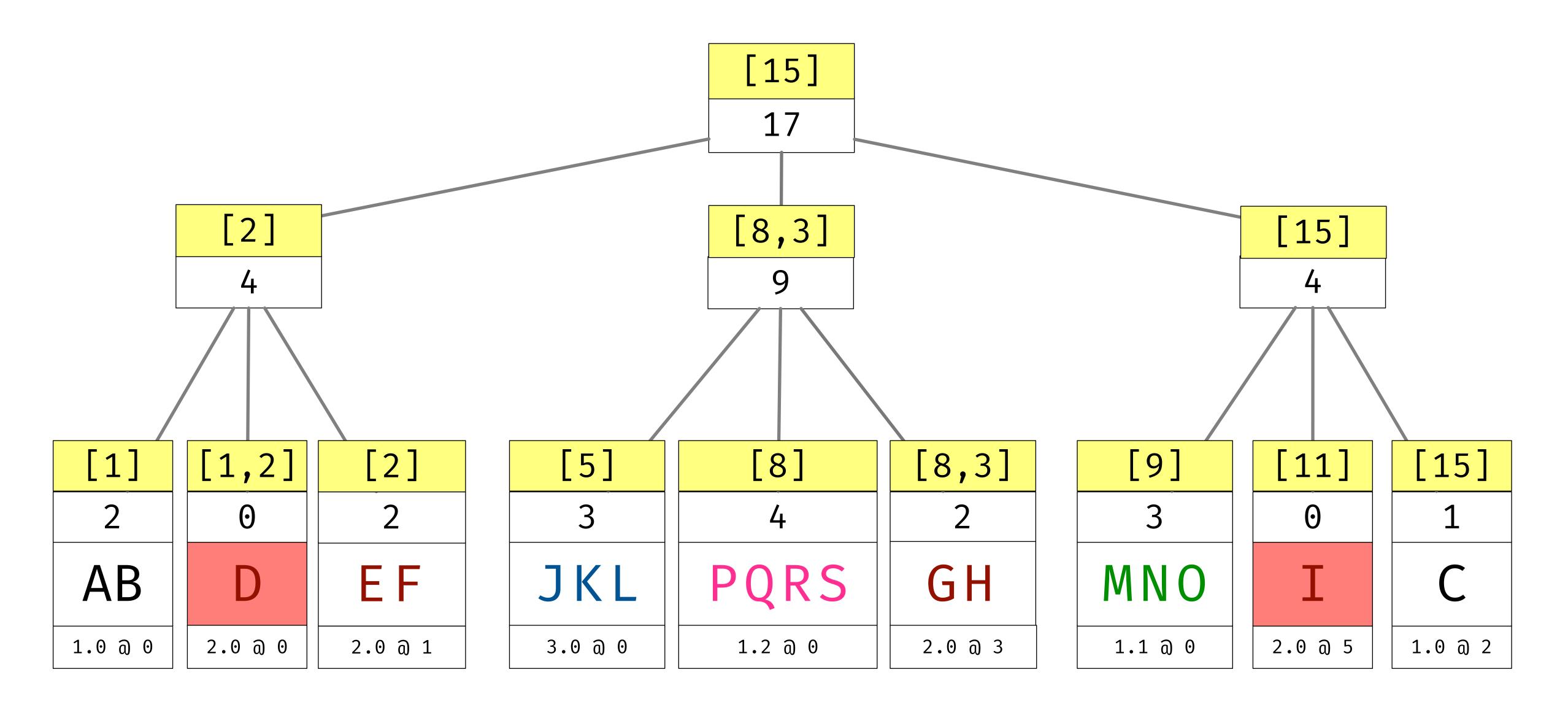
10-308 < ? < 2 × 10-308



Strings

A<B

A<B<B



Insert "X" at 2.0 @ 4

2.0 0 0

2.0 0 0

DEFGH	Ι	
2.0 0 0	2.0 a 5	

2.0 a 0

DEFGH	Ι	
2.0 0 0	2.0 a 5	

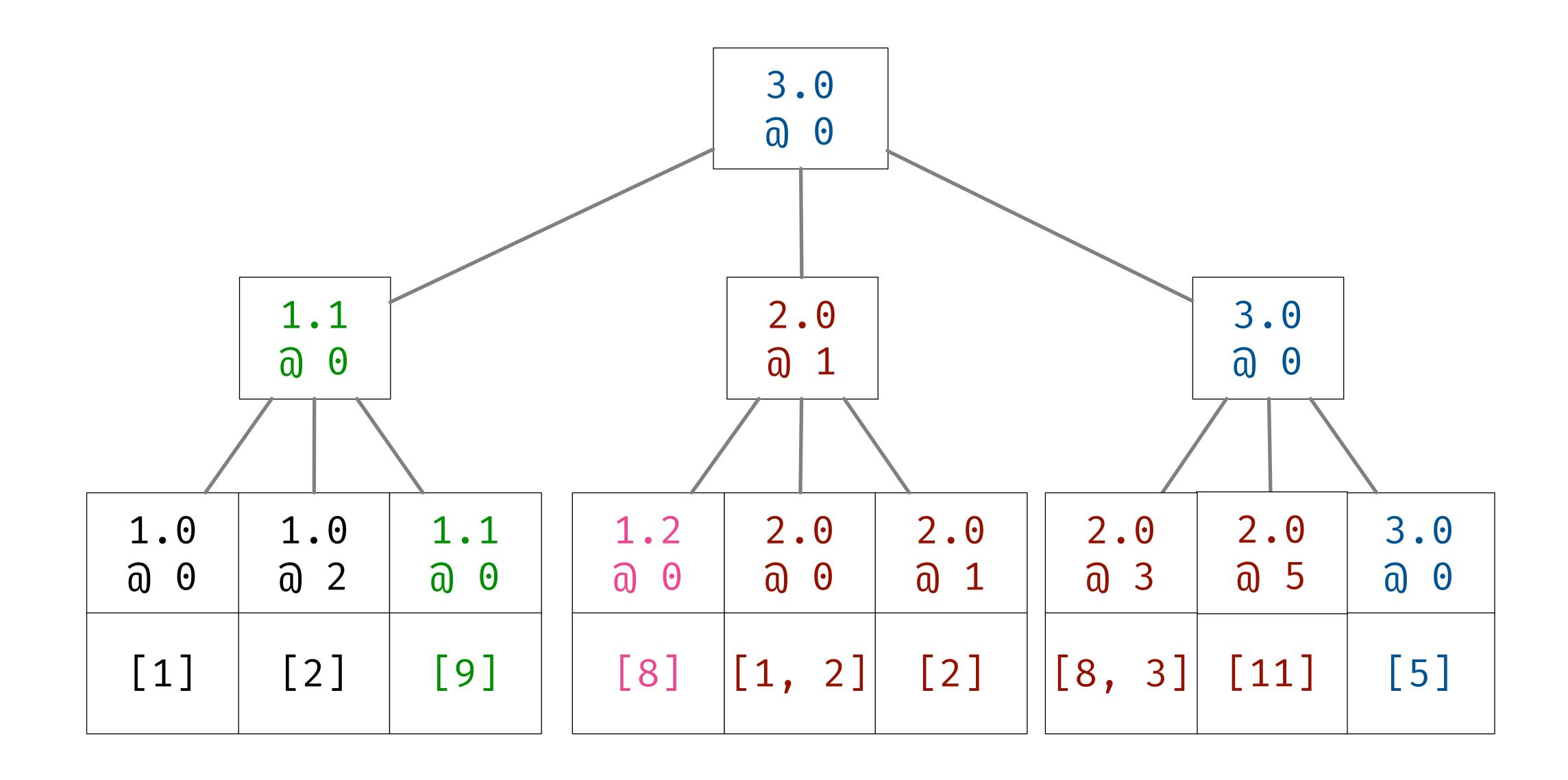
D	EFGH	
2.0 0 0	2.0 a 1	2.0 0 5

2.0 a 0

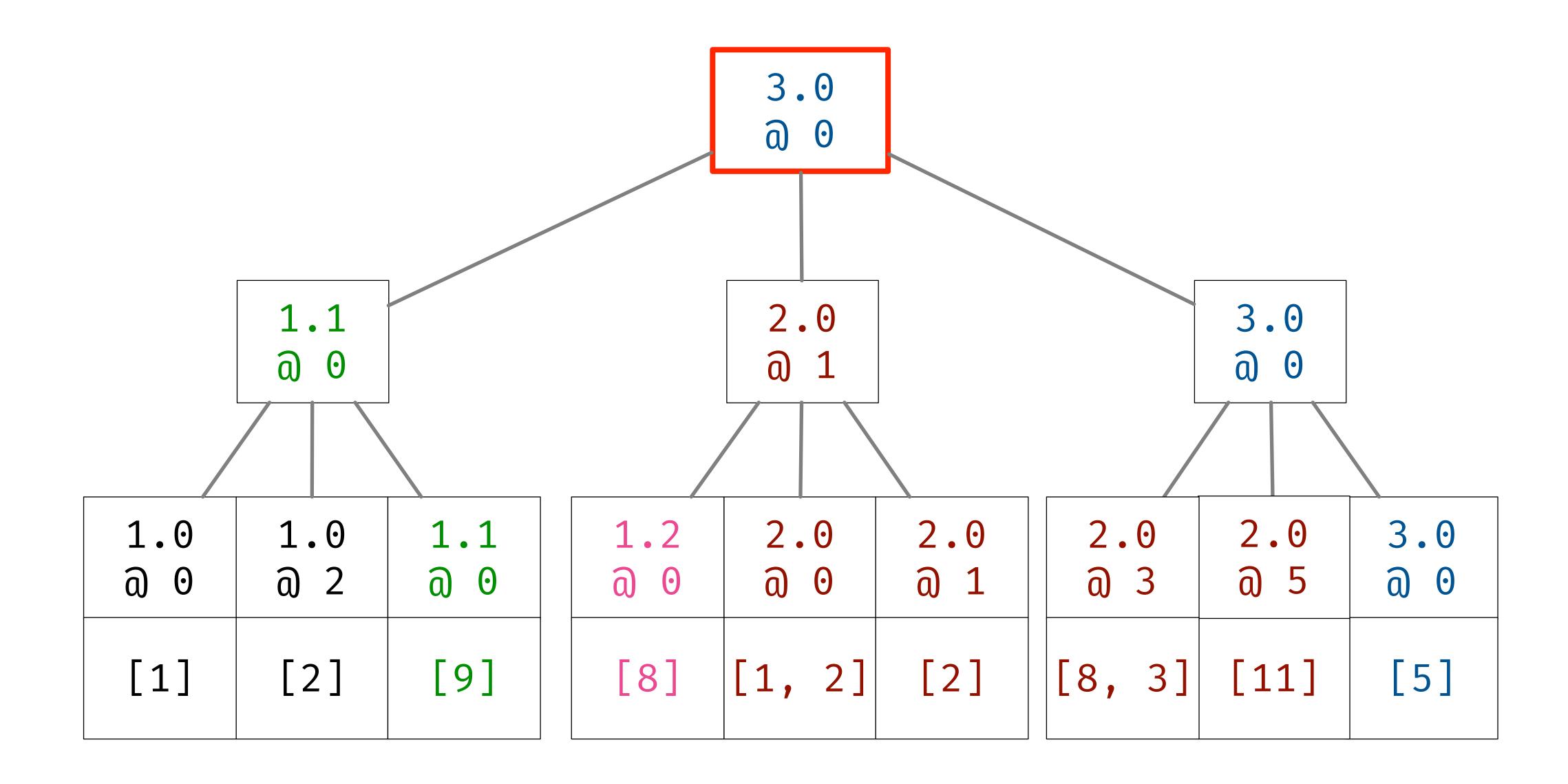
DEFGH	Ι		
2.0 0 0	2.0 0 5		

D	EFGH	Ι
2.0 0 0	2.0 a 1	2.0 a 5

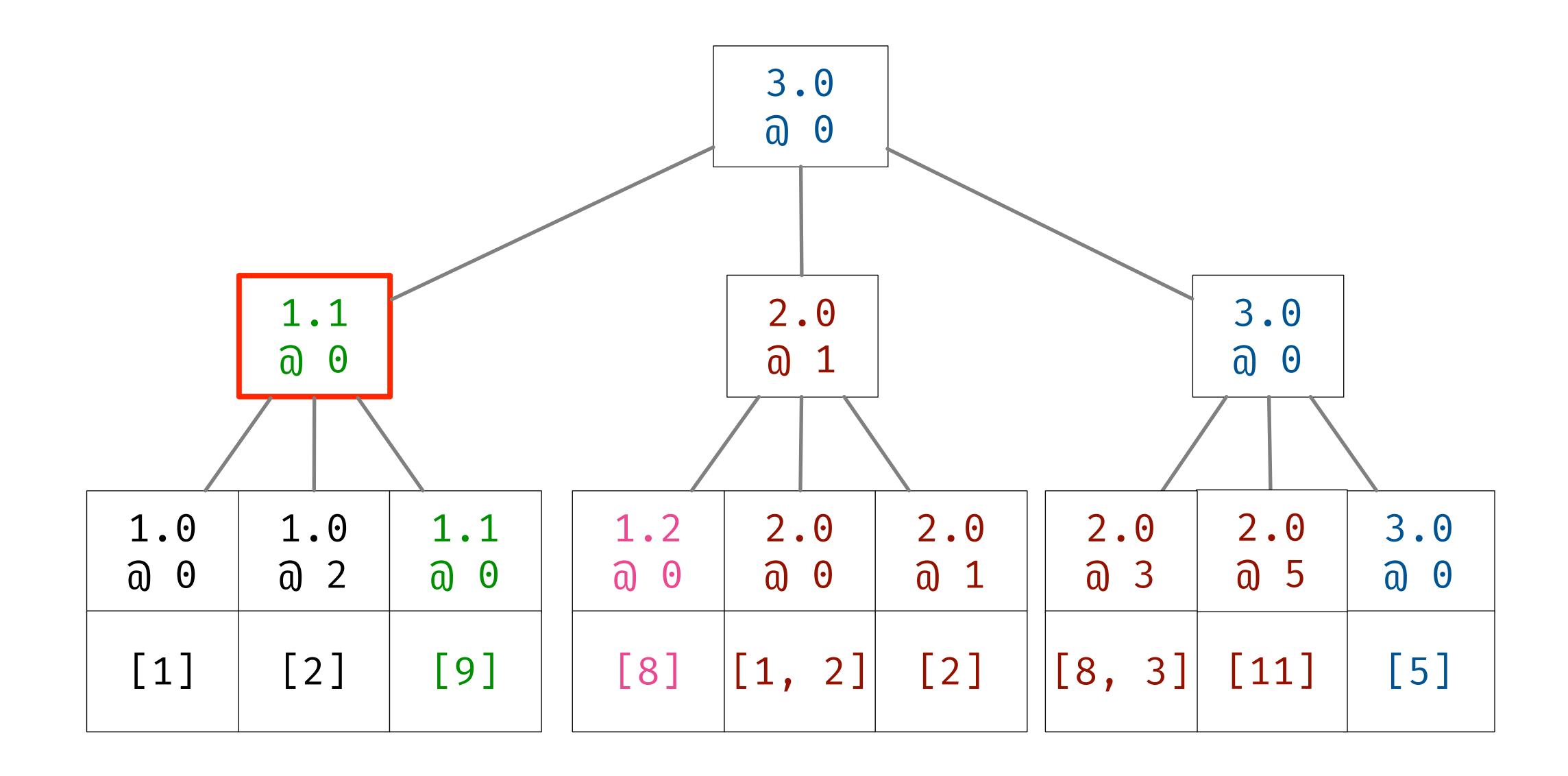
D	EF	GH	Ι
2.0 0 0	2.0 a 1	2.0 a 3	2.0 a 5



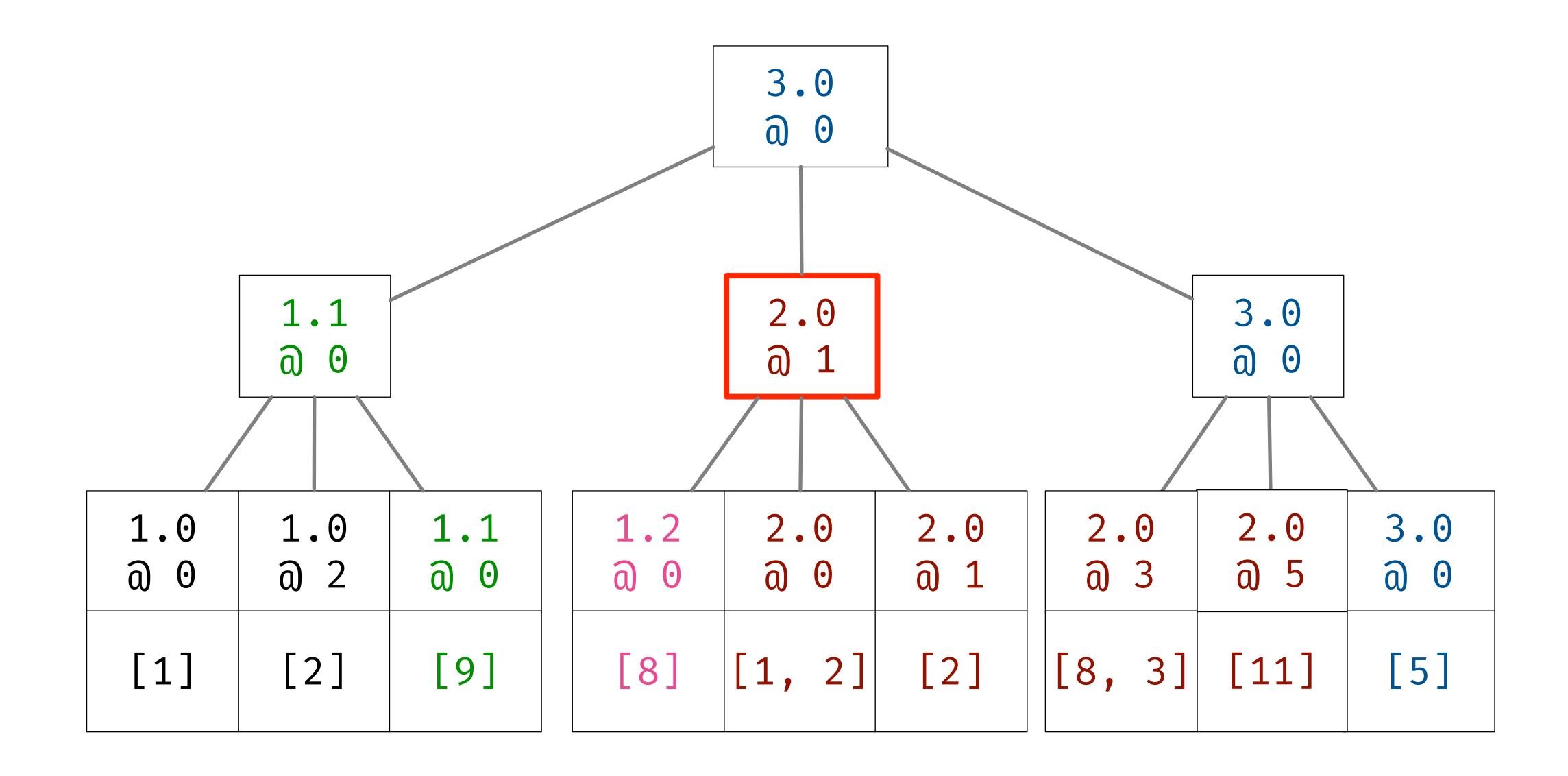
Insertion Split Tree



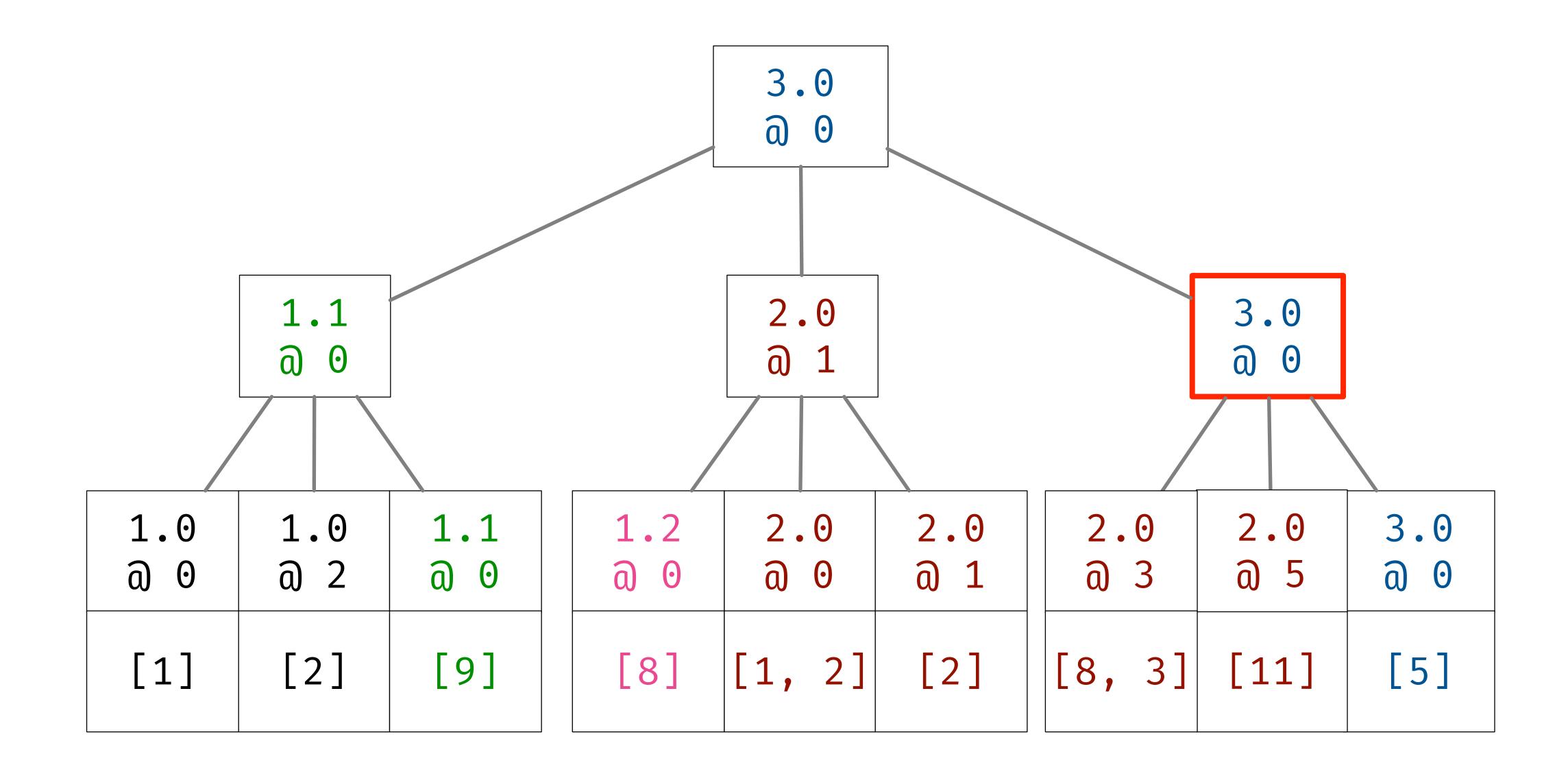
Insert "X" at 2.0 @ 4



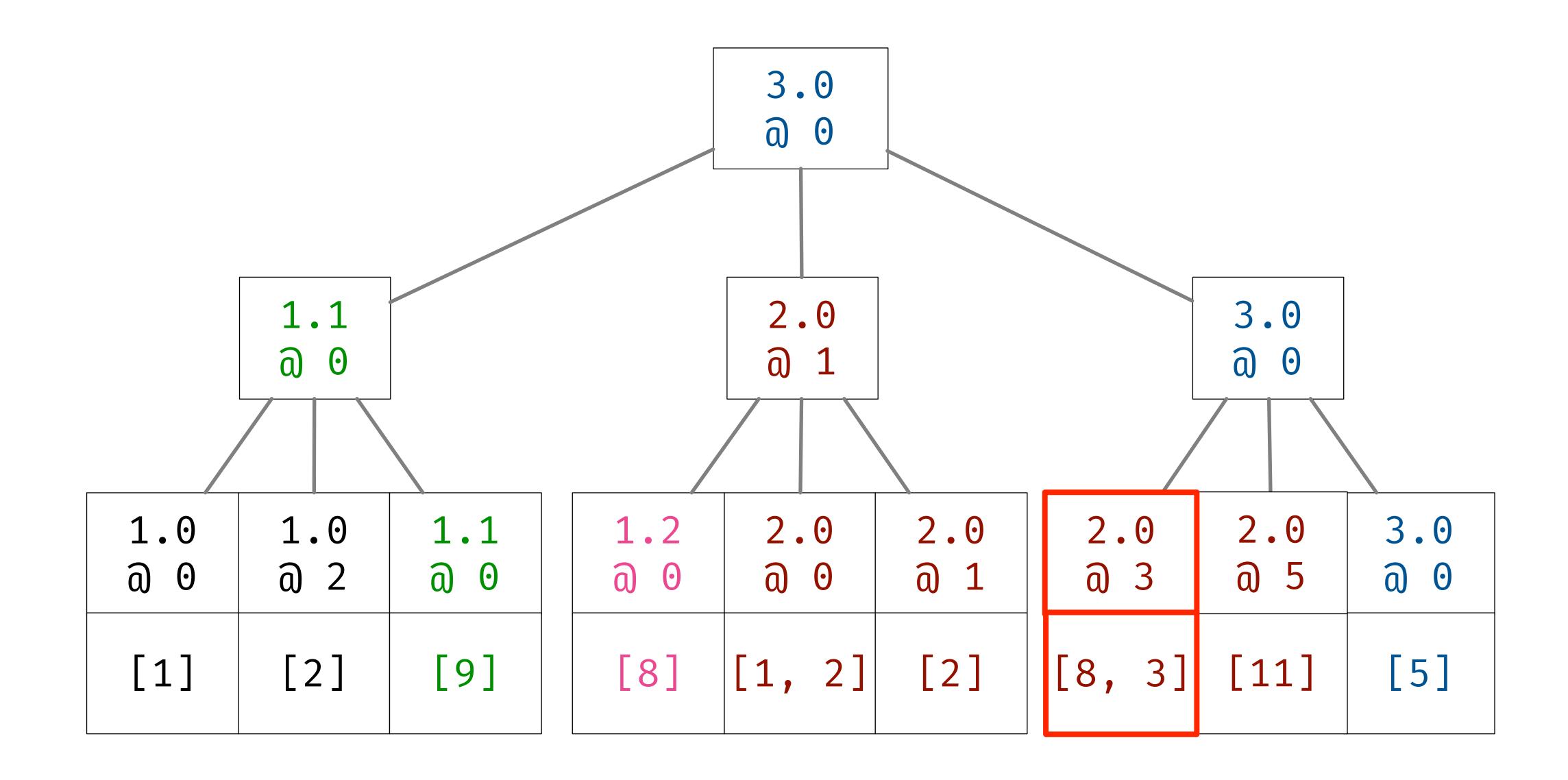
Insert "X" at 2.0 @ 4



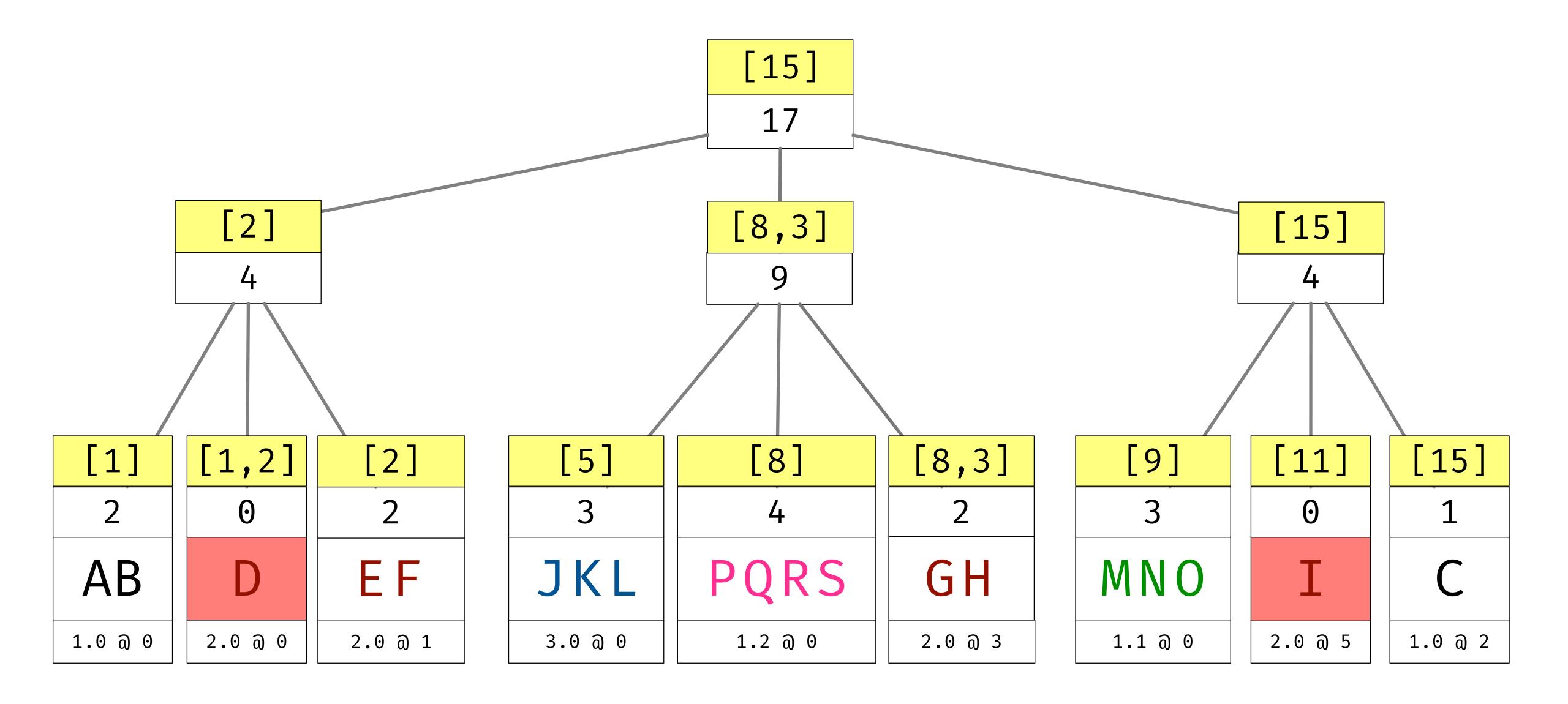
Insert "X" at 2.0 @ 4



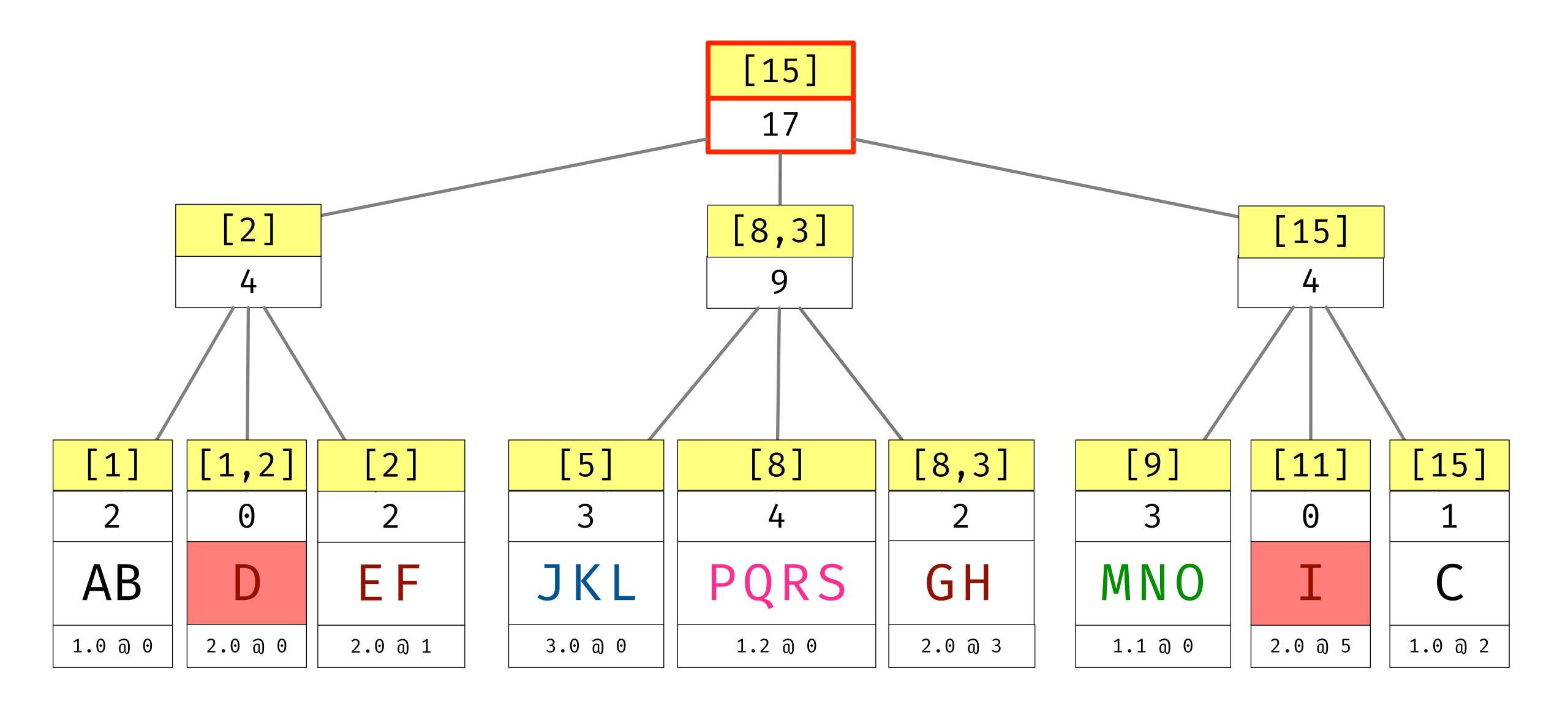
Insert "X" at 2.0 @ 4



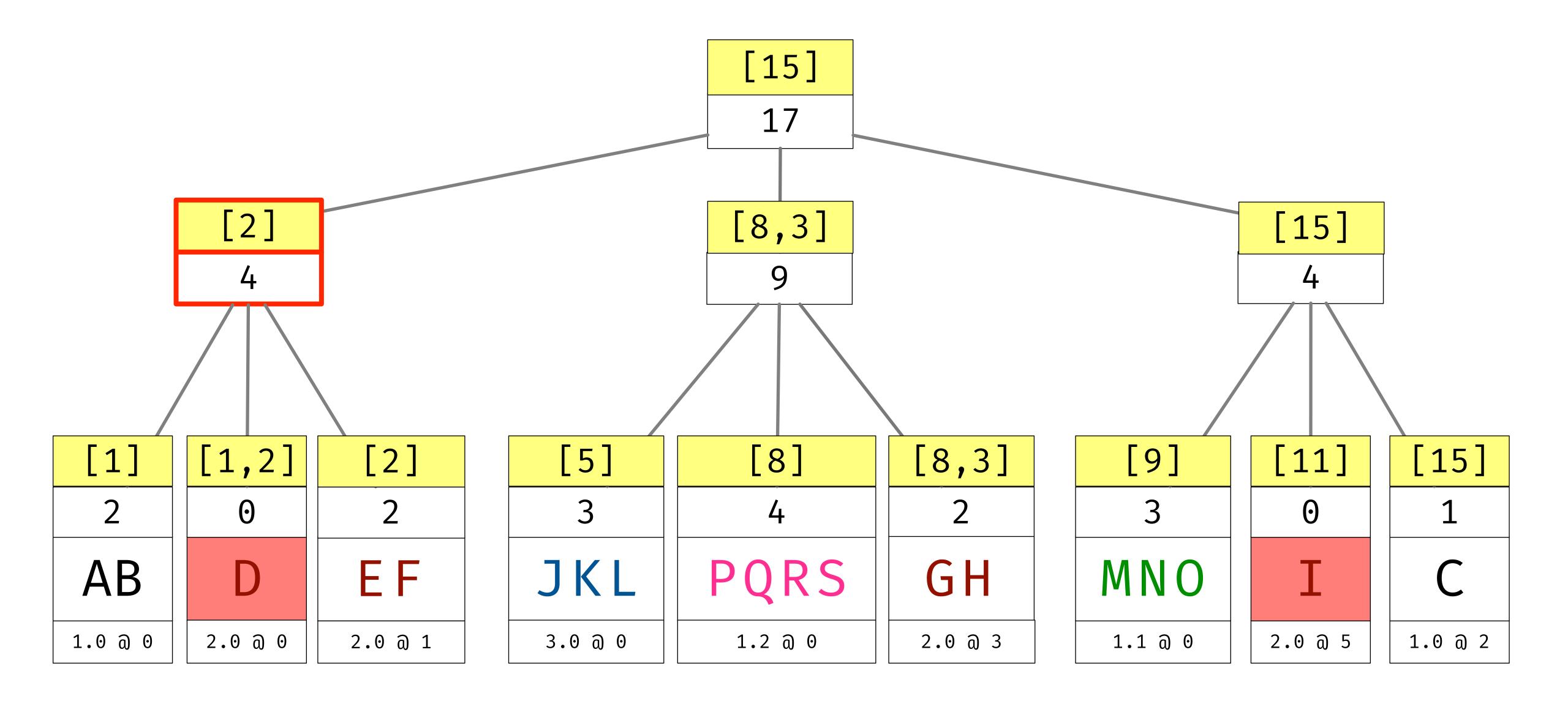
Insert "X" at [8, 3] @ 1



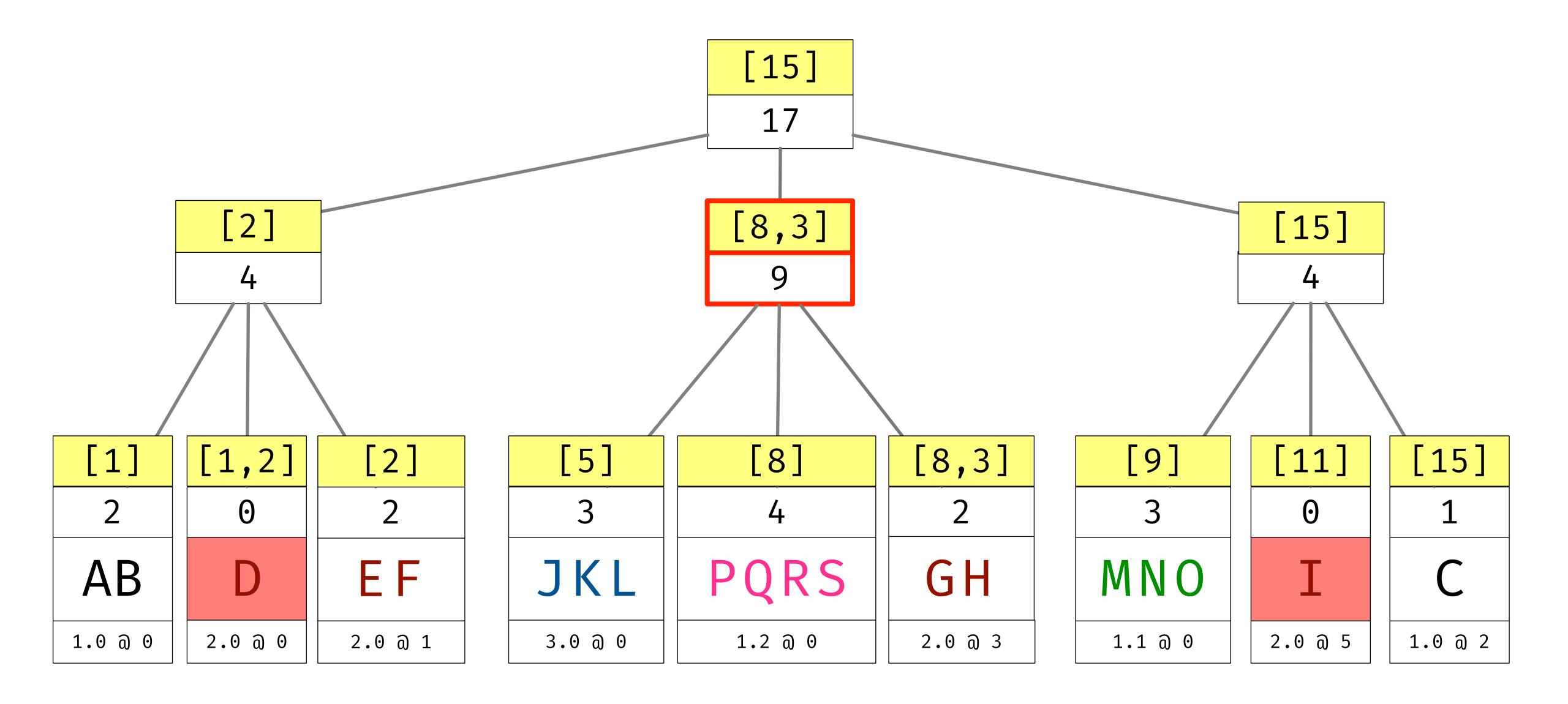
Insert "X" at [8, 3] @ 1



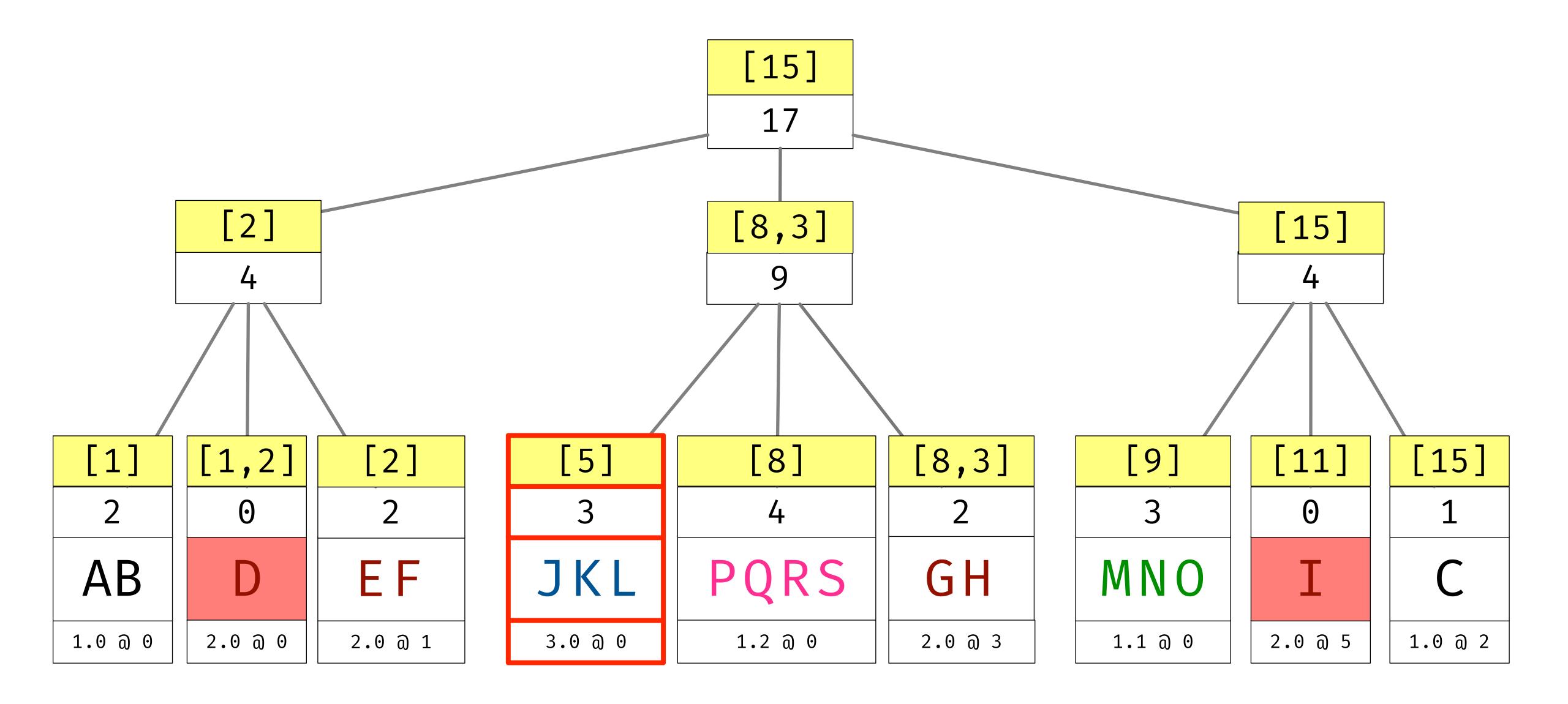
Insert "X" at [8, 3] @ 1



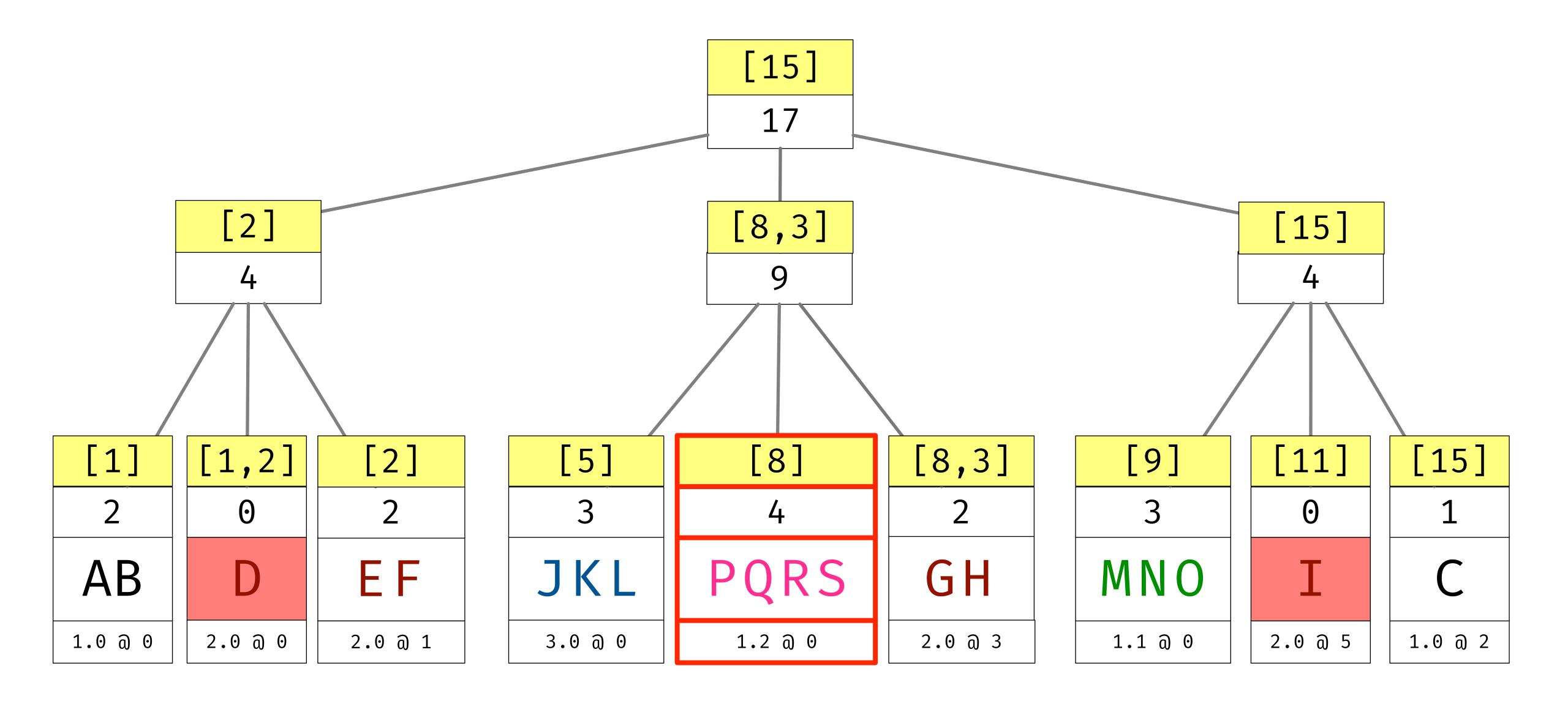
Insert "X" at [8, 3] @ 1



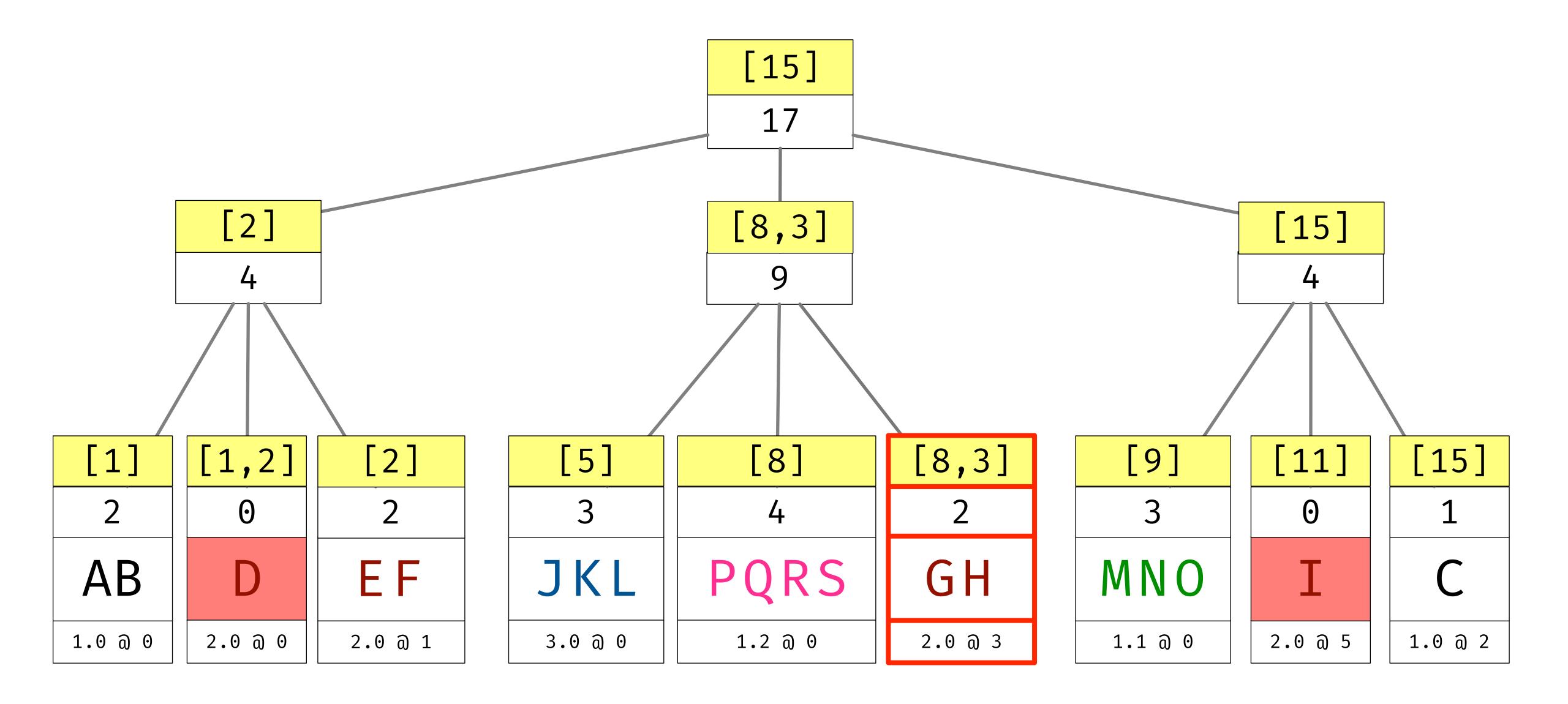
Insert "X" at [8, 3] @ 1



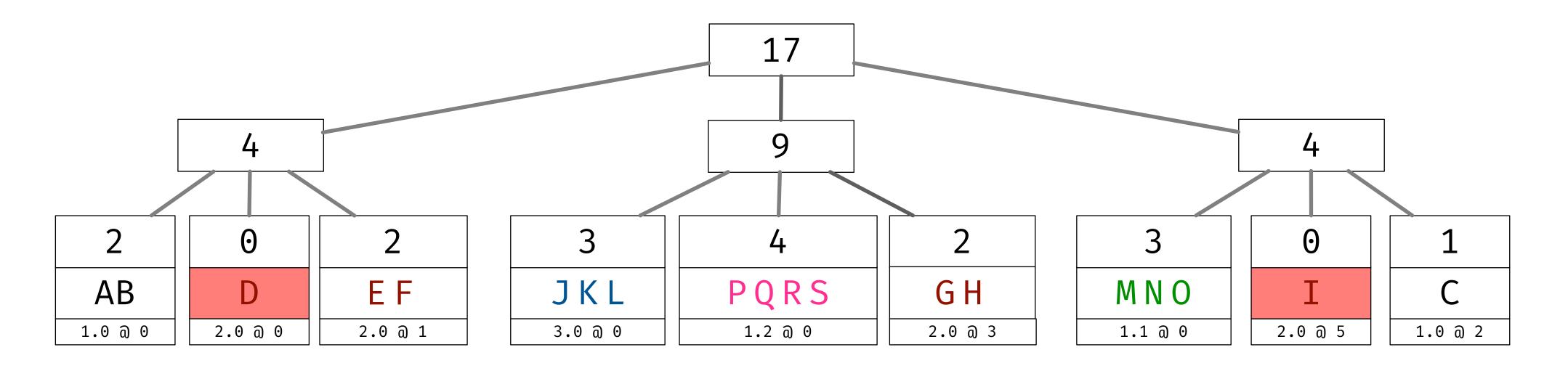
Insert "X" at [8, 3] @ 1



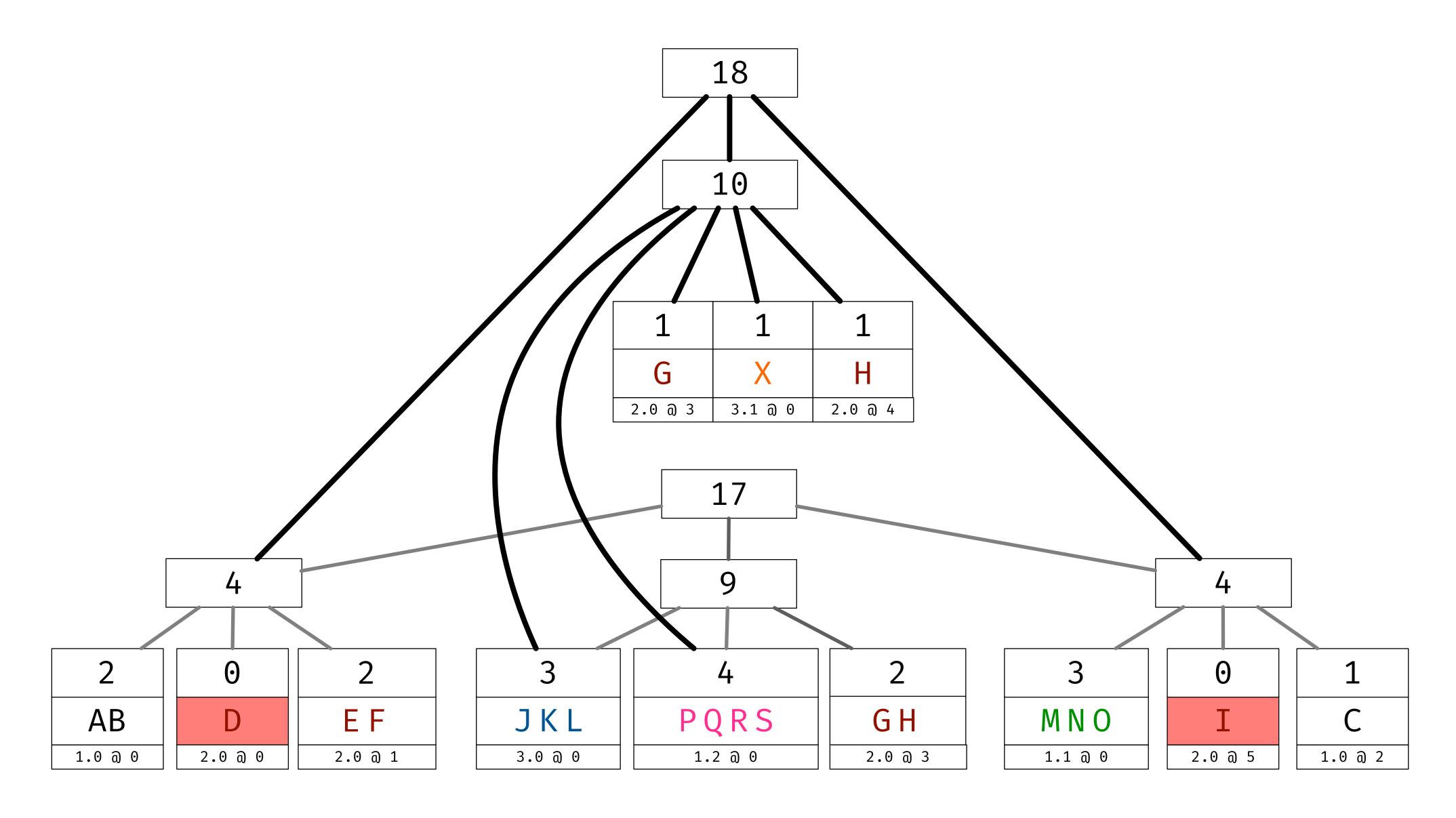
Insert "X" at [8, 3] @ 1



Insert "X" at [8, 3] @ 1



Insert "X" at 2.0 @ 4



Insert "X" at 2.0 @ 4

Buffer (v1)

Background Thread

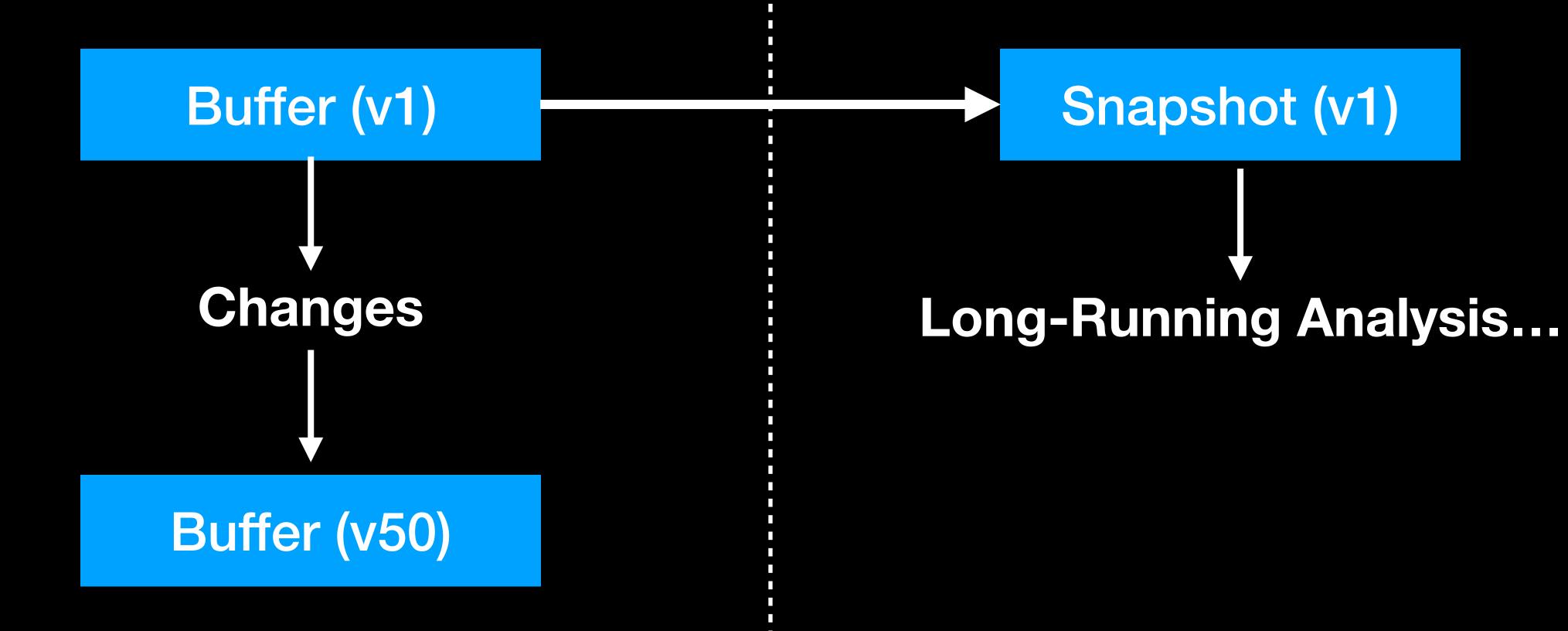
Background Thread

Buffer (v1)

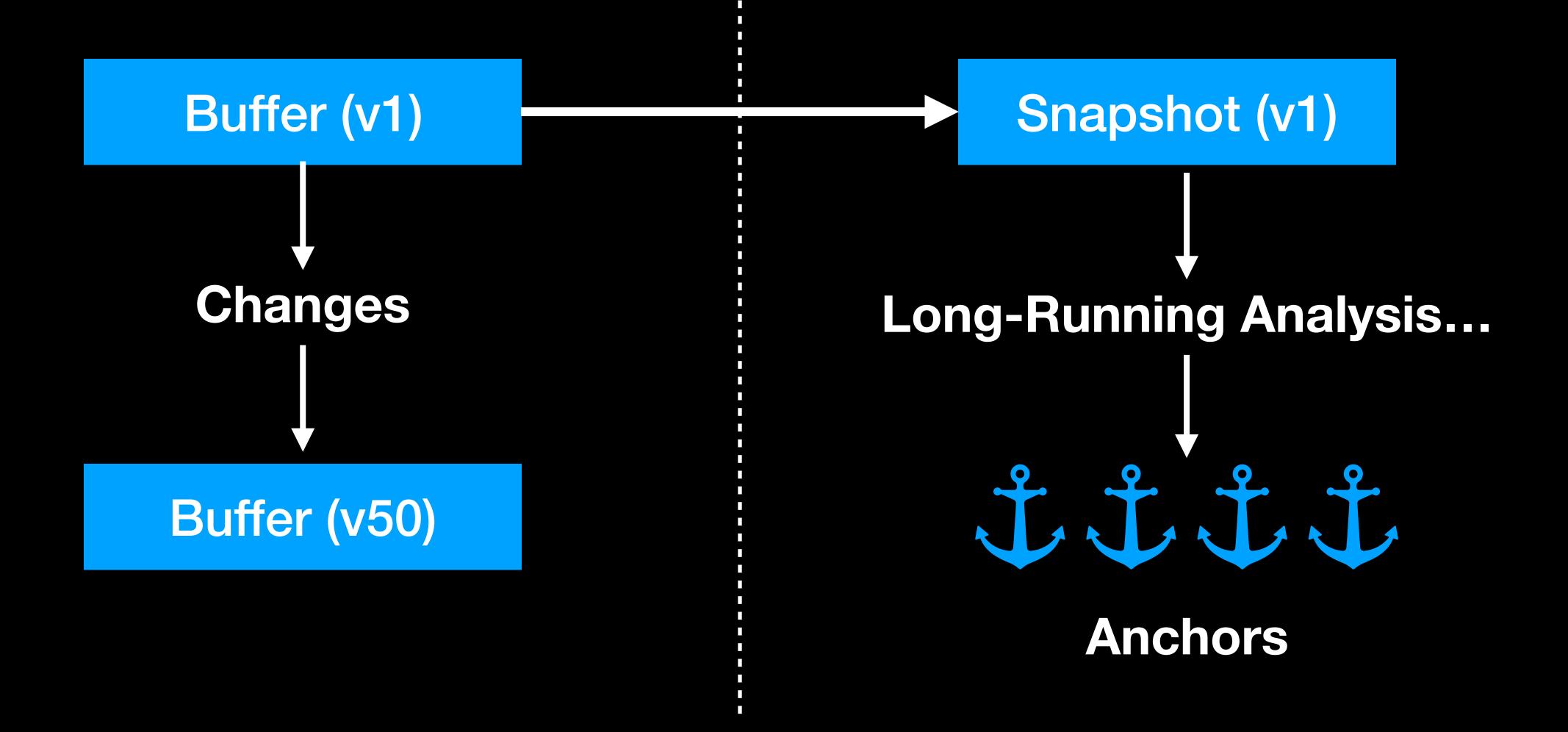
Snapshot (v1)

Foreground Thread Background Thread Snapshot (v1) Buffer (v1) Long-Running Analysis...

Background Thread



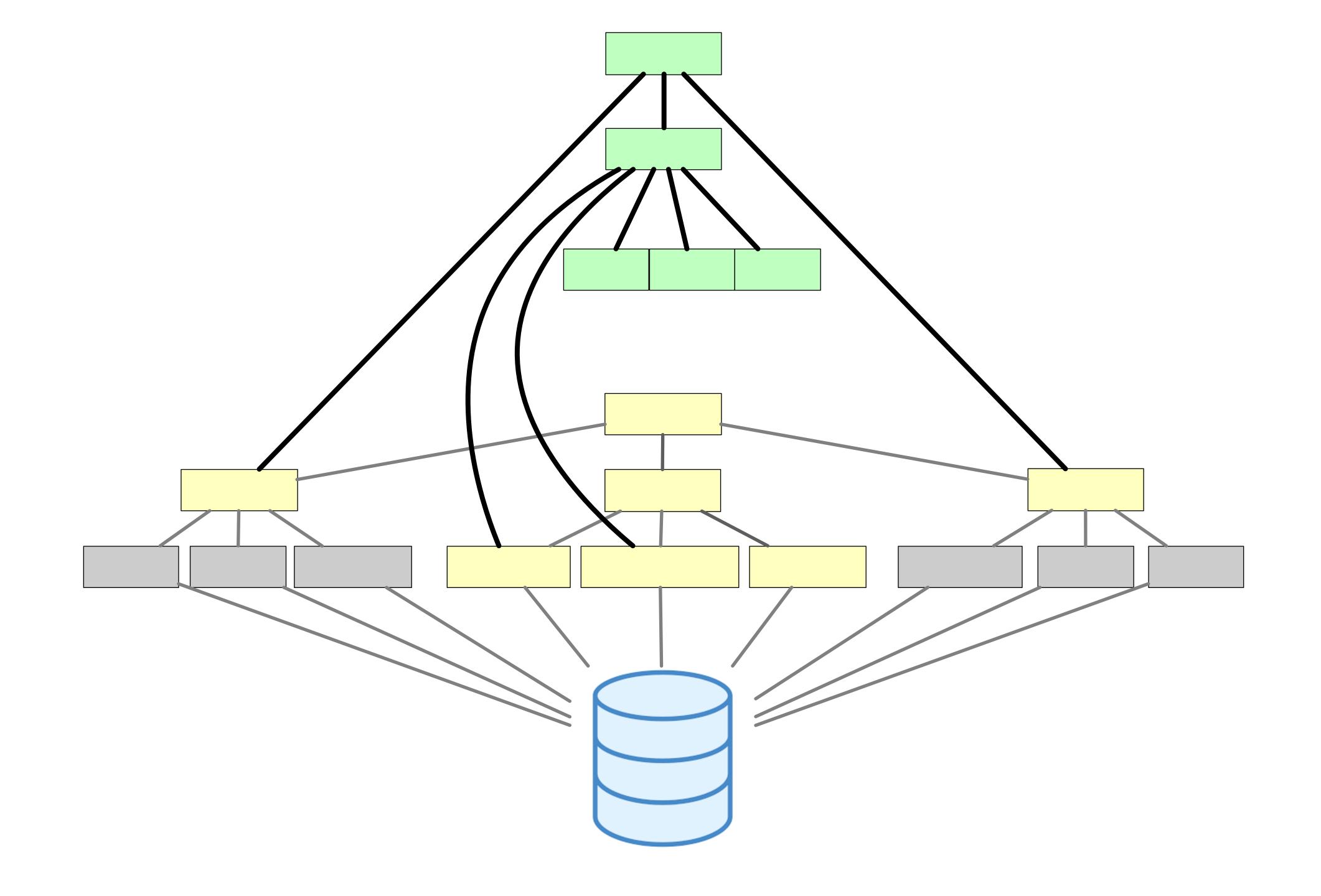
Background Thread

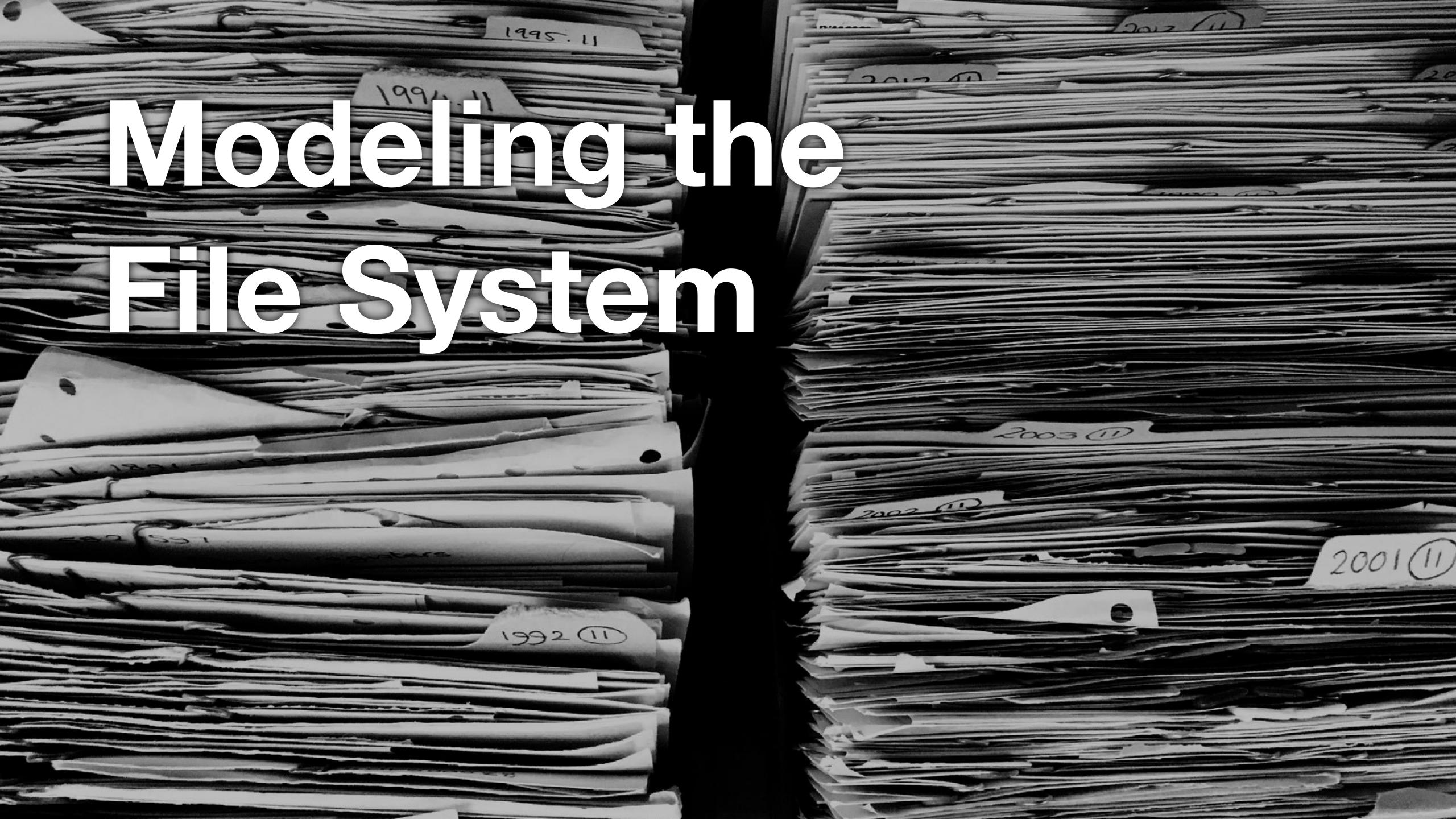


Foreground Thread **Background Thread** Snapshot (v1) Buffer (v1) Changes Long-Running Analysis... Buffer (v50) Anchors

Foreground Thread **Background Thread** Snapshot (v1) Buffer (v1) Changes Changes Buffer (v50) Operations

```
enum Tree<T: Item> {
    Resident(Arc<Node<T>>),
    NonResident(NodeId),
}
```





Site 1
Timeline 1.5

